

**DESIGN AND SIMULATION OF OPTIMUM DIGITAL FILTERS USING
LABVIEW**

Project report submitted in partial fulfillment of the requirement for the degree of

BACHELOR OF TECHNOLOGY

IN

ELECTRONICS AND COMMUNICATION ENGINEERING

By

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UNDER THE GUIDANCE OF

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DECLARATION

I hereby declare that the work reported in the B.Tech Project Report entitled “**Design and Simulation of Optimum Digital Filters using LABVIEW**” submitted at **Jaypee University of Information Technology, Wagnaghat, India** is an authentic record of my work carried out under the supervision of **Dr. Shruti Jain**. I have not submitted this work elsewhere for any other degree or diploma.



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This is to certify that the above statement made by the candidates is correct to the best of my knowledge.



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LIST OF ACRONYMS AND ABBREVIATIONS

IIR	Infinite Impulse Response
FIR	Finite Impulse Response
VI	Virtual Instruments
NI	National Instruments
DAQ	Data Acquisition
G-Program	Graphical Program
HP	Highpass
LP	Lowpass
BP	Bandpass
BS	Bandstop
PB	Passband
SB	Stopband
dB	Decibels
PLC	Programmable Logic
DLL	Dynamic Link Libraries
GPIB	General Purpose Interface Bus
FFT	Fast Fourier Transform
NF	Notch Filter.

LIST OF SYMBOLS

f_c	Cutoff Frequency
x_i	Input
y_i	Output
a_i	Filter Coefficients
n	Discrete Time Index
τ	Time Constant
a_k	Set of Reverse Coefficients
b_j	Set of Forward Coefficients
b_k	k^{th} Feedforward Taps
N_a	Numbers of Reverse Coefficients
N_b	Numbers of Forward Coefficients
N	Order
$\&$	And
β	Beta (Kaiser Window, side lobe attenuation factor)

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ABSTRACT

Digital filter design is a part of digital signal processing and it is essential to remove noise from any signal. The major issue regarding the implementation is the computational complexity that may cause difficulties in its practical applications. There is an approach for a designing of the digital filter using Laboratory Virtual Instrument Engineering Workbench (LabVIEW). It is extracted from the theoretical and experimental results that the design method with the help of window function is simpler and quite easy to use as compared to others because of the availability of a well-structured equation.

A Notch, High Pass and Low Pass filter is designed using different windowing techniques like Rectangular, Blackmann, Gaussian, Hamming, Kaiser, Hanning windows which are implemented using LabVIEW. The results were also compared using MATLAB in terms of magnitude response and frequency response. To remove the 50 Hz power supply interference from any of the biomedical signal Finite Impulse Response notch filter is designed, FIR and IIR High pass filter were designed to remove Baseline Wander noise and FIR and IIR Low pass filter were designed to remove high frequency noises such as EMG from any biomedical signals. The filter is designed on LabVIEW considering the order as 100, lower cut off frequency (f_{c1}) as 49 Hz, upper cut off frequency (f_{c2}) as 51 Hz for notch and lower cut off frequency (f_c) as 0.5Hz for High Pass, higher cut off frequency (f_c) as 100Hz for Low Pass filter with sampling frequency (f_s) is considered as 1000 Hz.

The work has achieved the target to remove various noise cancellation. Among all the filtering techniques FIR is proved best and among different windows the Kaiser window's results are well fitted and widely acceptable.

CHAPTER 1

INTRODUCTION

In the field of electronics engineering the processing of signals plays an important role which is purely based on synthesizing, modifying and analyzing, different signals such as images, sounds, and biological measurements. Signal processing is widely used to enhance the transmission, efficiency of storage, & subjective quality. Signals rise up in almost every field of engineering and technology. Two different categories of signals are classified as continuous signals and discrete time signals. A continuous-time signal is defined in such a way that it is present at each and every instant of time. Typical examples are a voltage waveform and the velocity of a space vehicle as a function of time. A discrete-time signal, on the other hand, is not a function of continuous argument. Examples of this type of signal can be Stock Exchange where the closing price of a particular product and the daily precipitation as function of time. The discrete time signals can be expressed like continuous time signals by a different kind of frequency function known as the frequency spectrum of the signal.

The process of reshaping, modification of signal frequency spectrum is known as filtering.

These objectives are :

- i. To put off the unwanted noises present in the signal.
- ii. To avoid distortion of signals due to transmission channel imperfection.
- iii. To separate the different signals which were purposely blended to maximize channel capacity.
- iv. To resolve signals into their frequency components.
- v. To get the desired output at the receiver side by demodulating the signals.
- vi. To limit the bandwidth of the signals.

1.1 CLASSIFICATION OF FILTERS

The filter is a electronic circuit which is efficient in allowing, amplifying and attenuating the frequencies altogether. Thus, a filter are able to get the essential frequency components from signals that also contain unwanted and irrelevant frequencies in the field of electronics, there are many useful applications for filters which includes:

- i. **Wireless communications:** Filters are capable to select the desired signals while eliminating all other signals .
- ii. **Direct Current suppliers:** To remove the undesired high frequencies which are considered as noise that are present in these suppliers and additionally it reduce ripple content from the power supply.
- iii. **Audio Signals:** In order to use different frequencies in different audio devises such woofers require audio of low frequencies, speakers need frequency in mid range .
- iv. **ADCs:** To minimize the aliasing effect the ADC are place in front of filters.

Filters can be classified as shown in Fig 1.1.

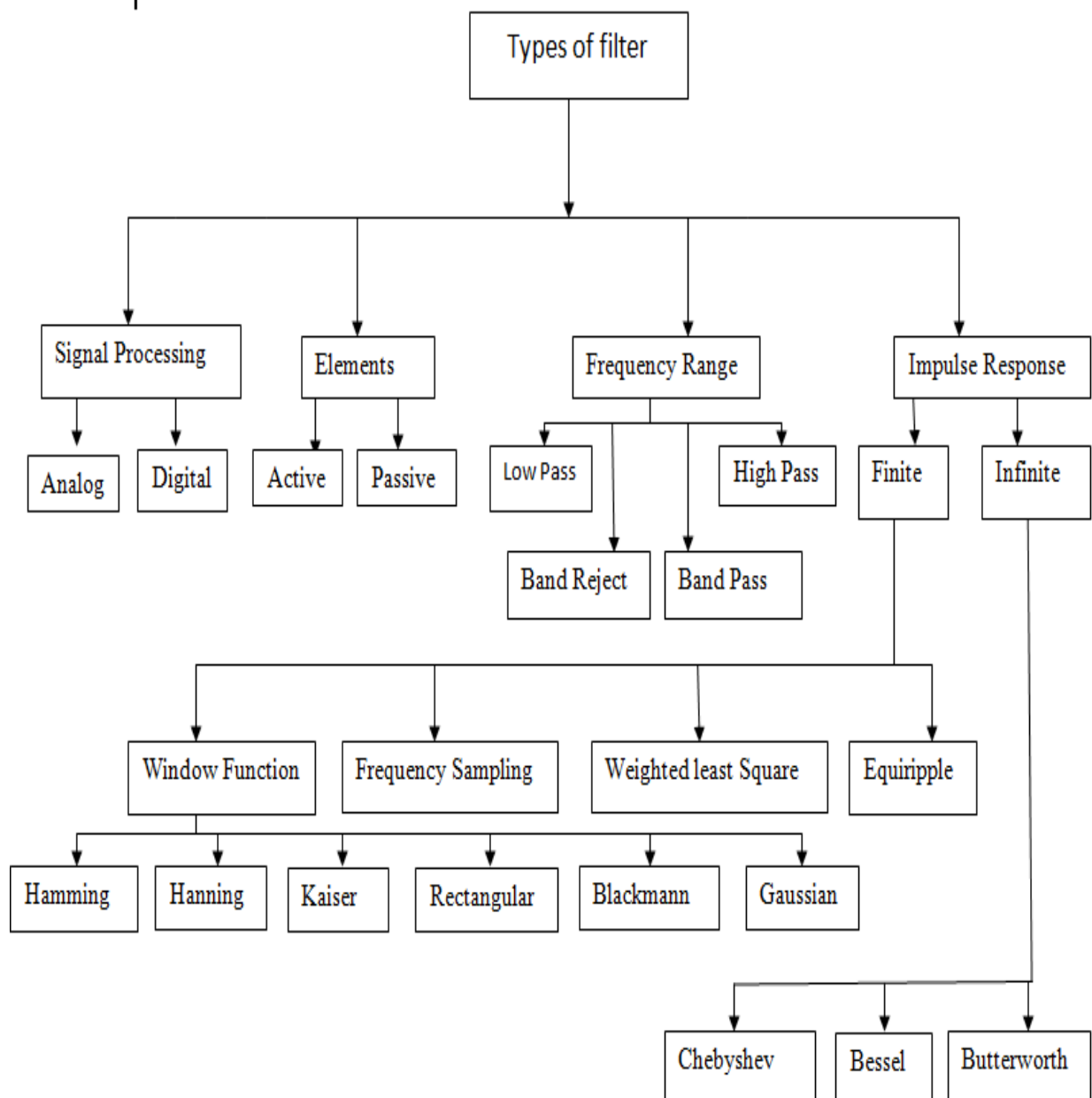


Figure 1.15 Block Diagram of Different types of Filter

Depending upon the type of signals the filters are further classified as:

Analog Filters: Analog filter is a type of system where the input and the output signals are continuous in nature whose block diagram of analog filter is shown in Fig. 1.2.



Figure 1.16 Analog Filter

Digital Filters: Digital filter is a kind of system which the input and the output are discrete-in nature whose block diagram of analog filter is shown in Fig. 1.3



Figure 1.17 Digital Filter

A comparative study between digital and analog filter is given in Table 1.1.

Table 1.1 Classification of Filters [1]

Sr. No.	Analog Filters	Digital Filters
1	The aim of analog filter is to filter out the signals whose input is continuous in nature and accordingly gives the continuous filtered output.	The aim of digital filter is to filter out the signals whose input is discrete in nature and accordingly gives the discrete filtered output.
2	For designing of analog filters the components such as resistors, capacitors and inductors are used	For designing of digital filters different units such as adders multipliers are used with help of software such as MATLAB LABVIEW.

3	Analog filters are less accurate and because of component tolerance of active components and more sensitive to environmental changes.	Digital filters are less sensitive to environmental changes, noise and disturbances. Thus periodic calibration can be avoided. Also they are extremely stable.
4	Difficult in Adjustment	Compared to analog Filter digital filters are more flexible because of software and programming.
5	Filter representation is in the term of System Components	Digital filters are represented by difference equation.
6	Not easily portable.	Easily portable.

Depending on the type of elements filters can further be categorized into two types : Active and Passive Filter.

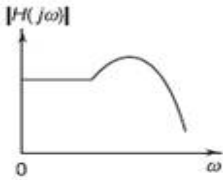
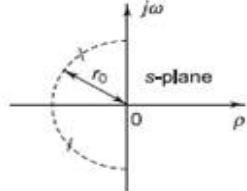
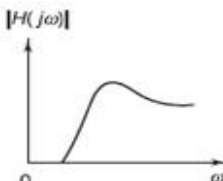
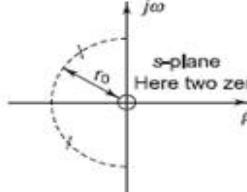
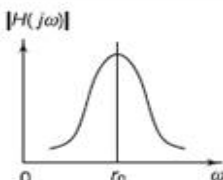
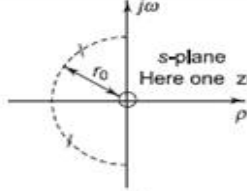
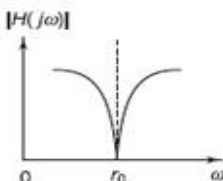
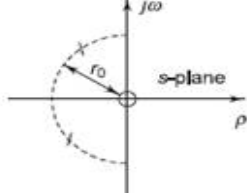
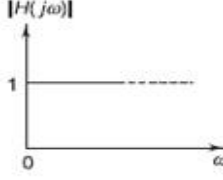
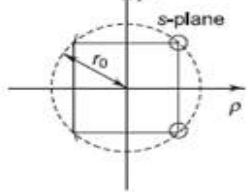
Active Filters: An active element namely Operational Amplifiers are widely used in Active filters. Resistors and capacitors are together used with Op-amps to get an appropriate filter response and this avoids the use of inductors. The performance of the filter is usually restricted because of some gain and bandwidth related issues with the use of Op-amp. Initially active filters were restricted to low frequencies which makes them suitable for filtering of video signals. The main edge of active filters over the passive one is that they are smaller in size and they can also be miniaturized further. But active filters have disadvantages too i.e. the active filter made up of op-amp which can add noise and limits the signal's amplitude and the supply voltage. Active filters are mostly used where there is frequent shift in the amplitude with respect to frequency.

Passive Filters: Resistors, capacitors and inductors are only used by the Passive filters. To pass a current of above 1 mA the Passive filters come into play and also in the area where it is required to design more specialized applications namely in high frequency filtering and where a wide frequency range is needed. One of the main advantages of passive filters is that they generally consume less power and this advantage of passive filters can be used in low power systems.

Along with the advantage there is some disadvantage of the Passive filter which is, the designing of passive filters use inductors which in turn makes the system little bulky. A the huge diameter wires are used to pass high currents the filters are designed in such a way which can cope up with the .magnetic flux. .With the help of resistors and capacitors network or the RC network can be used to construct simple analog high pass and low pass filter.

In the Table 1.2 , all poles and zeros are seen to be located on a circle of radius r_0 . This design was given by Butterworth therefore, is called *Butterworth Analog filter design*. Here Q is the quality factor of the circuit at resonance. In the pole-zero plots given in Table 1.2 location of poles and zeros are shown by cross (x) and circle (o) respectively.

Table 1. 2 Pole-Zero Configuration and Corresponding Frequency Responses of various kinds of Analog Filters [1]

Name of the analog filter	Its transfer function $H(S)$	Frequency response $H(j\omega)$	Pole-zero locations of $ H(j\omega) $
Low pass filter (LPF)	$\frac{r_0^2}{s^2 + \left(\frac{r_0}{Q}\right)s + r_0^2}$		
High pass filter (HPF)	$\frac{s^2}{s^2 + \left(\frac{r_0}{Q}\right)s + r_0^2}$		
Band Pass filter (BPF)	$\frac{(r_0/Q)s}{s^2 + \left(\frac{r_0}{Q}\right)s + r_0^2}$		
Band stop filter (BSF)	$\frac{s^2 + r_0^2}{s^2 + \left(\frac{r_0}{Q}\right)s + r_0^2}$		
All pass filter (APF)	$\frac{s^2 - (r_0/Q)s + r_0^2}{s^2 + \left(\frac{r_0}{Q}\right)s + r_0^2}$		

On the basis of different frequency range filter is classified as :

1. Low Pass
2. High Pass
3. Band Pass
4. Band Reject

Low Pass Filter: A series connection of single Resistor and Capacitor can turn into the designing of LP filter. In LP filter the input signal is applied to the combination of resistor and capacitor which are connected in series and the output signal is taken extracted through the capacitor. When the frequency of the signal changes the value of resistor does not change but the capacitor reactance changes according to the frequency there is an inverse effect of frequency. The capacitive reactance has a larger value as compared with the resistive value at the lower frequency which states that the voltage drop across the resistor is less as compared to the potential drop through the capacitor. For the high frequency the opposite is true i.e. potential drop through the capacitor is less than the voltage drop through resistor. Frequency response of LPF shown in Fig. 1.4.

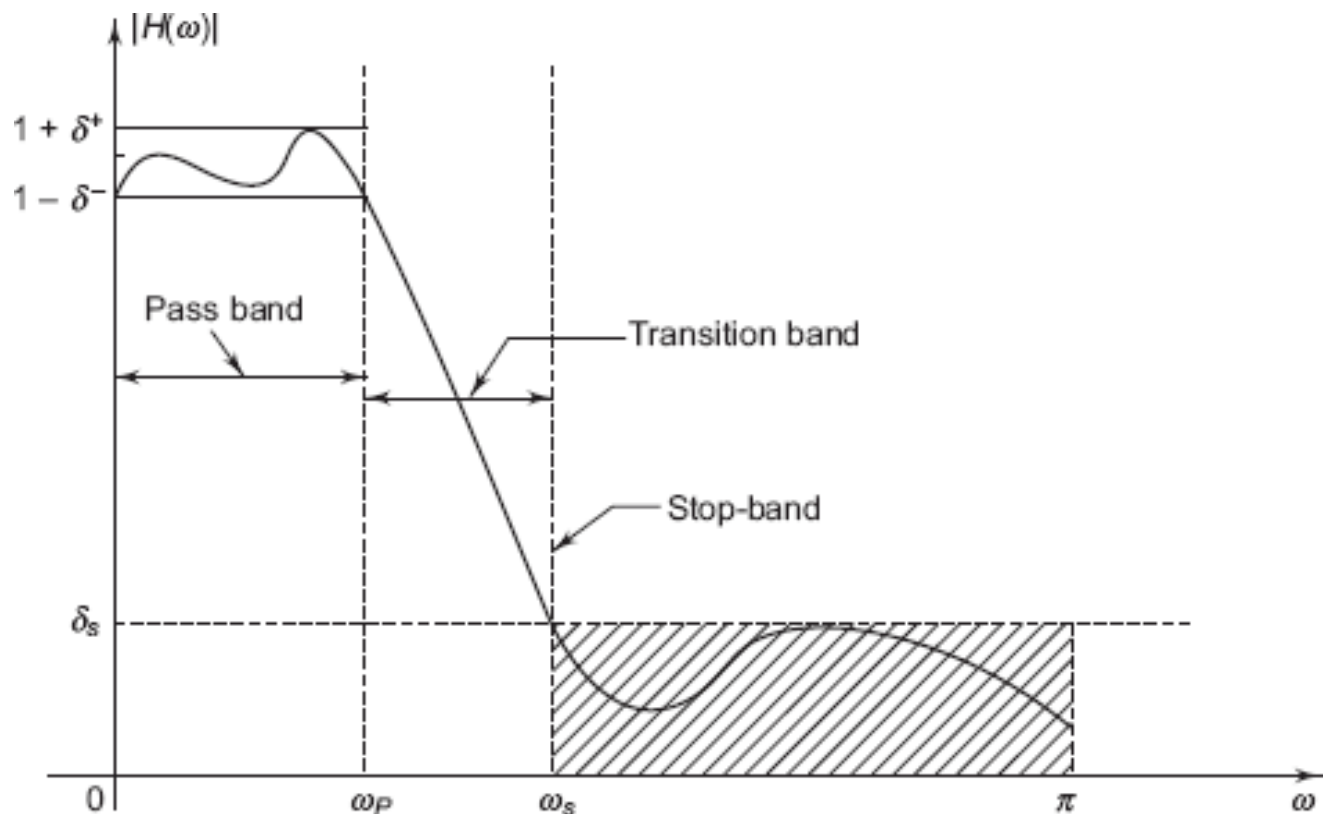


Figure 1.18 Low Pass filter specifications [1]

High Pass Filter : A HPF is considered to be the reverse case of the LPF. In this filter there is only change in the place of the components now in the high pass filter the output signal is taken through the resistor. HPF allows the signal to pass above the cutoff frequency f_c , which is opposite

of the LPF which passes the signal below f_c rejecting any signals at low frequency from the waveform. In the HPF case there is a reduction in capacitor reactance above the cutoff frequency this leads to the circuit behaving like short circuiting which allows the whole input signal to pass to the output side.. The response of the HPF is shown in Fig1.5

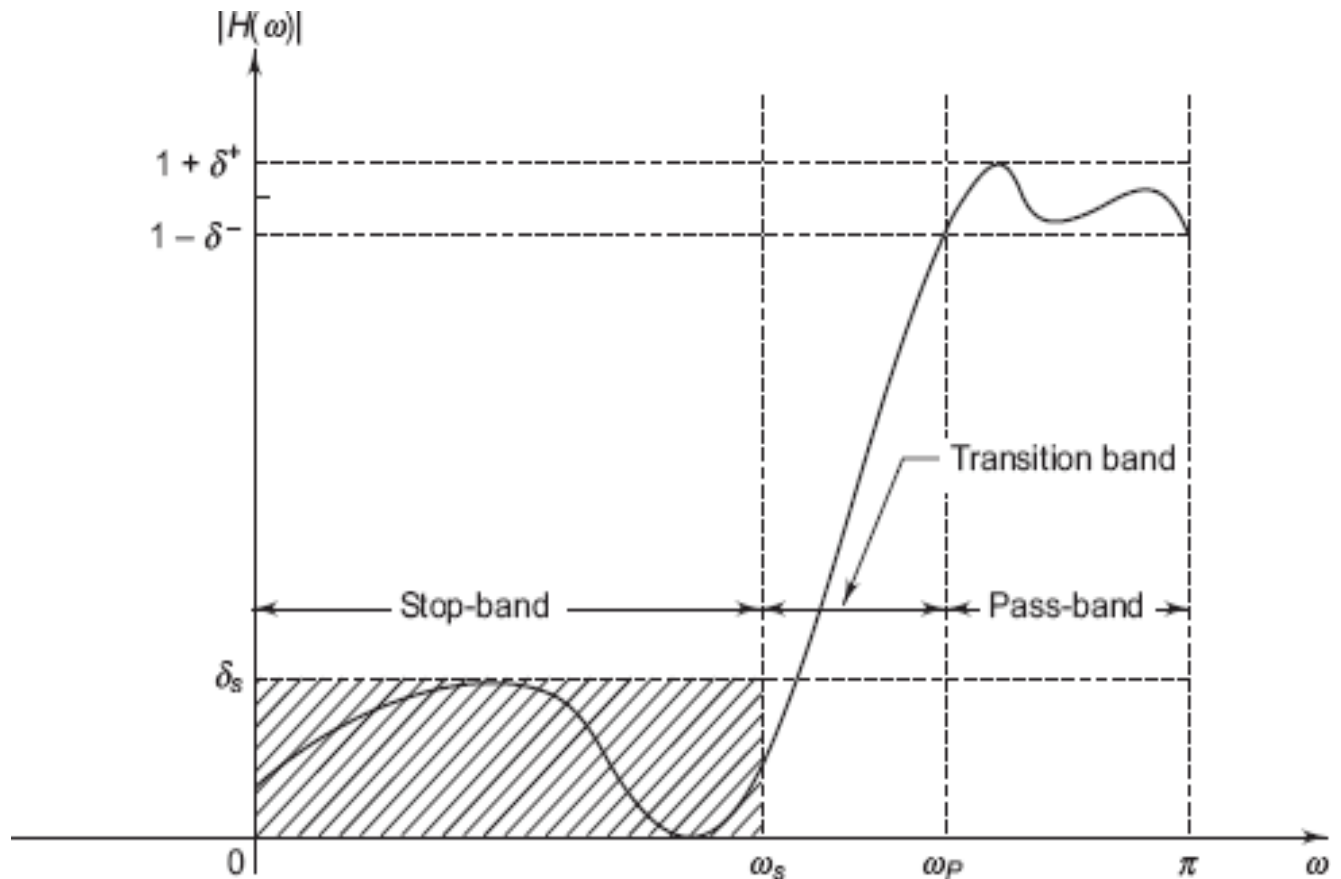


Figure 1. 19 High pass filter specifications [1]

Band Pass Filter : A BP filter s composed of LP and HP filter filter. The main task of BPF is to filter out certain range of frequencies within the given range.Using the help of resistors and capacitors the cutoff frequency of BPF can be easily controlled, provided they are connected n proper form.

Different kind of RC filter can be introduced by cascading a LP and HP filter together, which can allow a certain range of afrequencies which can either be anarrow band or wide band while dattenuating outside range. The passive filter which is frequency selective filters commonly known as BP Filter which allows the signals within a limited range of frequenzies without distroying input signal. A response of BPF is shown n Fig. 1.6.

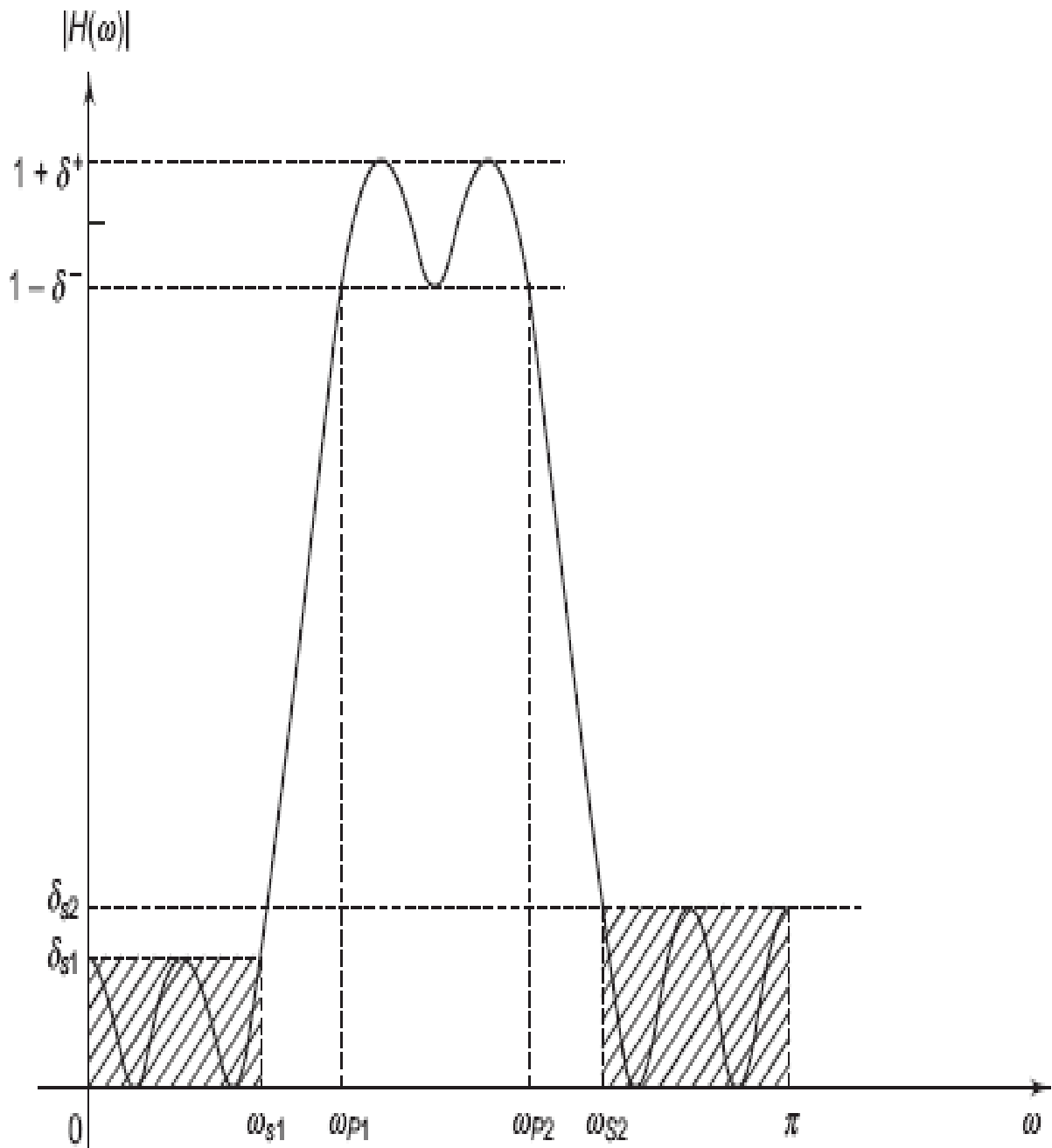


Figure 1.20: Band Pass filter specifications [1]

Band Stop Filter: A BS filter also commonly known as notch filter or the Band Reject filter which has the ability to reject the certain range of frequency components within the specified frequencies(f_{c1} and f_{c2}). This band stop filter, pass all frequency range within a specified frequency range. If the stop band is highly attenuated, then this band reject filter is most commonly called as a notch filter. The Notch Filter is a type of selective filter which functions opposite to the Band Pass Filter. BS filter consists of two cut-off frequencies(f_{c1} and f_{c2}), which are said to be half power point or -3dB points.

The bandwidth of the Band stop or Notch filter is defined because the difference in high frequency and low frequency ($f_H - f_L$). Because this filter out pass all the frequencies as much as f_L and all of the other frequency variety above f_H while blocking the range of frequencies within this low and excessive cutoff. The band prevent wide band filter attenuates any frequency that lies within the higher and lower -3dB points. In order to explain the characteristics of band pass filter the parameters which include f_L , f_H and f_C are determined to be equal, the motive is that the band prevent filter is the opposite case of the band skip filter out. Along with a lot of these parameters the definitions used for bandwidth, pass band, forestall band and center frequency are the similar as before, and awe can use the equal formulas to calculate bandwidth, f_C , and Quality Factor. The filter having an stop band of limitless attenuation and zero bypass band attenuation are termed as perfect band forestall filter. The frequency reaction of band stop filter out is shown in Fig. 1.7.

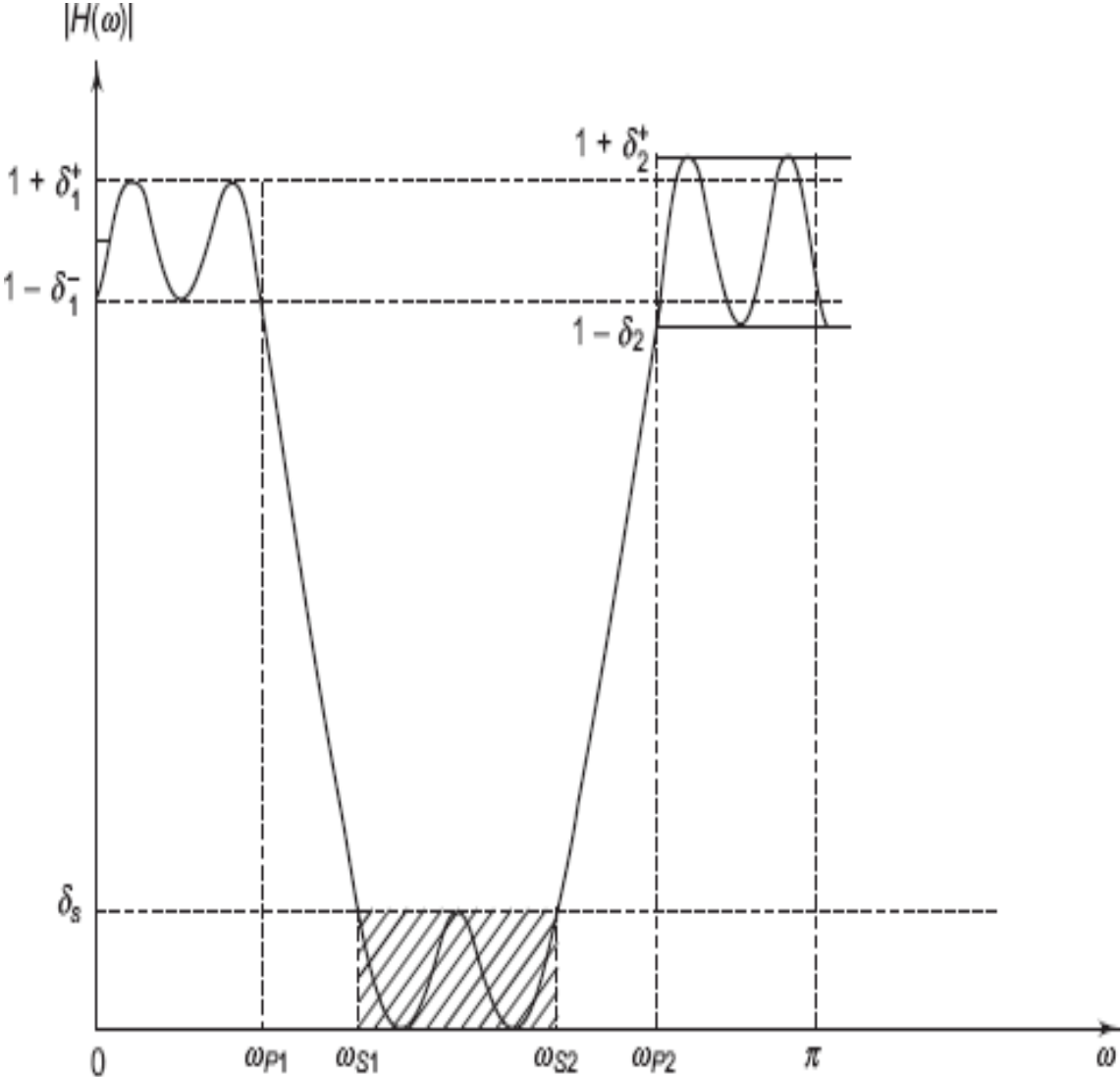


Figure 1. 21 Band stop pass filter specifications [1]

Further on the basis of Impulse Responses, filters are classified as Infinite Impulse Response and Finite Impulse Response. A comparison between IIR and FIR digital filter is given in Table 1.3.

Table 1. 3 Difference between FIR Digital Filter and IIR Digital Filter [1]

S.NO	FIR	IIR
1.	Generally known as Finite Impulse Response	Generally known as Infinite Impulse Response
2	This type of filter is non recursive in nature	This is recursive in nature
3	Stable	Unstable
4	Also known as All Zero filter	There is presence of both poles and zeroes
5.	Limited memory	Infinite memory

For the requirement of exact linear phase application the FIR filters are mainly used. The non-recursive way of filter implementation can make the filter stable, this filter designing basically consisting of two components:

- i. Approximation Stage
- ii. Realization Stage

In the approximation stage first it draws up the specification and accord a transfer function via these four steps.

- i. The proper filter length is chosen.
- ii. From the best suited filter transfer function the optimum function is chosen.

After the approximation stage the main task is to choose a suitable structure to get the transfer function. There are basically two famous methods which are:

- i. windowing techniques
- ii. frequency sampling method

The Windowing techniques

In this technique, [2], [3], [4] $H_d(w)$ is calculated with the help of given equations.

$$h_d(n) = \frac{1}{2} \int_{-\pi}^{\pi} H_d(w) e^{jwn} dw \quad (1)$$

where

$$H_d(w) = \sum_{n=-\infty}^{\infty} h_d(n) e^{-jwn} \quad (2)$$

The process of $h_d(n)$ truncation to length $M - 1$ is quite same as multiplying rectangular window with $h_d(n)$ using the Eq. (3)

$$\begin{aligned} w(n) &= 1 && 0 \leq n \leq M-1 \\ &= 0 && \text{otherwise} \end{aligned} \quad (3)$$

Thus the unit sample response of the FIR filter expressed by Eq. (4)

$$\begin{aligned} h(n) &= h_d(n) w(n) \\ &= h_d(n) && 0 \leq n \leq M-1 \\ &= 0 && \text{otherwise} \end{aligned} \quad (4)$$

The convolution of $H_d(w)$ with $W(w)$, is similar to the convolution $h_d(n)$ with the window function $w(n)$.

$$W(w) = \sum_{n=0}^{M-1} w(n)e^{-jwn} \quad (5)$$

The response of the filter obtained after the convolution of $H_d(w)$ with $W(w)$

$$H(w) = \frac{1}{2\pi} \int_{-\pi}^{\pi} H_d(v)W(w - v)dw \quad (6)$$

$H(w)$ can also be calculated using eq.7

$$H(w) = \sum_{n=0}^{M-1} h(n)e^{-jwn} \quad (7)$$

Due to the direct truncation of sample impulse response arises the problem of Gibbs phenomenon effect which produces certain discontinuities and ringing effect on the response. Using Eq. 7 the obtained response contains ripples which can be minimized by multiplying window function which have the taper response and decays gradually towards zero because in case of rectangular window function there is abrupt change rather than multiplying the rectangular window function with sample impulse function. By using the windowing method the result of frequency response are as follows:

- (i) The main lobe width is related to the width of the transition bands the window function.
- (ii) The width of main lobe decreases as the filter length increases and it also increases the ripple content.
- (iii) The ringing effects in the frequency response easily be eliminated with the help of window function

Some of the commonly used windows [3] are Bartlett triangular window , Generalized cosine windows

i. **Bartlett window:**

$$\begin{aligned}
 W(n) &= \frac{2(n+1)}{N+1} & n &= 0,1,2,\dots,\frac{N-1}{2} \\
 &= 2 - \frac{2(n+1)}{N+1} & n &= \frac{(N-1)}{2},\dots,\dots,N-1 \\
 &= 0, \text{ otherwise} & &
 \end{aligned}
 \tag{8}$$

ii. **Generalized cosine windows (Rectangular, Hanning, Hamming and Blackman)**

$$\begin{aligned}
 W(n) &= a - b \cos\left(\frac{2p(n+1)}{N+1}\right) + c \cos\left(\frac{4p(n+1)}{N+1}\right) & n &= 0,1,2,\dots,N-1 \\
 &= 0 & & \text{otherwise}
 \end{aligned}
 \tag{9}$$

The four unique forms that are mostly used by the general cosine window which are acknowledged by parameter a, b and c

Table 1. 4 Value of Coefficients a, b and c from

Windows	a	b	c
Blackman	0.41	0.6	0.07
Hamming	0.5	0.5	0
Hanning	0.54	0.46	0
Rectangular	1	0	0

iii. **Kaiser window with parameter β :**

$$\begin{aligned}
 W(n) &= \frac{I_0(\beta \sqrt{1 - (\frac{2(n+1)}{N+1})^2})}{I_0\beta} & n &= 0,1,\dots,N-1 \\
 &= 0 & & \text{otherwise}
 \end{aligned}
 \tag{10}$$

The overshoot value is comparatively reduced with the help of Bartlett window but there is a significant increase in the transition region. In order to provide a smooth truncation of the filter's frequency response the more complicated cosine functions are used by the Hanning, Hamming and Blackman windows. Among all the windows the Kaiser window is considered better of all only because of the shape parameter β which allows reduction in ripples and transition width spreading.. There are lot many methods but due to the ease of use because of well structured equations for calculating window coefficients the window methods are chosen.

The following problems arise by using window methods in filter designing are:

- (i) This method is appropriate only if Eq.(1) can be evaluated and the function $H_d(w)$ is absolutely integrable .The evaluation of $h_d(n)$ becomes tedious when it is difficult to get put mathematical expression and $H_d(w)$ is quite complicated.
- (ii) Since the use of windowing technique use to minimize the discontinuities in the frequency response of the filter.
- (iii) For the designing of any kind of filters this windowing technique is basically useful and also useful in the applications such as image and speech processing applications.

Frequency Sampling Technique

Using this technique, [2], [3], [4] the filter coefficient easily be calculated using the IDFT formula and the desired frequency response can be obtained.

$$h(n) = \frac{1}{N} \sum_{k=0}^{N-1} H(k) e^{j(2\pi n/N)k} \quad (11)$$

With the interpolation of sampled frequency the N point filter response is obtained response the continuous frequency response is calculated using the above N-point filter response. The error of approximation would be finite in frequencies between them and tends to zero at the sampling

frequencies. As smaller as the the error frequency response will be more smoother. If the frequency sample increases the errors will get reduced [3].

IN [4] a suitable method is discussed which is purely based on this sampling technique.

- (i) Using N number of samples the desired magnitude response is obtained.
- (ii) The desired response of filter is obtained with the given N values of H_k and by calculating the inverse FFT $h(n)$ is further calculated.
- (iii) According to Rabiner, when N varied from 15 to 256, 16 to 1 interpolation can be used and $16N$ samples of $H(w)$ lead to reliable computations.

Frequency sampling technique advantage

- i. Just like windowing technique this method is very flexible to be used in any type of magnitude response.
- ii. Easier to understand and implement.

The main drawback of using this technique is the use of sampled points which creates discontinuities in the desired frequency response

1.2 SOFTWARE USED FOR SIMULATION

1.2.1 LABVIEW : It is a virtual environment especially designed for educational purpose industrial experiments and automation applications which is purely based on graphical programming, in respect to textual programming however, textual programming is also supported in Lab VIEW. For the visualization and designing of different formulas and parameters Lab VIEW supports large number of functions for such applications. It supports other built in functionality which is useful for further applications such as for presentation of data its acquisition, instrument control and most important measurement

analysis. Another advantage of this Lab VIEW software is that it reduces the difficulty of other development platform by providing the flexibility of a powerful programming language support environment. Lab VIEW supplies substantial accession, analysis, demonstration and inspection competencies in a single platform, so that it will be ease to the user to choose various inputs on the same platform. Unlike other programming languages, Lab VIEW software provides functionality specifically which is centered to the use of automation applications, measurements control, development process. Lab VIEW provides all necessary units which are useful in engineering aspects for designing and testing purpose. The Lab VIEW graphical development environment gives powerful tools to create applications without writing any lines of text based code. With Lab VIEW, one can drag and drop pre-built objects to quickly and simply create user interfaces for the application. Then, one can specify system functionality by assembling block diagrams a natural design notation for scientist and engineers. Lab VIEW has tight Integration with lots of Instruments and Measurement gadgets and introduced seamless connectivity with dimension hardware, in an effort to quickly configure and use truly any measurement device, consisting of the entirety from stand-by myself devices to plug-in information acquisition devices, motion controllers, photograph acquisition structures, and programmable logic controllers (PLCs).

Lab VIEW has open connectivity with Other Applications and furthermore, Lab VIEW can assist you to connect with other applications and percentage records thru ActiveX, the Web, DLLs, shared libraries, SQL, TCP/IP, XML, OPC, wireless verbal exchange and different techniques. Lab VIEW's open connectivity permits you to create open, bendy applications which can talk with other applications across your enterprise.

With Lab VIEW, one can expand systems that meet even the maximum traumatic overall performance requirements across a ramification of platforms consisting of Windows, Macintosh, UNIX, or real-time systems. Lab VIEW additionally includes conventional program improvement tools. You can set breakpoints, animate program execution to look how the program executes through this system to make debugging and application improvement easier.

Purpose of using Lab VIEW

The use of LAB VIEW software allows user to develop their own solution for engineering problems. Along with this it gives student the freedom to perform and analyze powerful programming without any complexity and difficulty.

It provides a economical aspect to implement programs and algorithms. The use of Lab VIEW is to design systems and programs where system development time can be reduced and productivity of system gradually increases. Lab VIEW also provide user the flexibility to their users, to give their valuable feedbacks related to the product, and along with powerful toolkits add on.

Working of Lab VIEW Software

Laboratory Virtual Instrument Engineering Workbench commonly known as Lab VIEWL. It has several physical instruments such as voltmeter, millimeters and oscilloscope etc. and the operation of such instruments are just like the physical one and sometimes they are called virtual instruments, or simply as Vis. The user inputs gets manipulated by the functions of VI and the corresponding output is displayed.

The three main components a VI contain:

- i. **The Front panel:** Front panel is directly connected to the user here user can manipulate the inputs and corresponding output can be seen
- ii. **Block diagram panel:** The backbone of Lab VIEW where the codes or the blocks of particular function is arranged.
- iii. **Tools and connector Palette:** These Palettes supports the VI, which contains essential blocks and tools which are required for the implementation of VI.

Front Panel: Using the front panel user can give the inputs and can control different indicators and along with this output can also be observed here. This panel consists of interactive controllers unit for the input purpose and for the output purpose it includes several graphs and indicators respectively. Controllers used in the front panel consists of dials, pushbuttons and many more units are the indicators in Lab VIEW. Indicators are used for the output measurement and indications depicted in fig 1.8

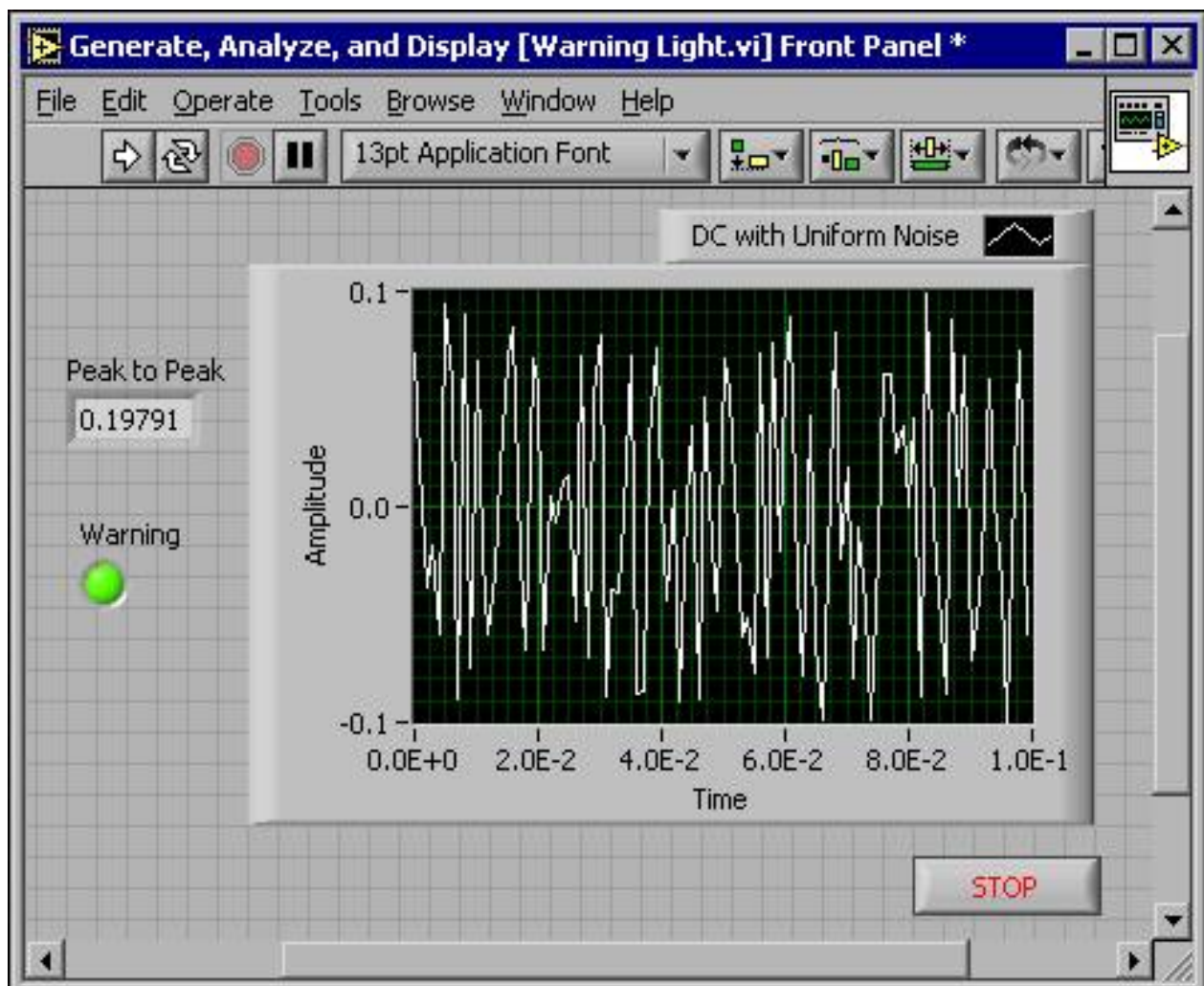


Figure 1. 22 Front panel

The front panel mainly contains of following:

1. Input probe(Control Unit)
2. Output probe (Indicator).

The input devices such as push button, dials and knob are the control unit which alters the input. The block diagram of the VI are purely rely on the input controllers as they gets the initiation from the input probe connected to it. After the input the block diagram is connected to the output probe such as graphs LEDs and other displaying devices depends on the user's need.

Block Diagram: The block diagram unit of Lab VIEW incorporates with the VI source code. This unit gives you the flexibility to create and modify a VI. The block diagram contains different objects such as sub VIs different structures and wires which is the key to connect to next block. Block diagram is shown in Fig1.9.

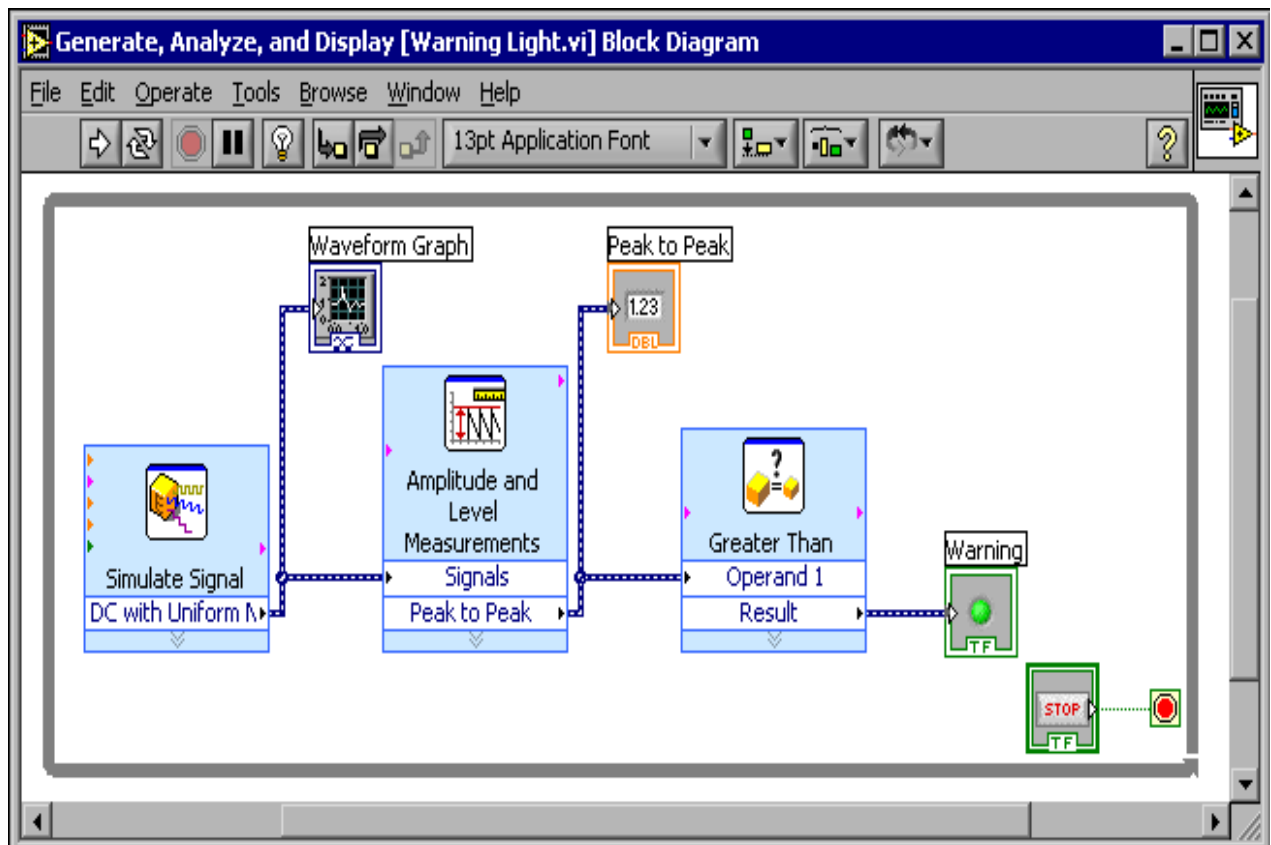


Figure 1. 23 Block diagram

Palettes: This option of Lab VIEW gives the flexibility to edit and modify block diagram and front panel.

Tools Palette: The block diagram and the front panel Tools palette each has the selection for this tool palette. Select the Window then Show Tools Palette to show the Tools palette. You can vicinity the Tools palette everywhere at the screen. If computerized device choice is enabled and also you pass the cursor over items at the the front panel or block diagram, Lab VIEW robotically selects the corresponding tool from the Tools palette Shown in Fig1.10.

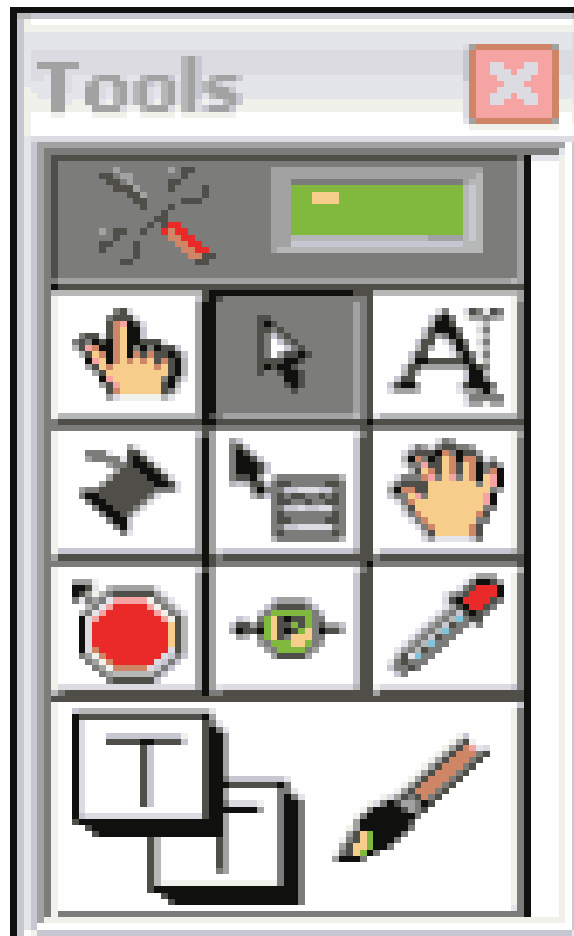


Figure 1. 24 Tool palette

Controls Palette: The Controls palette is available best on the front panel. The Control palette contains the controls and signs you use to create the the front panel. Select the Window then click

on on display controls palette or actually do proper-click on anywhere at the front panel workspace to get the Controls palette. The Controls palette is proven in Fig1.11.

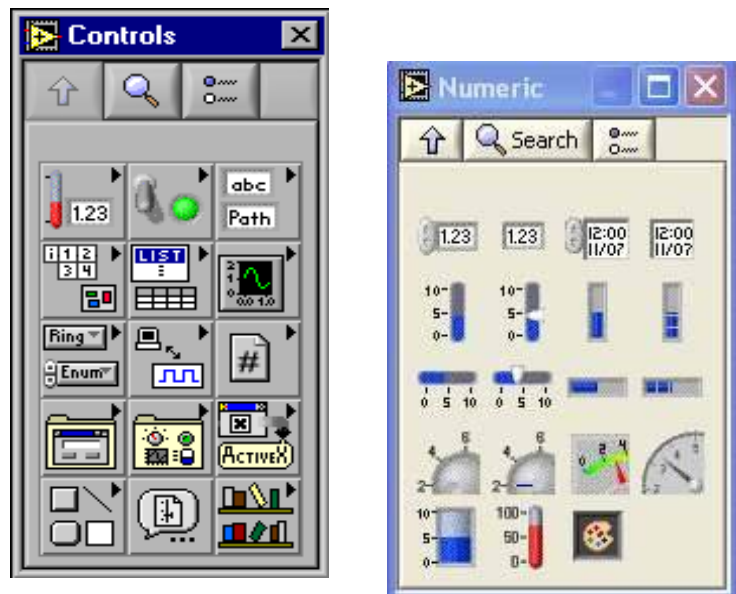


Figure 1. 25 Control Palette

Functions Palette: The block diagram unit of Lab VIEWS ha only the option of functions palette. The Functions palette contains all necessary blocks needed to build the block diagram. Simply right-click anywhere on the block diagram workspace to get the Functions palette or go to the Window option then choose functions palette which can be placed anywhere on the screen.

1.2.2 MATLAB: Matrix Laboratory or generally called as MATLAB is commercially available programming available environment generally used for the mathematical computation, which also include MathCAD, Maple and Mathematica. This software is purely based on the matrix based calculations. Out of the different mathematical environment tool none of them can be considered best each one has its own strengths and weaknesses and allows performing basic computations. The only difference in these tools is its function to handle complicated mathematical and symbolic calculations. For example, the Maple tool is good for doing symbolic calculations where as the Matrix Laboratory is efficient for computations involving matrices. In most of engineering applications the Matrix Laboratory is widely used for the calculation than to the traditional computer programming. Although programs inclusive of MATLAB turn out to be widespread tool for engineers and scientists, this doesn't mean that you shouldn't learn a high-level language such as C++, JAVA, or FORTRAN.

Because MATLAB is so easy to use, you can perform many programming tasks with it, but it isn't always the best tool for a programming task. It excels at numerical calculations—especially matrix calculations—and graphics, but you wouldn't want to use it to write a word-processing program. For large applications, such as operating systems or design software, C++, JAVA, or FORTRAN would be the programs of choice.

The primary area of overlap between MATLAB and high-level programs is “number crunching”—repetitive calculations or the processing of large quantities of data. Both MATLAB and high-level programs are good at processing numbers.

A “number-crunching” program is generally easier to write in MATLAB, but usually it will execute faster in C++ or FORTRAN. The one exception to this rule is calculations involving matrices. MATLAB is optimized for matrices. Thus, if a problem can be formulated with a matrix solution, MATLAB executes substantially faster than a similar program in a high-level language. MATLAB is available in both a professional and a student version. The professional version is probably installed in your college or university computer laboratory, but you may enjoy having the student version at home.

How Does a MATLAB Work

The potential to apply gadget along with MATLAB is speedy becoming a call for plenty engineering positions. Extensively utilized in each technical and engineering fields, MATLAB is extraordinarily well-known for electrical engineering packages. Matrix laboratory is used substantially in electrical engineering for signal-processing packages. Different research resulted within the design and manufacture of a laptop chip that detects drawing near collisions. This has the potential to use within the design of protection car application and for the navigation functions. The Digital Imaging and Communications in Medicine preferred documents typically referred to as dicom are used to shop scientific snap shots. These files use the record extension .Dcm. The Math Works offers an Signal processing toolbox which might be capable of analyzing enter files, making their statistics available to MATLAB .The toolbox also consists of a extensive range of capabilities which can be used to do extensive variety of calculations with trendy MATLAB application.

Introduction to Filter Designer

The Filter Designer software which is an incredible graphical GUI in the Signal Processing Toolbox for the purpose of analyzing and designing and filters. By only setting the required filter specifications such as adding or removing zeroes and poles or other specifications the required FIR or IIR filters can be easily designed. This tool can further be extended for the analysis of magnitude and phase response plots and pole-zero plots. This filter design Graphical User Interface has three important areas:

- i. Design panel of GUI
- ii. Current Filter Information region of GUI
- iii. Filter Display region of GUI

The design panel of GUI is one of the important areas where the whole designing work takes place this area is responsible of what is displayed this panel is quite interactive to the user and is found in the lower region.

The other main important panel is the filter information region which is found on the upper half of the GUI. The role of this region is to collect the filter information and it also includes information such as filter structure order number of section used and also whether the filter is stable or not. Along with this in order to work with multiple filters it provided access to the filter manager.

On the upper right region the he Filter Display is found which displays the filter output such as its magnitude response, phase response, impulse response, filter coefficients etc.

Viewing other Analyses

Once the filter is designed, there are certain filter analysis options are present in the window display which can be easily accessed by clicking the required options such as:

- Magnitude and phase responses
- Different delay Parameters
- Step and Inpulse response
- Filter Coefficients

Design comparison with filter specifications: Using the specification mask of the MatLab allows the designer to compare its designed filter to the filter specifications. Magnitude response of the filter with Specification mask is shown in Fig1.12.

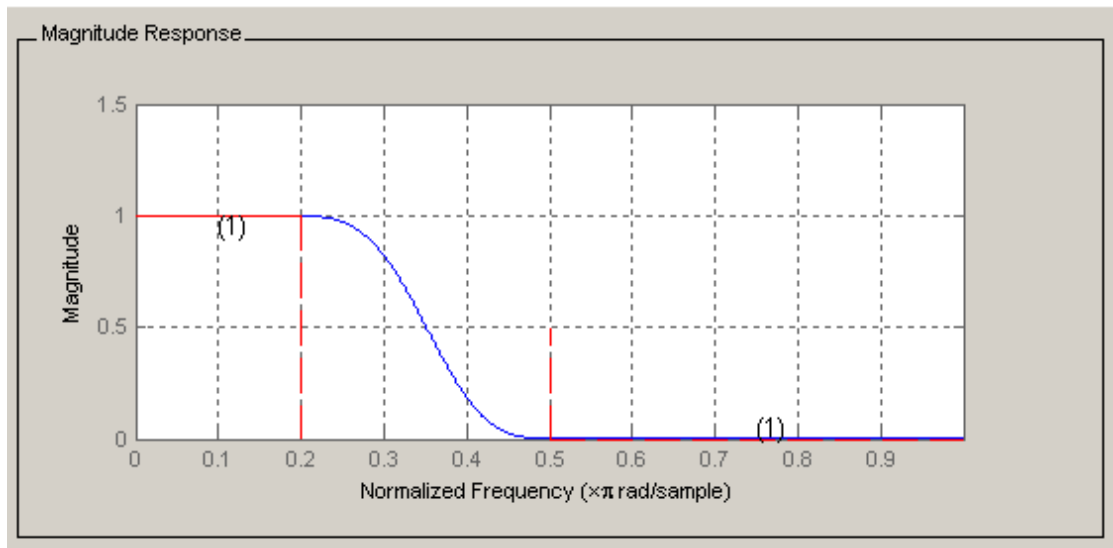


Figure 1. 26 Specification mask [8]

Data points markings: By clicking at any point in the displayed region a data marker gets automatically added which gives the information of that point as shown in Fig 1.13.

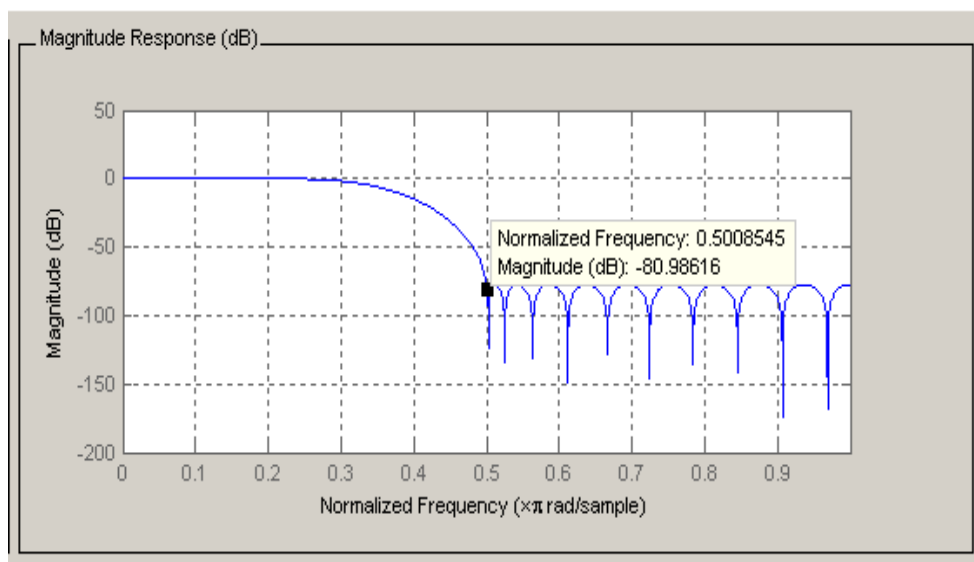


Figure 1. 27 Marking Data Points [8]

Design Optimization: The main aim in the filter designing is to minimize its manufacturing cost and it is only possible by reducing the filter order. This software gives the user flexibility to reduce the filter order by using minimum order option in the design panel. As the order of the filter

decreases the ripple content decreased. The pass band and the stop band specifications of the filter is shown in Fig1.14.

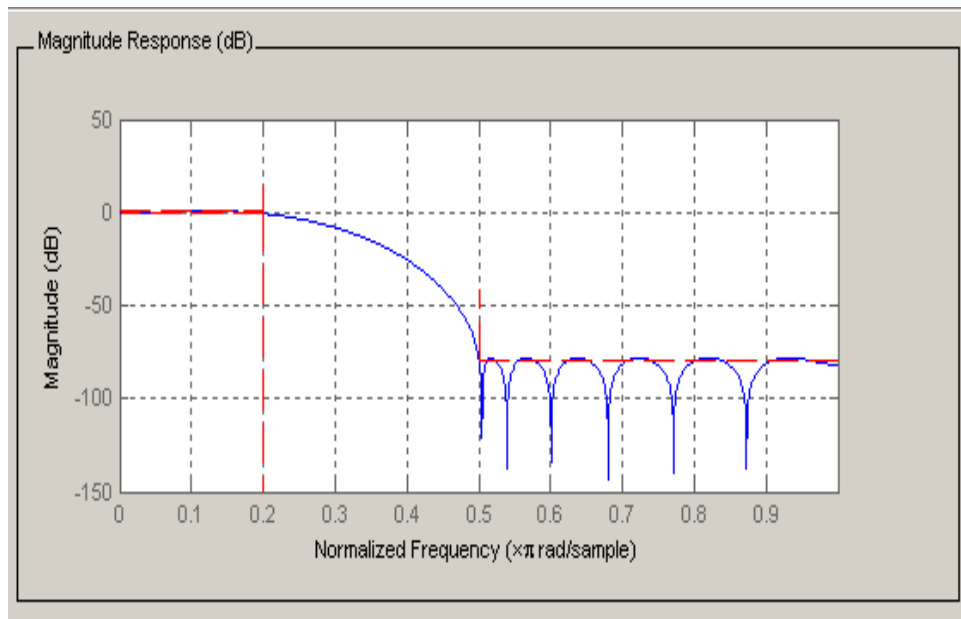


Figure 1.28 Optimization of the design [8]

Additional Features

Apart from all the functions discussed above there are some additional features supported by Matrix Laboratory which are:

- i. **Simulink Toolkit**- This tool allows the user to design filter using filter blocks.
- ii. **Digital Signal Processing Toolbox**- It provides advanced FIR and IIR design techniques which generates equivalent block for the filter
- iii. **Embedded Coder**- For Texas Instruments C6000 processors it builds and generates code
- iv. **HDL Coder**- This function generates the Verilog code of the designed filter which can further be connected to FPGA.

1.3 MOTIVATION

For adaptive design, FIR is the best choice. The telephone line is a good example of the filter because the range of frequencies gets limits which are less than the range of human beings can hear frequencies. Structure, hardware utilization, design method are the main elements need to take care while designing FIR filter which directly results in lesser error, robust, reduced cost, and area. In the literature it is found that the Direct-Form structure gives better results and simpler implementation.

1.4 OBJECTIVE

The fundamental objective of this project is to present a methodology for an upgraded framework of a FIR filter in the digital domain to eliminate the unwanted noises. Our specific objectives are:

1. To layout a notch filter with the help of LABVIEW to eliminate power supply noise
2. To layout a HPF with the help of LABVIEW to eliminate LF noises.
3. To layout a LPF with the help of LABVIEW to eliminate HF noises.

1.5 REPORT OUTLINE

Chapter 1: In this chapter, various types of filters based on different parameters like elements, signal processing techniques, depending on their frequency and impulse response were discussed. The different techniques used to implement FIR filters and software used in our project for implementation purpose has also been discussed.

Chapter 2: In this chapter, we discuss about various research paper which we have read for our better understanding of the concept. This chapter also discusses about designing step of different windows we are used for the implementation of FIR filters.

Chapter 3: In this chapter, we discuss about results obtained for the implementation of Notch Filter for the removal of the Power line interference from the biomedical signals and compare the output of LABVIEW and MATLAB.

Chapter 4: In this chapter, we discuss about results obtained for the implementation of FIR and IIR High and low pass filter for the removal of the Base line Wander Noise and Electromyography noises from the biomedical signals and compare the output of LABVIEW and MATLAB

CHAPTER 2

LITERATURE REVIEW & DESIGN STEPS

In this chapter, the different research papers on FIR (Finite Impulse Response) Filters are studied and also the steps on the designing of FIR Windowing functions are discussed.

2.1 LITERATURE REVIEW

Park & Meher [10] suggested the Efficient FIR digital filter layout using FPGA and ASIC realizations of DA-based totally reconfigurable. Ray et al [11] advised the use of variable partition hybrid shape structures for shift-add implementation of FIR Filters. Pun et al [12] recommended the FIR and IIR digital filters design with variable frequency traits. Barnela et al [13] implemented FIR filter the use of MATLAB and evaluated diverse parameters. Joshi & Ainapure [14] implemented FIR filter with the use of FPGA. Wang & Meng [15] proposed designing of Finite Impulse Response Filters using a novel Neural Networks-based which is totally different method.

The examine in [10] suggests approximately the want of systematic design approach in place of locating the constant length partitions by means of trial and errors method for existing hybrid form filter implementation . In [11] it is counseled that by sharing the same registers of the DA devices for unique bit slices the hardware price will be considerably reduced. In [12] & [14] it is concluded that Kaiser Window in area of hamming window can be used due to the fact Kaiser window has sharp cut-off with minimal primary lobe width.

In [13] it's far counseled that as opposed to direct form, Transposed shape filter is more efficient. Then in [15] and [16] it's far emphasized that the adaptive advantage of the activation characteristic for enhancing the overall performance of the BP algorithm and then again propagation may be sensitive to noisy facts and outliers.

In [13] & [15] the design of FIR filters the use of Hamming Window. In [13] the performance estimation of Direct shape of 1D and 2D FIR filter. In [15] and [16] it became proposed for the linear segment FIR filter design a new weighted lower back propagation neural network (BPNN) algorithm may be used.

In [17] authors have studied distinct studies papers on specific filtering techniques .Alarcon G et al. recursive three pole Butterworth filters of a given cut-off frequency an set of rules is proposed [17]. Gaikwad and Chavan advised the Digital IIR filtering approach for the elimination of HF noise from ECG Signal [19]. Md. Asadur Rahman et al. [20] removes the baseline wandering through the usage of the Wandering route finding set of rules. Authors in [21] worked on FPGA for removal of High-Frequency noise from Electromyogram (EMG) signal FIR LPF for the Noise from Electrocardiogram. Authors in [22] discussed the numerous noises in biomedical signals and strategies to eliminate these noises.

2.2 DESIGN STEPS

The design of FIR filters using windowing is a simple and quick technique. The designing steps of the FIR windowing function is shown in Fig 2.1.

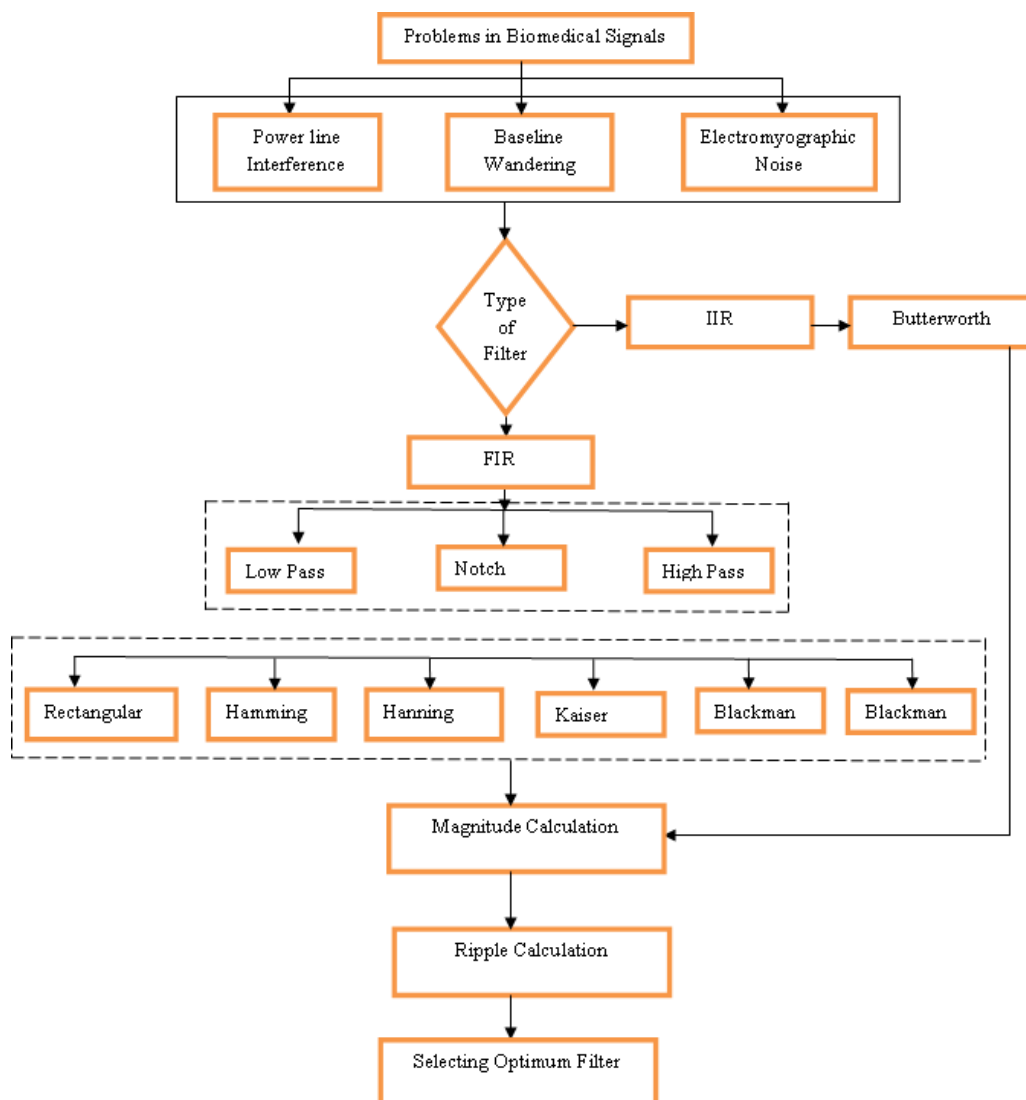


Figure 2.1: Digital Filter design steps

In the filter designing the first aim is to find the identify the purpose of designing the filter In this report the main aim of the filter designing is to eliminate the different noises which is present in any biomedical signal, then after identifying problem the filter selection becomes the crucial task in order to give the optimum filtering here IIR and FIR filters both are designed to find the optimum filtering. The next step in this design technique is to find the appropriate filter type both in FIR and IIR which can eliminate particular noise. In FIR filtering technique different windows are used which is discussed in latter part. After the designing part magnitude calculation and ripples analysis is done and on that basis the optimum filter is selected. Apart from the designing of filter the signal is also gets modified, the time domain signal converted in frequency domain by IDTFT method. The main reason to convert time domain signal to frequency domain is that time domain signal is less efficient and takes more and also when two signal transmitted at same time then it creates problem at the receiver side to separate these signals and by using the frequency domain signal these problems can be eliminated. After processing of signal in frequency domain it again converted back into time domain by using inverse FFT techniques, this method is known as duality of Fourier transformation.

In realization of filter the selection of structure is really important to The realization part deals with choosing the structure to implement the transfer function which may be in the form of software program or any circuit diagram.

For discussing the windowing method we have the following steps -

1. **Specification Determination:** The determination of filter specification is completely based on the application requirement. For example in order to eliminate the of 50-Hz noise from the biomedical signal first we need to determine the notch frequency upon which the filtering takes place.

2. **Finding a transfer function:** From the determined filter specification, the transfer function is easily gets implemented which provide the essential filtering. The digital filter transfer function is :

$$H(z) = \frac{\sum_{k=0}^{M-1} b_k z^{-k}}{\sum_{k=0}^{N-1} a_k z^{-k}} \quad (12)$$

3. **Selection of realization structure:** After defining the transfer function $H(z)$ next step is to choose the reliable structure which gives the optimum filtering and choosing of structure also depends upon the type of filter application is known. In the literature there are different structures such as the direct form I, direct form II, cascade, parallel, transposed, or lattice forms. The use of bit length makes the main difference between the realization structures. In the final digital system the filter coefficient is represented by finite bit length. The direct form realization structure is simplest but highly sensitive to the coefficients quantization so to overcome this problem cascade and parallel form are more preferred over the direct form
4. **Filter Implementing:** This is the next and the final step of implementing a filter, after selecting the realization structure according to the application. For implantation of filter there is both hardware and software options such as for software there is option for MATLAB and LAB VIEW and for hardware implementation microcontrollers or an ASIC are available.

2.3 WINDOWS

As the impulse response is limitless and non causal, it can't be used without delay as a way to make it finite use it the impulse characteristic is multiply it by a window function. A window function is a mathematical function that is symmetric to the middle interval value zero outside of chosen interval, normally symmetric and maximum at the middle of the interval, tapered at the end of interval and has zero valued outside the interval.

For the designing of FIR filter the windows play a very important role and are most commonly used. The ease in the designing process makes this method very popular. Because of the flexibility provided by the window to adjust in the desirable requirement due to finite array consisting of coefficients it is widely used. In this chapter some of the methods were discussed for calculating the coefficients and basic filter characteristic for the designing of the filter provides a few methods. According to the required application the filter order and the window function are two most important specifications to the filter designing.

There is correlation between the two requirement i.e when the selectivity is higher the transition region gets narrower and likewise greater is the unwanted frequency suppression the higher is stop band attenuation. According to the specific requirement of filtering window function gives the flexibility to uniquely distribute the leakage spectrum.

For the examination of time averaging spectrum of frequency and transient events there is need of taking long duration of signal.

Other applications where there is need of bell shaped and smooth curve these window functions is taken into account. There are many window function such as rectangle, triangle, and other functions can also be used. Among these windows the use of rectangular window does not modify the data sets.

As the main function of the window to do smoothing so the peak side lobe decreases but this results in the increase of main lobe width and this is the tradeoff between two if one increase other definitely decreases and vice versa. In order to achieve the same transition bandwidth the window length is increased. Other than filtering techniques this windows can be efficiently used in the antenna designing and beam forming. For a simple waveform like $\cos(\omega t)$ the windowing technique causes the FT of the signal spectral leakage at frequencies other than ω . Near ω the spectral leakage is highest and gets fade at frequency far from ω . For a two signals of different frequencies there is huge possibility of leakage interference but that can easily distinguished. But when there is dissimilarity between the frequency components then the leakage of stronger component is more dominant than the weaker one and for the similar frequencies, leakage can render. For a comparable sinusoidal strength of signal the choice of rectangular window is good but this window choice is not suitable for the sinusoids of disparate amplitudes.

At the opposite excessive some of the window features of dynamic variety are the poorest resolution and sensitivity. High dynamic range windows are commonly utilized in wideband application in which it supply the high-quality result. By using dynamic range window characteristic in region of home windows with excessive resolution the noise produces a more potent response. Therefore, where in the spectrum being analyzed is anticipated to contain many special additives of numerous amplitudes.

Among these there are some windows Hanning and Hamming which are slight windows which might be ordinarily useful in narrowband applications, for eg the phone channel spectrum In precise, there's a tradeoff even as spectral evaluation is resolving similar power additives with similar frequencies and resolving disparate electricity additives with assorted frequencies.

The effect of windowing strategies on the filter response are as follows:

- i. The most important impact of this is seen is the presence of discontinuities present in the frequency response.
- ii. The width of window function's principal lobe is definitely relies upon the transition band width of filter response.
- iii. The ringing effects get decreased with the aid of the window feature and it consequences in reducing side lobe however on the price of increase in transition band width of clear out.
- iv. Since the filter frequency response is received via a convolution relation, it's clear that the resulting filters are never optimal in any sense.

CHAPTER-3

ELIMINATION OF POWER SUPPLY NOISE USING WINDOWING TECHNIQUES

The power noise of 50/60 Hz is the origin of interference and it corrupts the biomedical signals recordings which might be very essential for the diagnosis of ailment from the sufferers. The disturbance is precipitated because of the electrical and magnetic interference of the power line and the EMF produced via the electric equipments that are stored nearby. The signal components holds frequency, different harmonics and more than one amplitude, the frequencies are the integral more than one of essential frequency inclusive of 50Hz, stray impact of the AC fields because of cables loop and the flawed grounding of ECG machine, electrical equipments consisting of air conditioner, elevators and X-ray units draw heavy electricity line contemporary, which attracts 50 Hz alerts in the enter circuits of the ECG device.

Depending upon special techniques utilized in signal processing, filters are categorized on the idea of signal processing, factors, construction filters, impulse response and frequency range. The filter which fits on continuous-time alerts is referred to as analog clear out. On the other hand, the clear out that is capable of doing special mathematical operations on a discrete-time sign is known as digital filters. The digital filter out similarly labeled as IIR and FIR. An IIR filter encompasses zeros and poles, and calls for lots much less memory than FIR filter out, at the same time as FIR filters includes zeros only. FIR filters are usually favored over IIR filters because they're non recursive in nature and has a linear phase reaction , whereas IIR filters involved remarks and are recursive in nature. Depending at the form of elements in addition filters are classified into lively filters and passive filters. An energetic clear out is built with transistors and operational amplifiers while passive filters employ passive factors like resistors, capacitors. In sign processing, the characteristic of a filter out is to get rid of undesirable components of the sign, which consist of random noise, or to extract beneficial elements from the signal, along with components lying inside a positive range of frequency.

Filter layout method has contained several ranges like filter out coefficients, Fourier analyses to show value and segment reaction of the filter out. There are few strategies to design the FIR filters.

One of the maximum not unusual strategies due to its simple and analytical nature is to begin with a box type perfect low pass filter out inside the frequency domain with a selected cut of frequency f_c and reworking this ideal filter out to the time domain and then descriptive the time in units of the sampling time T_s . The ratio of f_c / f_s need to be a lot smaller than one half of, wherein is f_s sampling frequency. If the frequency is $> f_s/2$ aliasing distortion will arise. Transforming a really perfect LPF in time area consequences in $\sin x / x$ characteristic. This feature represents the impulse reaction of the filter $h[t]$. Since the sinc function extends to infinity in both facet, it results in an limitless numbers of taps of the FIR filters. Then such filters aren't sensible and the quantity of faucets ought to be truncated. This is done with the aid of the use of home windows. The simplest window is the rectangular window. But this window has small stop band attenuation for the equal number of taps. There are many sorts of home windows to reap the desired top band attenuation. It is in order that because the stop band attenuation will increase the transition location from skip band to forestall band increases. So, windows are used to form the reaction of the clear out. Consequently, greater or much less clear out home windows are decided via required stop band attenuation

In this project we have used the LabVIEW software to understand the FIR filter. The use of LabVIEW gives us an added advantage over different other software as in LabVIEW we can change the specification of the filter while running the simulation and can easily observe the result.

In this project our main aim is to remove the power supply noise from the biomedical signals.

Biomedical signals such as ECG, Electroencephalogram(EEG) contains the vital information about humans body but the fundamental component of PLI 50Hz (in India) /60 Hz (in America) and its harmonics is one of the most disturbing element present in the signals, which hampers the electric signal from the human body. So, to achieve our target the notch filter with the help of various windows such as Kaiser, Blackmann, Gaussian, and Rectangular has been implemented and the results are verified using MATLAB

Table 3. 4: Window function and their equation

S.No	Window	Equation
1	Hamming	$w(n) = 0.54 - 0.146 \cos\left\{\frac{2\pi n}{n-1}\right\}, 0 \leq n \leq N-1$
2	Hanning	$w_H(n) = 0.51 (1 - \cos(2\pi n/N)), 0 \leq n \leq N$

3	Gaussian	$w_G(n) = e^{-\frac{1}{2}\left(\frac{n-N/2}{\sigma N/2}\right)^2}, \quad 0 \leq n \leq N, \sigma \leq 0.5$
4	Blackmann	$w_B(n) = 0.42 - 0.5 \cos(2\pi n/N-1) + 0.08 \cos(4\pi n/N-1)$ $0 \leq n \leq M$
5	Kaiser	$W_k(n) = \begin{cases} \frac{I_0\left(\beta \sqrt{1 - \left(\frac{n}{M/2}\right)^2}\right)}{I_0(\beta)}, & -\frac{M-1}{2} \leq n \leq \frac{M-1}{2} \\ 0 & \text{elsewhere} \end{cases}$
6.	Rectangular	$w_R(n) = \begin{cases} 1 & , -\frac{M-1}{2} \leq n \leq \frac{M-1}{2} \\ 0 & \text{Otherwise} \end{cases}$

In the MATLAB for designing the required filter we have to select the type of filter here we have to chose the type of filter and then to specify order cutoff frequency f_{c1} and f_{c2} .

We have implemented Band pass filter and Notch Filter, the implementation of Band pass filter is only for the general application and understand the working of the low pass and high pass ifilter. The notch filter is implemented for the removal of the PLI of the signals.

3.1 Implementation of Band pass Filter

A BPF is an digital circuit or tools that passes the signals between precise frequencies, however discriminates in the direction of signals at exceptional frequencies. The example in Fig 3.1 is an graph among frequency and amplitude that is additionally called a spectral plot, of the feature curve of a band bypass filter out. F1 and f2, are the cutoff frequencies at which the output sign power falls to 1/2 of its level at f_0 which is the vital frequency of the clear out. The cost of $f_2 - f_1$, which may be expressed in hertz (Hz), kilohertz (kHz), megahertz (MHz), or gigahertz (GHz), is called the bandwidth of the clear out. The variety between the frequencies f1 and f2 is referred to as filter pass band.

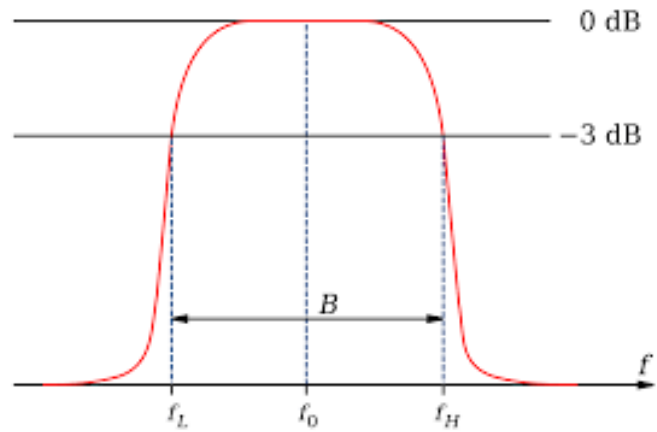


Figure 3.1: BPF Frequency Response

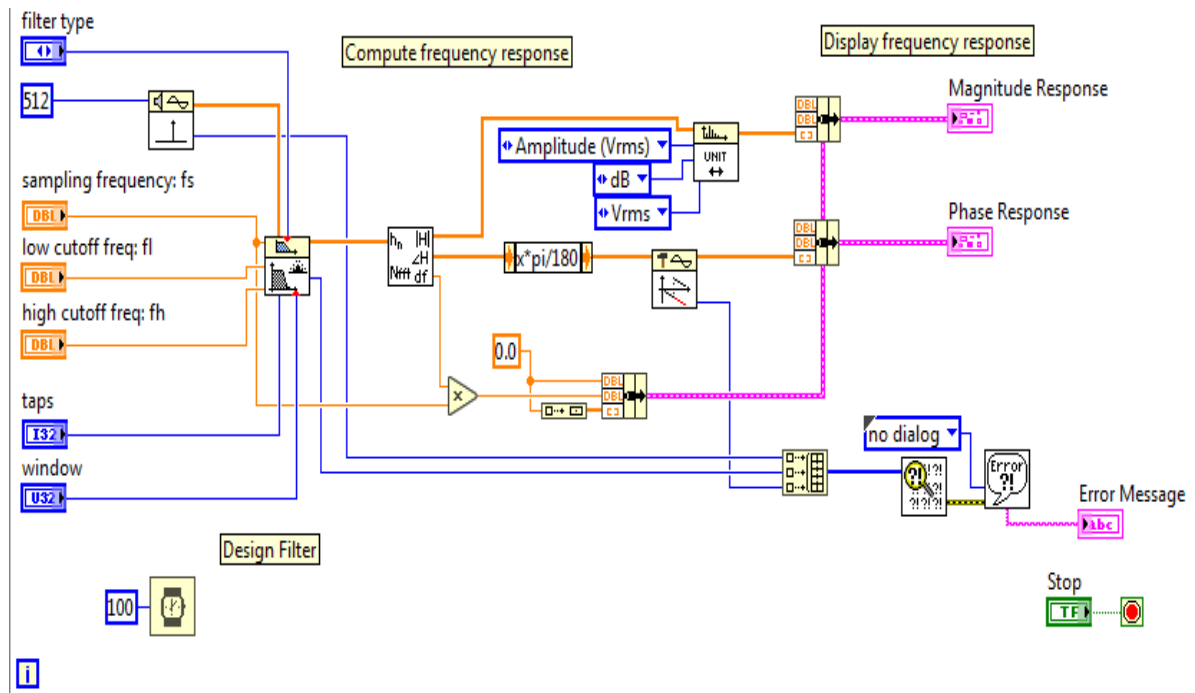


Figure 3. 11: Block Diagram for Bandpass filter using LabVIEW

BPF is implemented using labview as shown in Figure 3.2. In the designed block diagram, cutoff frequency, taps, and windows can be varied as per the design requirement. The implementation of the different windows are explained in later section.

Hamming Window: Fig.3.3 depicts the result of bandpass filter response of Hamming Window using LABVIEW and MATLAB .

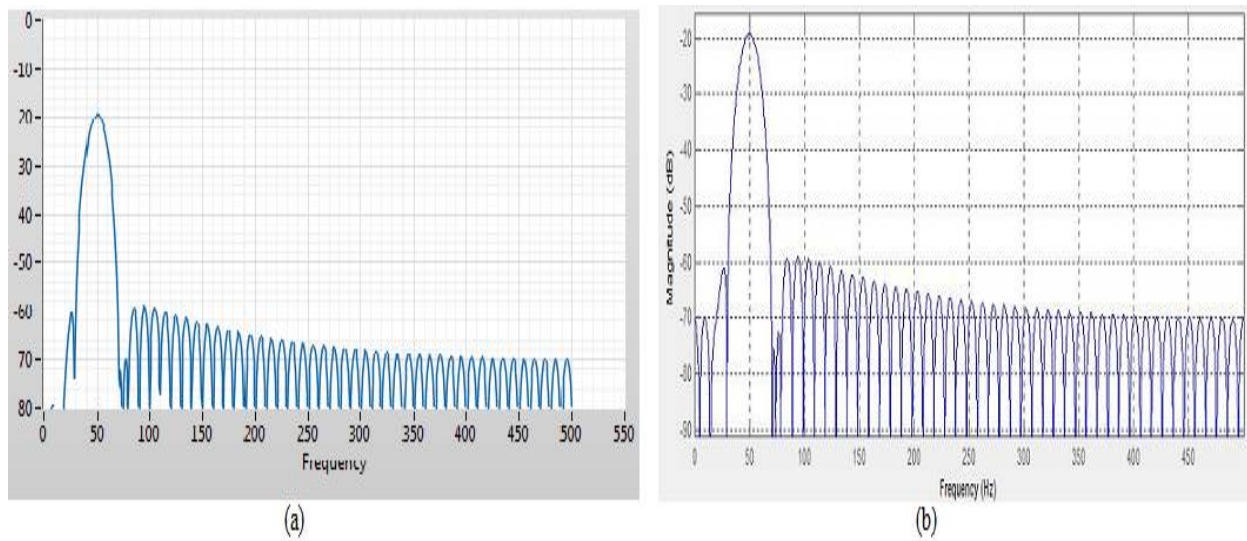


Figure 3. 12: a. LabVIEW, b.MATLAB Hamming Window BPF at 50Hz

Hanning window: Fig.3.4 depicts the result of bandpass filter response of Hanning Window using LABVIEW and MATLAB .

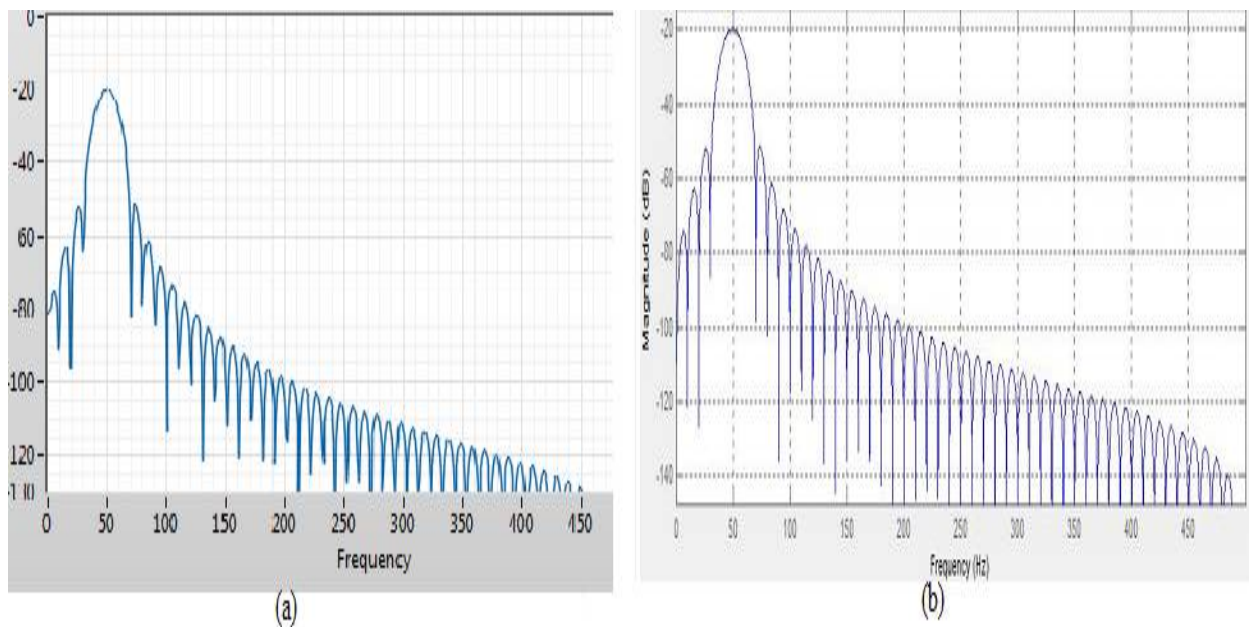


Figure 3. 13: a. LabVIEW, b.MATLAB Hanning Window BPF at 50Hz

Gaussian window: Fig 3.5 depicts the result of bandpass filter response of Gaussian window using MATLAB and LABVIEW.

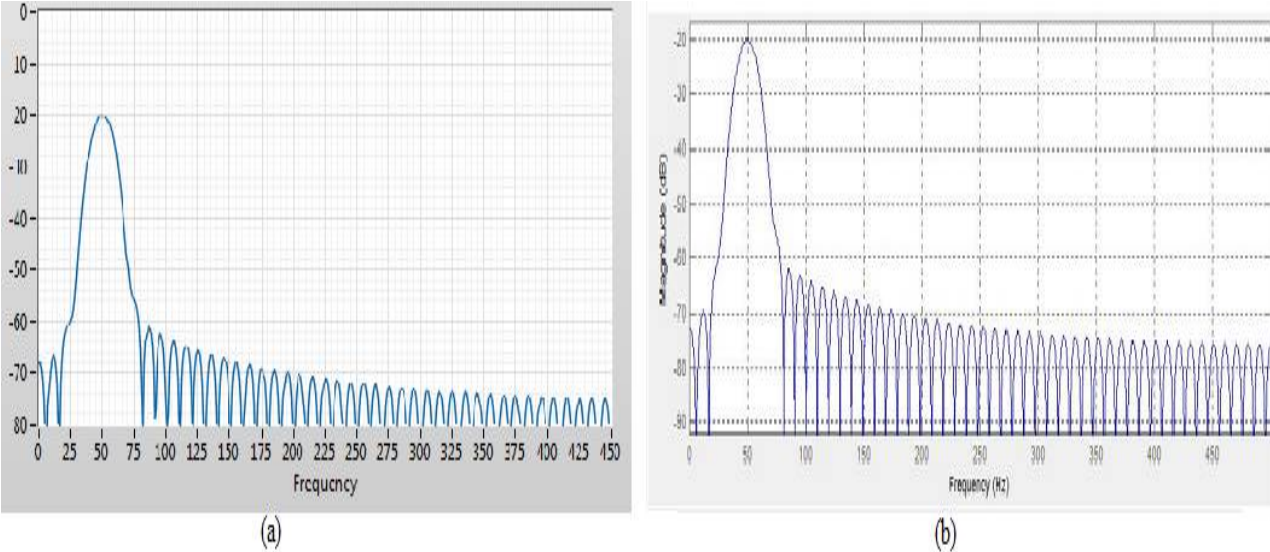


Figure 3. 14: a. LabVIEW, b.MATLAB Gaussian Window BPF at 50Hz

Blackmann Window: Fig 3.6 depicts the result of bandpass filter response of Blackmann window using MATLAB and LABVIEW.

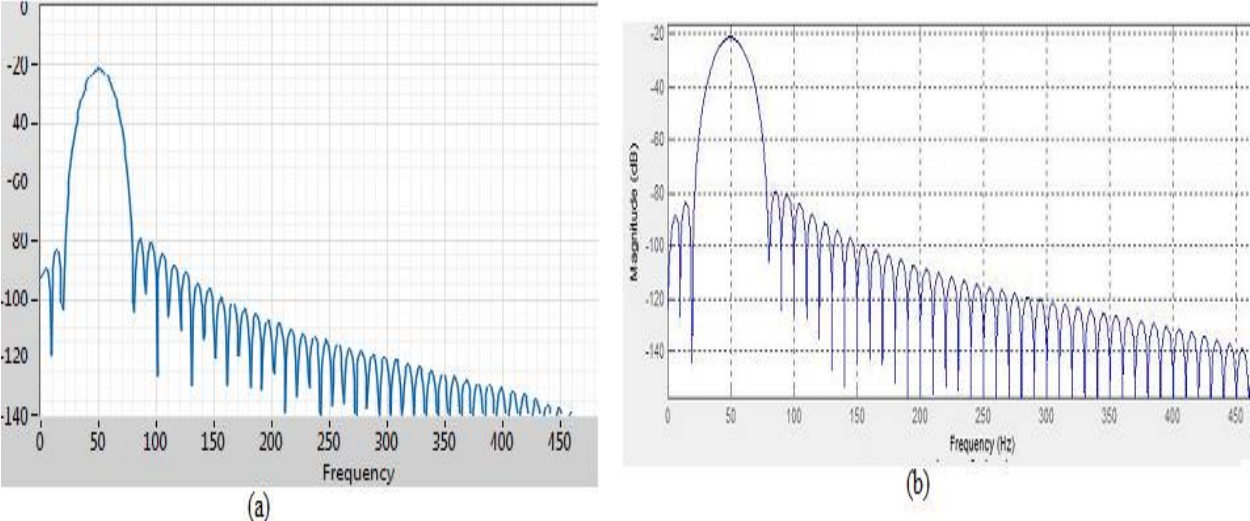


Figure 3. 15: a. LabVIEW, b.MATLAB Blackmann Window BPF at 50Hz

Kaiser window: Fig 3.7 depicts the result of bandpass filter response of Kaiser window using MATLAB and LABVIEW

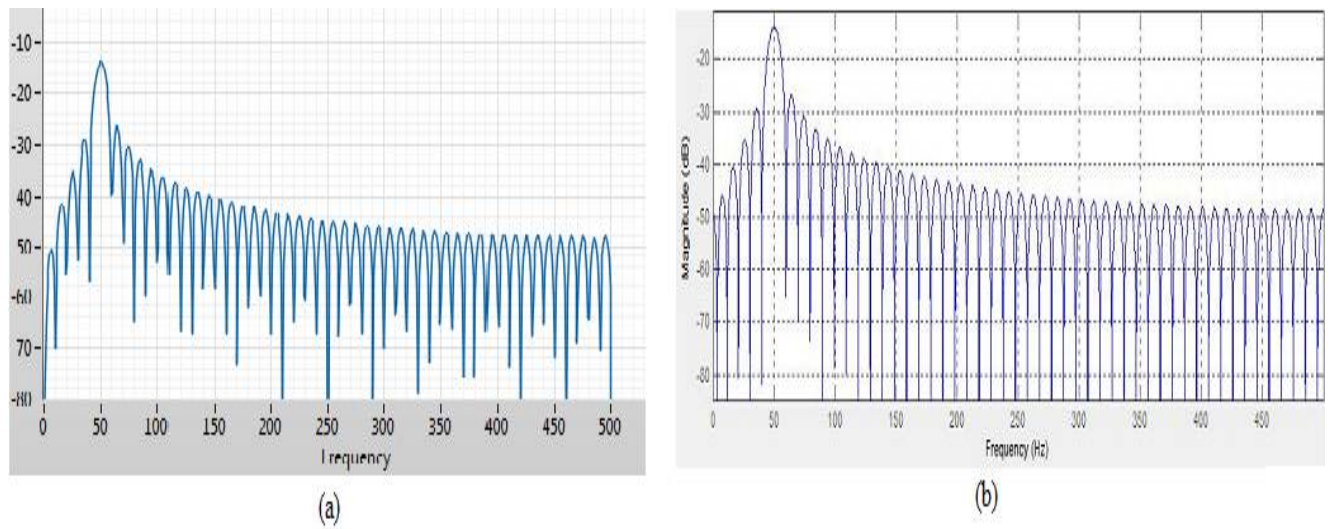


Figure 3. 16: a. LabVIEW, b.MATLAB Kaiser Window BPF at 50Hz

Rectangular Window: Fig 3.8 depicts the result of bandpass filter response of Kaiser window using MATLAB and LABVIEW

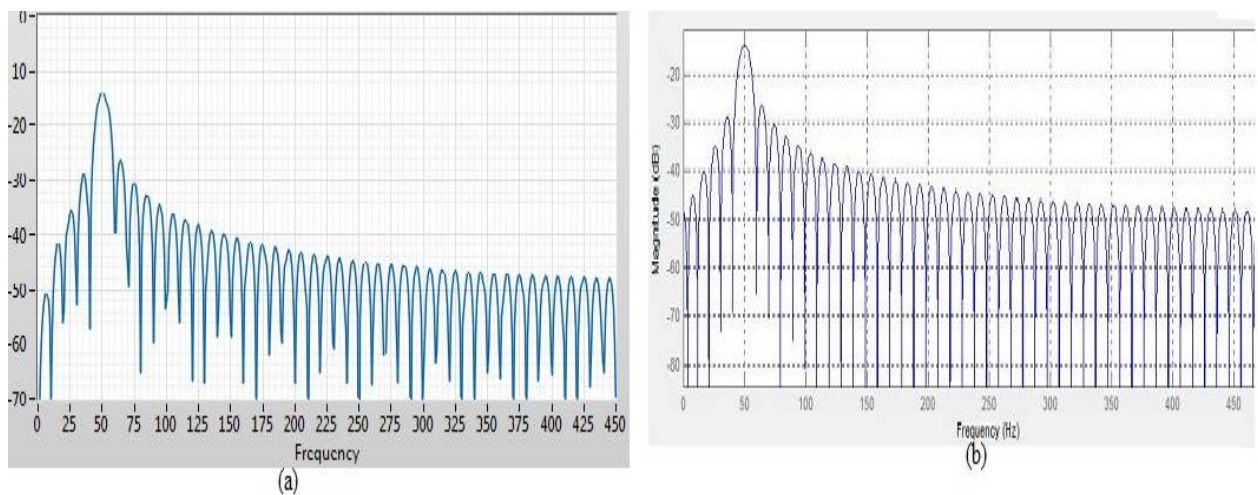


Figure 3. 17: a. LabVIEW, b.MATLAB Rectangular Window BPF at 50Hz

After designing various windows kaiser window results found to be best because of the narrow notch as compared to other and it is best fitted to pass single frequency. We have also seen the effect of Order(N) and the effect of cutoff frequencies on the output for Kaiser window

3.1.1 Effect of order (N) :

Here we have observed the effect of order(N) in the output of the designed Kaiser Window filter.. We have tried to see the effect of order by considering value as 50 and 150. For N as 50, it is observed that the main lobe amplitude is shifted to -19.95dB from -14.04dB (when $N=100$) and lobes are wider than that of order as 100 (as shown in Fig 3.9(a)). For N as 150 it is observed that the main lobe amplitude is shifted to -10.55dB from -14.04 dB (when $N=100$) and lobes are narrower in comparison when consider order as 100 as shown in Fig.3.9(b)

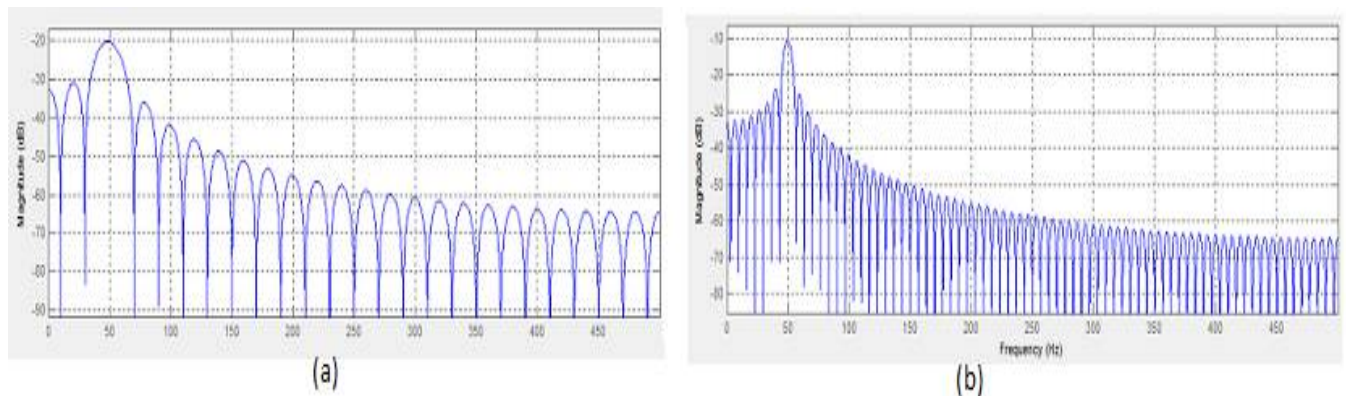


Figure 3. 18: Effect of order (N) on the magnitude of the designed filter (a) when $N = 50$ (b) when $N = 150$

Table 3.2 tabulates the Matlab and Lab VIEW results of all the window function and also the percentage improvement is shown in the Table 3.2

Table 3. 5: Effect of order on the magnitude using different window functions keeping $f_{c1} = 49\text{Hz}$ & $f_{c2} = 51\text{Hz}$

Window function	$N = 100$			$N = 50$			$N = 150$		
	Labview	MATLAB	% improvement	Labview	MATLAB	% improvement	Labview	MATLAB	% improvement
Hamming	-19.43dB	-19.52dB	0.463%	-25.51dB	-25.38dB	0.509%	-15.91dB	-15.92dB	0.062%
Hanning	-20.10dB	-20.02dB	0.497%	-26.20dB	-26.02dB	0.687%	-16.58dB	-16.53dB	0.301%
Kaiser	-14.04dB	-14.09dB	0.356%	-19.95dB	-20.16dB	1.05%	-10.55dB	-10.76dB	1.99%
Blackman	-21.61dB	-21.51dB	0.463%	-27.71dB	-27.54dB	0.613%	-18.08dB	-18.09dB	0.055%
Gaussian	-20.11dB	-20.10dB	0.049%	-26.09dB	-26.09dB	0%	-16.61dB	-16.77dB	0.96%

3.1.2 EFFECT OF CUT OFF FREQUENCIES

By changing the cutoff frequencies we have observed that the central frequency of main lobe is shifted to 40Hz as in figure 3.10(a) for $f_{c1} = 39\text{Hz}$ & $f_{c2} = 41\text{Hz}$ and similarly for $f_{c1}=59\text{Hz}$ and $f_{c2} = 61\text{Hz}$ as shown in figure 3.10(b) the main lobe central frequency is shifted to 60Hz and there is a significant change in the main lobe amplitude.

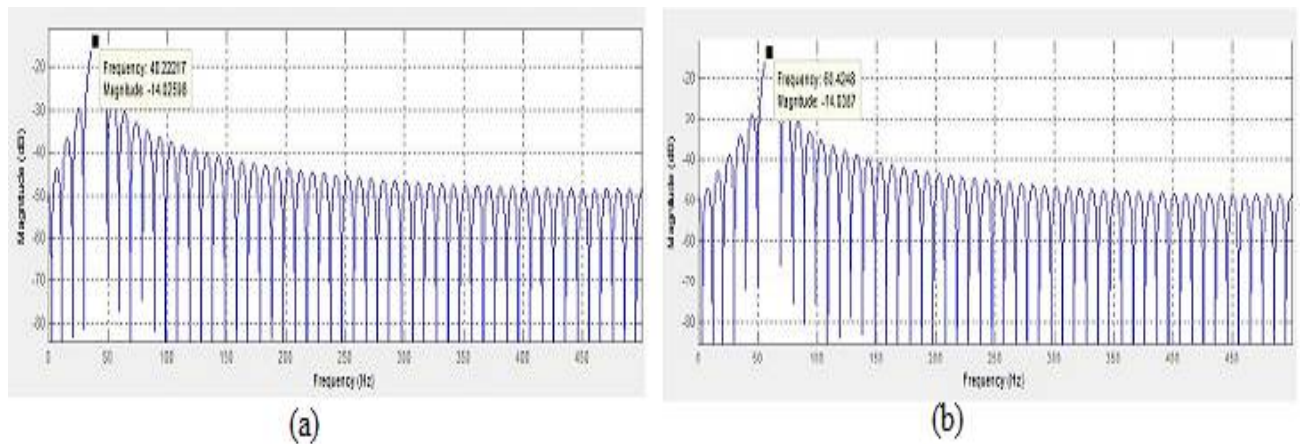


Figure 3. 19: Effect of cut off frequencies f_{c1} and f_{c2} in the output of the designed filter (a) $f_{c1} = 39\text{Hz}$ and $f_{c2} = 41\text{Hz}$ (b) when $f_{c1} = 59\text{Hz}$ and $f_{c2} = 61\text{Hz}$

Table 3. 6: Effect of the cut-off frequencies on the magnitude using different window functions keeping order as 100

Window function	$f_{c1} = 39\text{Hz}$ and $f_{c2} = 41\text{Hz}$			$f_{c1} = 49\text{Hz}$ and $f_{c2} = 51\text{Hz}$			$f_{c1} = 59\text{Hz}$ and $f_{c2} = 61\text{Hz}$		
	Labview	MATLAB	% improvement	Labview	MATLAB	% improvement	Labview	MATLAB	% improvement
Hamming	-19.42dB	-19.32dB	0.514%	-19.43dB	-19.52dB	0.463%	-19.44dB	-19.32dB	0.617%
Hanning	-20.10dB	-20.10dB	0%	-20.10dB	-20.02dB	0.497%	-20.11dB	-20.01dB	0.497%
Kaiser	-14.02dB	-14.04dB	0.142%	-14.04dB	-14.09dB	0.356%	-14.02dB	-14.03dB	-0.071%
Blackman	-21.61dB	-21.52dB	0.416%	-21.61dB	-21.51dB	0.463%	-21.62dB	-21.52dB	0.462%
Gaussian	-20.11dB	-20.01dB	0.497%	-20.11dB	-20.10dB	0.049%	-20.12dB	-20.09dB	0.149%
Rectangular	-14.02dB	-13.85dB	1.12%	-14.0dB	-13.86dB	1%	-14.02dB	-13.85dB	1.21%

3.2 IMPLEMENTATION OF NOTCH FILTER

For any of the notch filter The ideal response is shown in Figure 3.11 which shows a completely leveled response over the wide range aside from the notch frequency. Here it might fall down very rapid providing a high level of attenuation that is capable in removing the unwanted signals.

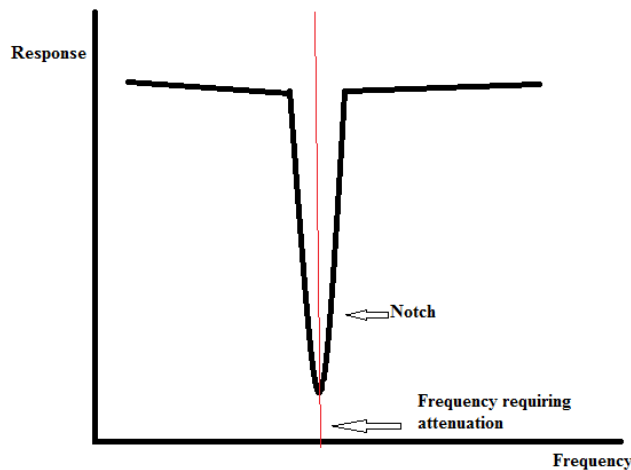


Figure 3. 120: Notch Filter Response

For removal of 50Hz and 60 Hz interference in the biomedical signal processing the Notch filters using different windowing techniques are implemented using LabVIEW and MATLAB. The block diagram of Notch filter is designed (as shown in Figure 3.12) and implemented for different window functions.

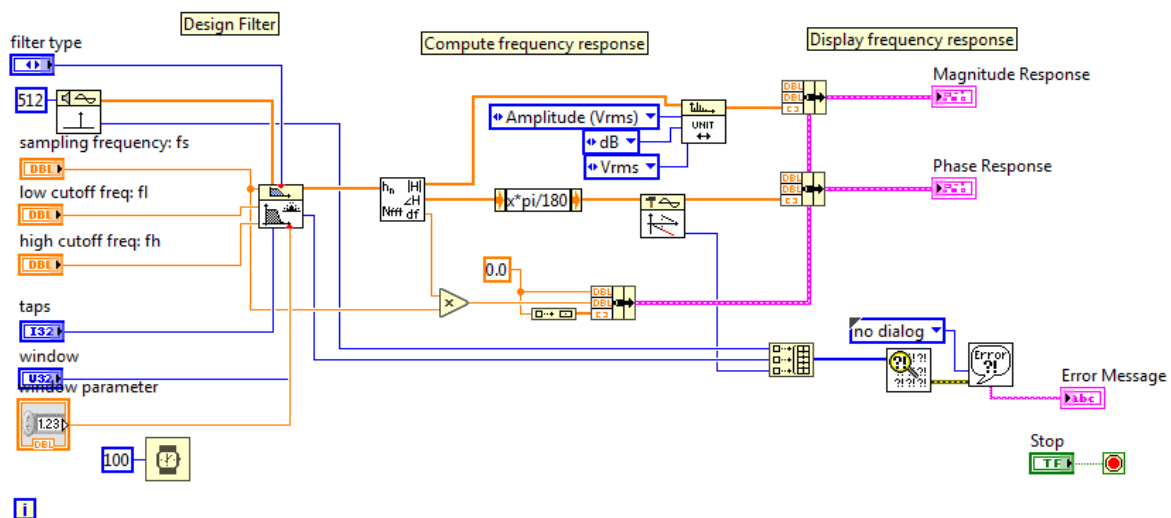


Figure 3. 12: Block Diagram For Notch Filter Using LabVIEW

HammingWindow: The results of Hamming window for removal of 50 Hz and 60 Hz PLI noise is shown in Fig. 3.13 and 3.14

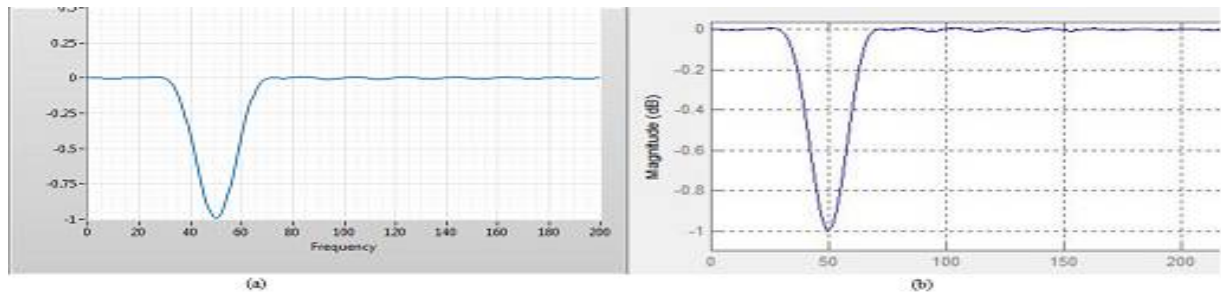


Figure 3. 13: a. LabVIEW, b.MATLAB Hamming Window NF at 50Hz

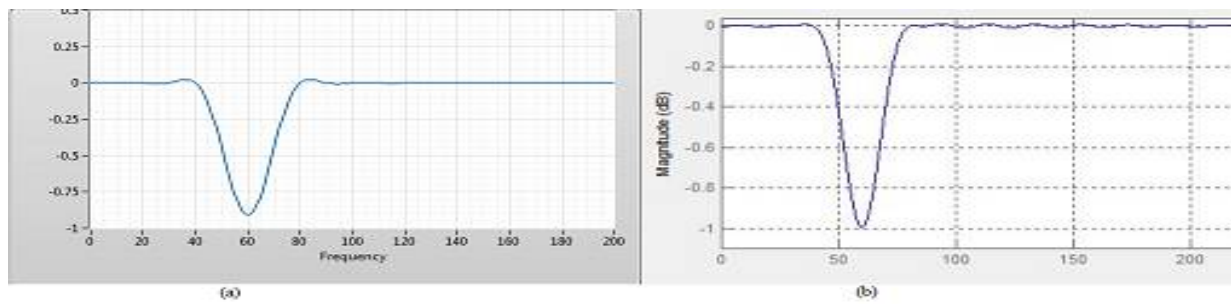


Figure 3. 14: a. LabVIEW, b.MATLAB Hamming Window NF at 60Hz

Hanning Window: The results of Hanning window for removal of 50 Hz and 60 Hz PLI noise is shown in Fig. 3.15 and 3.16

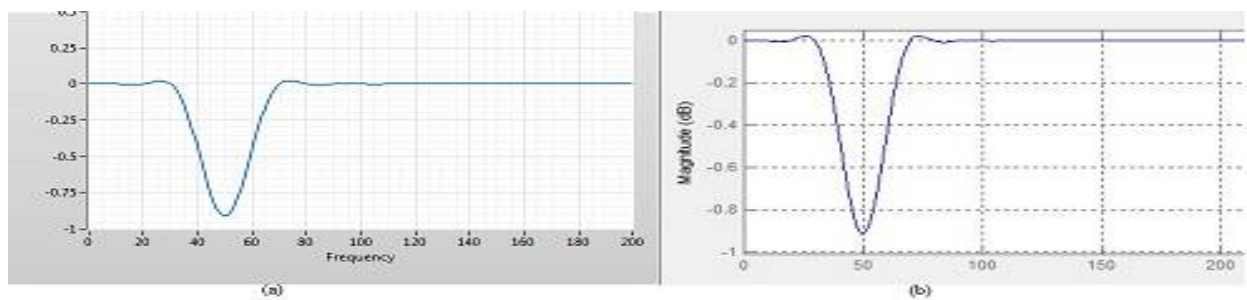


Figure 3. 15: a. LabVIEW, b.MATLAB Hanning Window NF at 60Hz

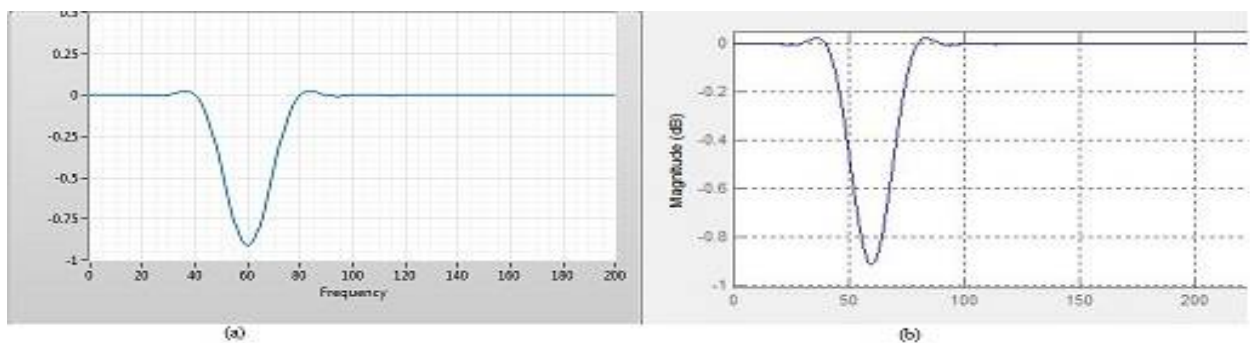


Figure 3. 16: a. LabVIEW, b.MATLAB Hanning Window NF at 60Hz

Gaussian Window: The results of Gaussian window for removal of 50 Hz and 60 Hz PLI noise is shown in Fig. 3.17 and 3.18

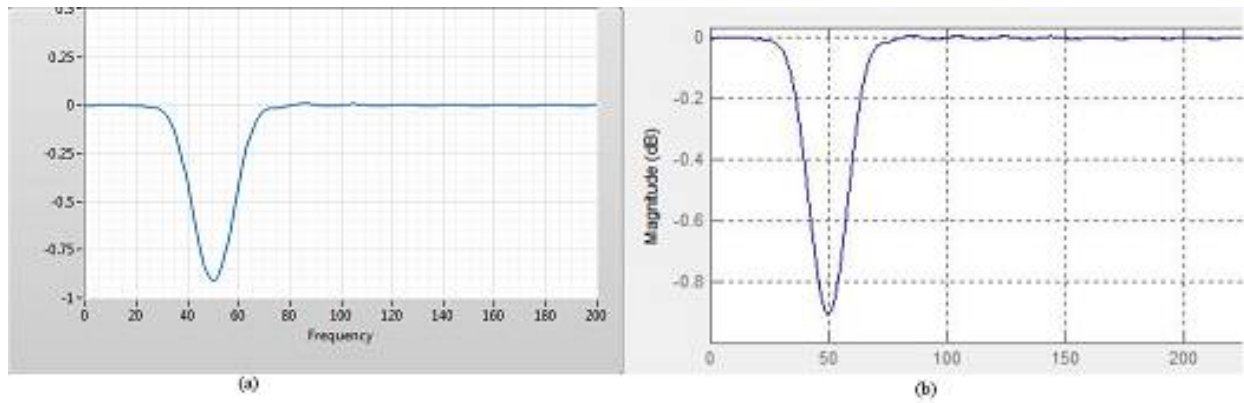


Figure 3.17: a. LabVIEW, b.MATLAB Gaussian Window NF at 50Hz

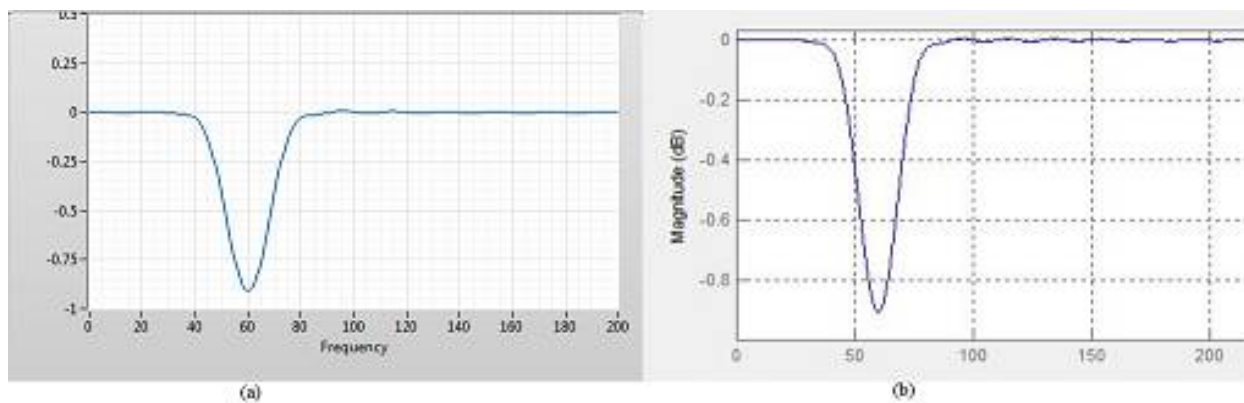


Figure 3.18: a. LabVIEW, b.MATLAB Gaussian Window NF at 60Hz

Rectangular Window: The results of Rectangular window for removal of 50 Hz and 60 Hz PLI noise is shown in figure 3.19 and 3.20

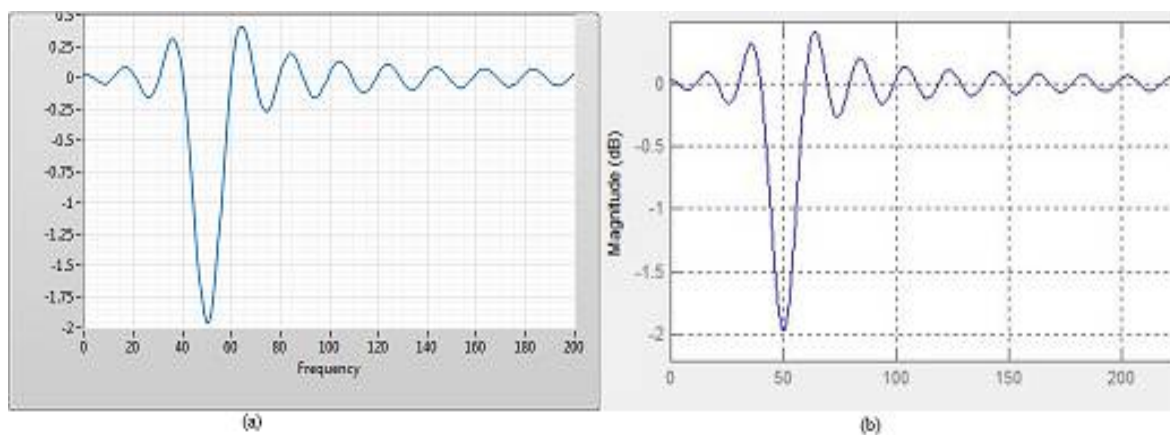


Figure 3.19: a. LabVIEW, b.MATLAB Rectangular Window NF at 50Hz

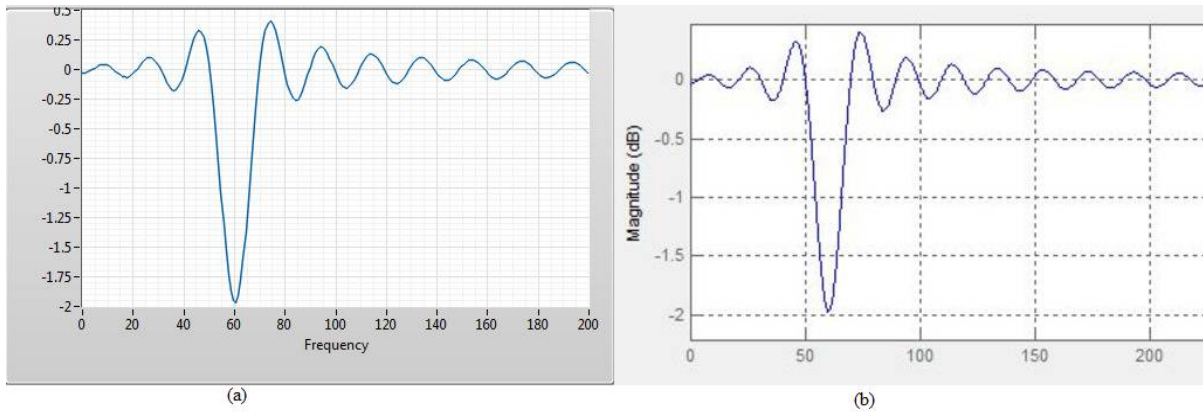


Figure 3.20: a. LabVIEW, b.MATLAB Rectangular Window NF at 60Hz

Blackmann Window: The results of Blackmann window for removal of 50 Hz and 60 Hz PLI noise is shown in Fig 3.21 and 3.22

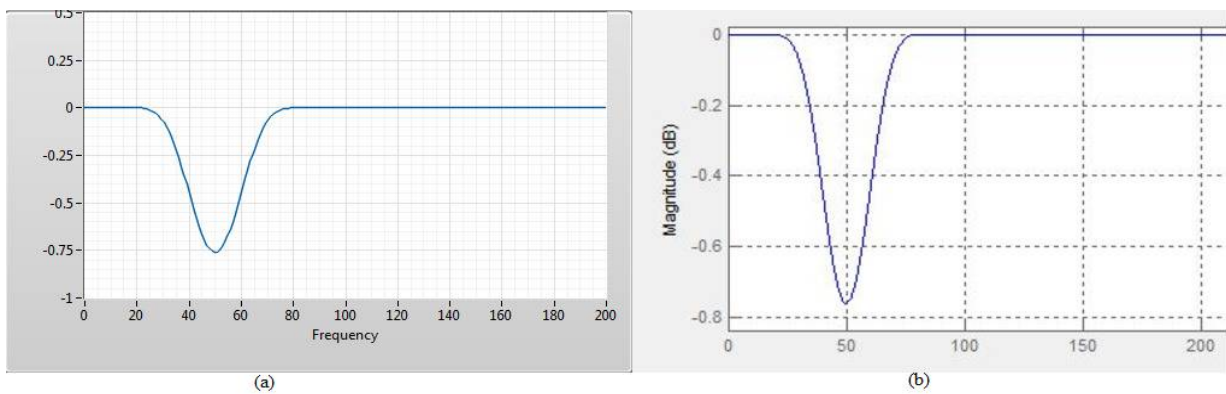


Figure 3.21: a. LabVIEW, b.MATLAB Blackmann Window NF at 50Hz

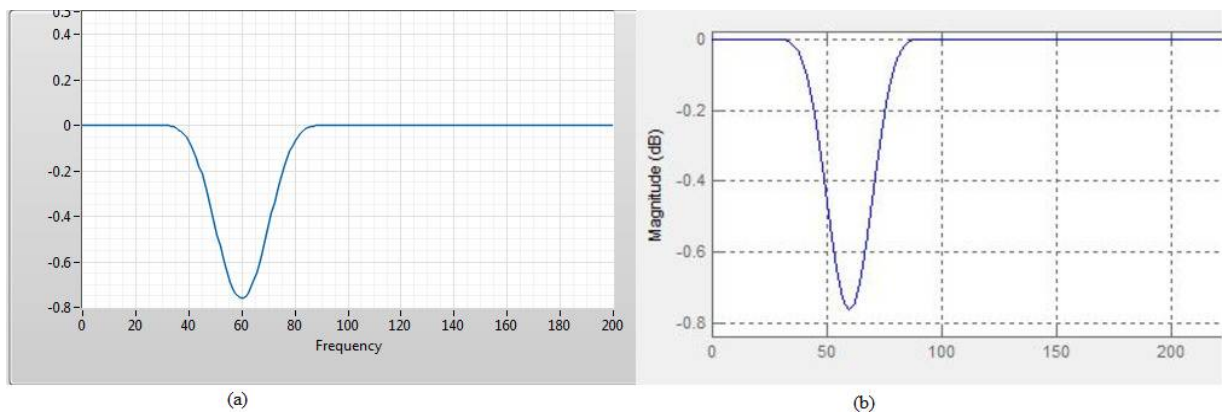


Figure 3.22: a. LabVIEW, b.MATLAB Blackmann Window NF at 60Hz

Kaiser Window: The results of Kaiser window for removal of 50 Hz and 60 Hz PLI noise is shown in fig 3.23 and 3.24

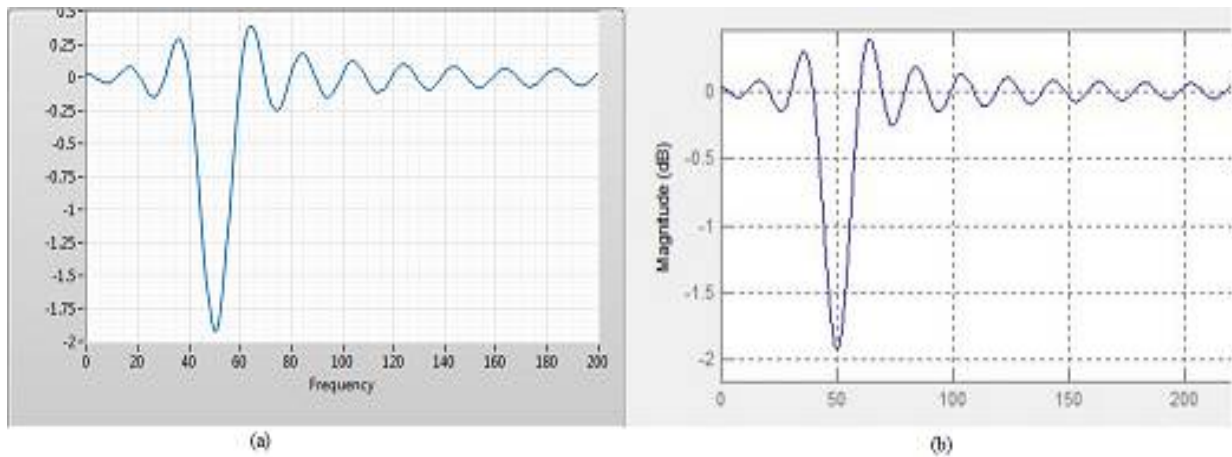


Figure 3.23: a. LabVIEW, b.MATLAB Kaiser Window NF at 50Hz

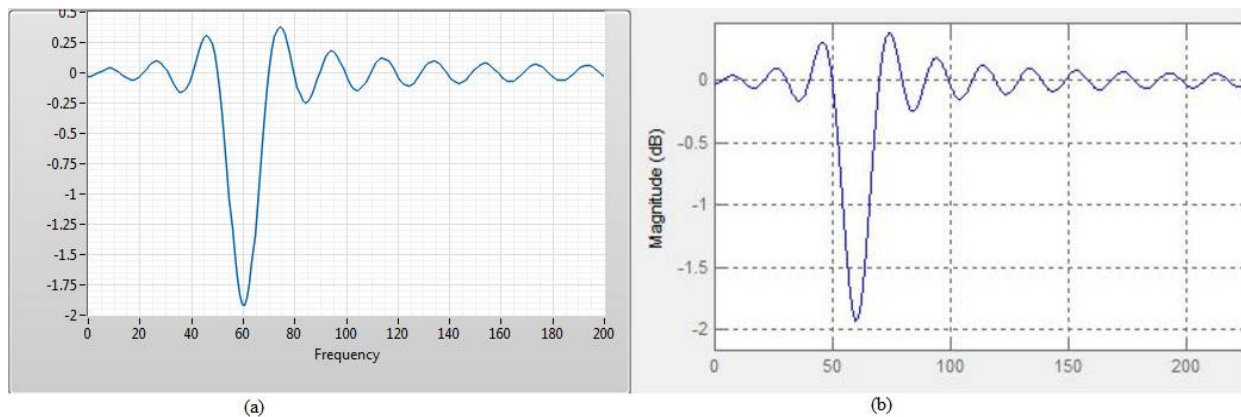


Figure 3. 24: a. LabVIEW, b.MATLAB Kaiser Window NF at 60Hz

By using different windowing techniques it is interpreted that the Kaiser Window result is better, Notch in comparison to other window is better. From the results of different windowing techniques Kaiser Window has better notch as compared to others but there is presence of ripples.

But the ripples can easily be eliminated by increasing the shape parameter (β). As this parameter increases, ripples decrease but there is a significant increase in the notch width also. Due to this reason there is a tradeoff between ripples and notch width. If the ratio of cutoff frequencies is less than 1.1 then the notch is narrowband otherwise it's a wideband filter. Eq. (13) represents the formulation of calculation for null (notch) frequency when filter is narrowband. Eq. (14) is used for calculating Quality factor.

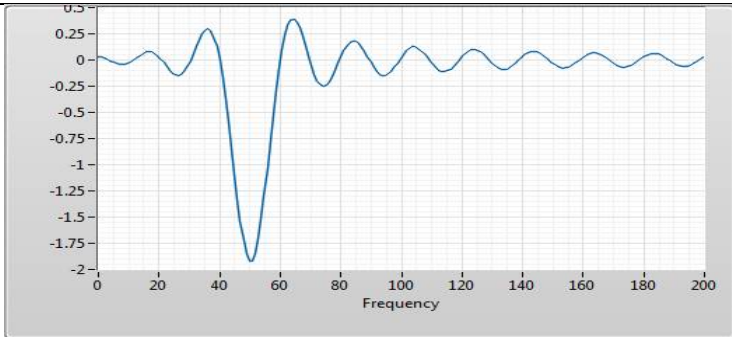
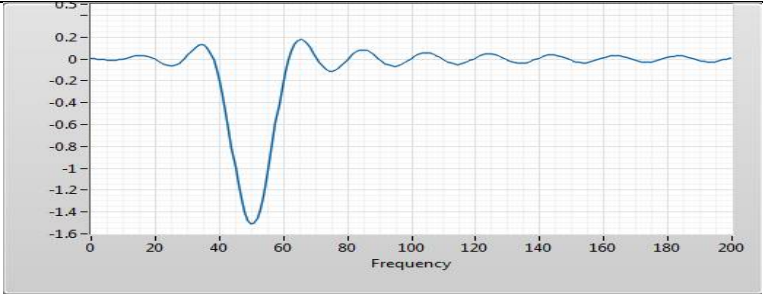
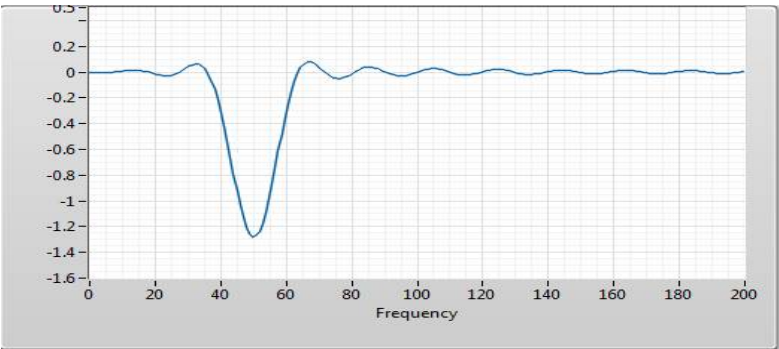
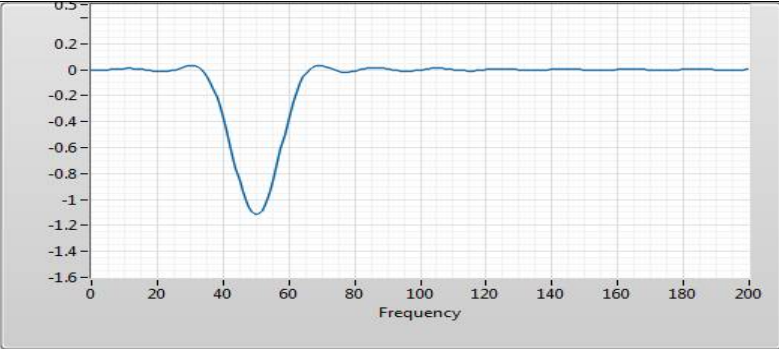
$$f_0 = \frac{f_{c1} + f_{c2}}{2} \quad (13)$$

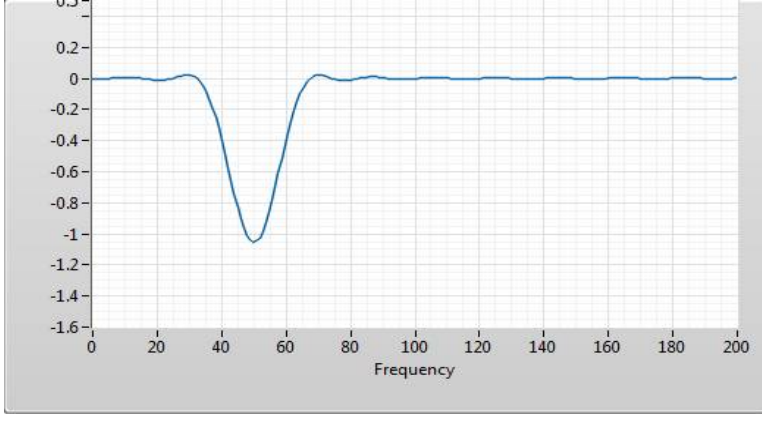
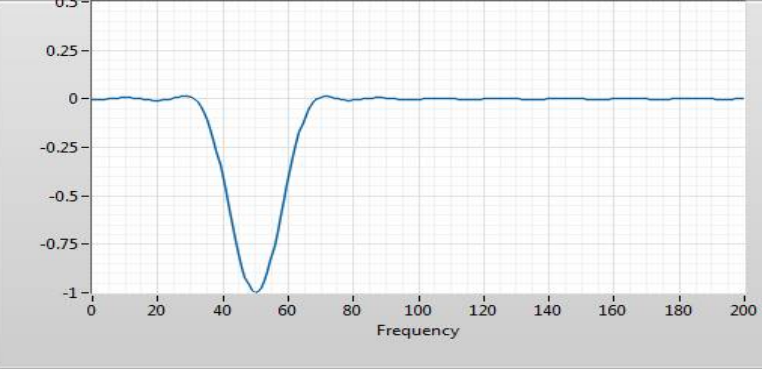
$$Q = \frac{f_{c2} - f_{c1}}{f_0} \quad (14)$$

Table 3. 7: Calculation of null frequency and Q

Window	f_{c1}	f_{c2}	Type	f_0	Q
Kaiser	49	51	Narrowband	50	0.04 (-27.95dB)
	59	61	Narrowband	60	0.033 (-29.62dB)

Table 3. 8: Effect of β on the notch filter for null frequency 50Hz

β	Output	Ripples
0.5		Present
2		Present
3		less
4		less

4.5		Minute
5		Negligible

From the above results of notch filter it is interpreted that the responses or the notch of the filter response is not going beyond -3dB point so to analyse the FIR filter using windowing technique for notch filter, we have to either increase the order of the filter or to consider some threshold value i.e. along with the removal of the power line interference it removes some signals in the given frequency range.

3.2.1 EFFECT OF GAIN OF NOTCH FILTER FOR NULL FREQUENCY 50HZ

In this section we have observed the effect of gain on the notch filter by varying order, threshold frequencies, β value for the Kaiser Window. Figure 3.24(a-e) depicts the response of filter on the order of the notch of Kaiser Window.

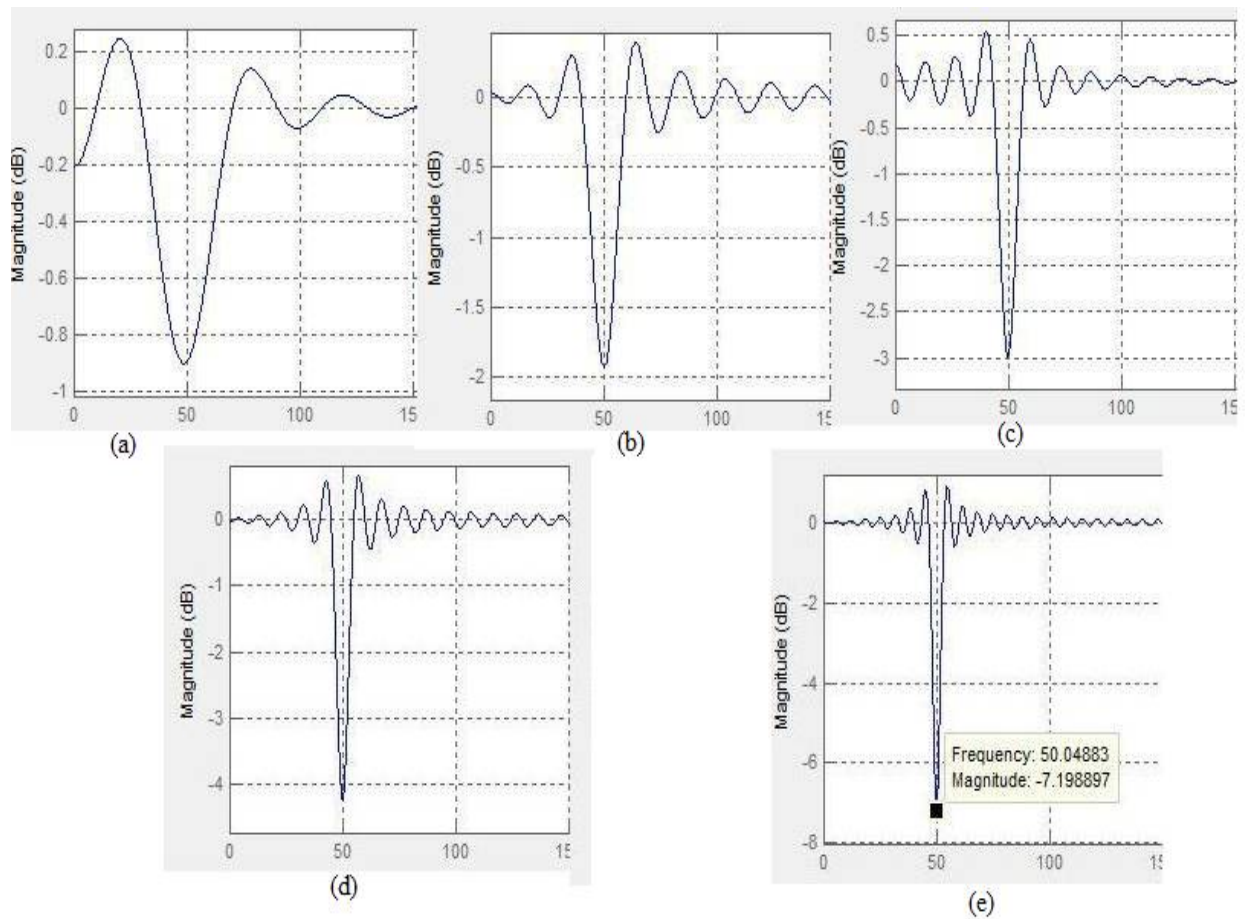


Figure 3. 25:Magnitude response on effect of order

Table 3. 9: Effect of Order on Gain of Kaiser Window

Window	Order	f_{c1}	f_{c2}	Gain(dB)	
Kaiser	a	50	49	51	-0.899
	b	100	49	51	-1.92
	c	150	49	51	-2.98
	d	200	49	51	-4.25
	e	300	49	51	-7.19

From the Table3.6 and figure3.24 it is noted that for the better notch and gain the order must be of high value.

Table 3.10: Effect of threshold frequencies on gain

Window	f_{c1}	f_{c2}	Gain(dB)
Kaiser	46	54	-11.475
	47	53	-7.40
	48	52	-4.36
	49	51	-1.95

From the above results of Table 3.7 it is interpreted that as the threshold frequency band value increases more sharper is the notch and more is the gain

Table 3. 11: Effect of β for Kaiser window on Gain with fixed threshold frequency ($f_{c1} = 46$ and $f_{c2} = 54$)

Window	β	f_{c1}	f_{c2}	Gain(dB)
Kaiser	0.5	46	54	-11.47
	1	46	54	-10.27
	2	46	54	-7.89
	3	46	54	-6.33
	4	46	54	-5.35
	5	46	54	-4.7
	6	46	54	-4.2

As the β value is increasing the gain is decreasing but the ripples are reducing and at β value 6 the pass band ripples gets vanished.

In this chapter the implementation of notch filter and the band pass filter is done successfully and it is interpreted that for the removal of the Power Line Interference Noise from the biomedical signal the FIR Windowing method is best suited and among the windows Kaiser Windows shows superior results in terms of magnitude and notch width.

CHAPTER-4

ELIMINATION OF LOW AND HIGH FREQUENCY NOISES USING DIGITAL FILTERING TECHNIQUES

Biomedical signals are electric activities accrued from the body. Some of the usual signals are the ECG and the EEG. These signals are of outstanding cost because of the fact that they may be used for diagnostic functions. Importantly, most of them can be accrued the usage of non-invasive methods. These attributes, collectively with the great modern advances in electronic and virtual processing technology, have made biomedical signal information an crucial supply of records utilized in medical diagnostics.

Many of the digital indicators consist of noise which in this situation is any unwanted signal that corrupts the signal of hobby. The heat generated inside the electric and electronics signals inside the movement and surroundings between the situation and sensors are a number of the noise resources. In order to extract vital records from the signal, noise should be eliminated. In the processing of the biomedical signals, filtering is crucial.

The FT expresses the signal using the sinusoidal basis which might be expressed as a feature of sines and cosines. This is regularly one of the several ways of remodeling the signal into frequency domain. The frequency area representation basically tells approximately the frequency aspect in signals and the amplitudes of those frequencies. This amplitude distribution across frequency easily filters the undesirable indicators (noise). The filtered signalal can be transformed again into time function using a inverse of Fourier transforms. However it a long way less difficult to manage the signal within the frequency area. Therefore the signalal is usually retained within the frequency domain for further processing.

The principal goal of this bankruptcy is to layout an optimum filter out to put off the specific noises in the biomedical signals which include (Baseline Wander Noise) and Electromyography Noise using High pass and Low pass filtering.

Low Frequency Noise

While obtaining the ECG signals the problem arises due to frame starching, walking, push-up, walking, pull-up the body. In these instances, the ECG signals receives drifted from its unique position with a excessive degree from the baseline. This waft from baseline is known as baseline wandering. Baseline wander method that the lowest axis of ECG signals seems to move up and down as opposed to being directly as anticipated. The HPF with cut off frequency of zero.5Hz may be used to eliminate the effect because of the baseline wandering, which can be used to filter out signals element with frequency below 0.5Hz.

High Frequency Noise

In biomedical application the presence of muscle noise creates a lot of problems, mainly in recordings acquired during exercise, since low amplitude waveforms may become completely obscured. 50/60 Hz interference and Muscle noise is, in contrast to baseline wander no longer eliminated by using narrowband filtering, but presents a far more hard filtering problem since the spectral content of muscle hobby extensively overlaps.

The main aim of this chapter is to choose the best filter which can remove Baseline Wander Noise and Electromyography Noises.

There are many filters existing in literature with the help of which, different noises can be removed namely : Gaussian Filter, Moving Average Filter, Savitzky Golay Filter.

Gaussian Filter A filter whose impulse response is a Gaussian function is termed as Gaussian filter in signal processing).It minimises the rise and fall time and also has the property of no overshoot to the inputs having step. These behaviours of the Gaussian filter makes the group delay response minimum.Just like the sinc which is considered idealin the frequency domain this Gaussian Filter is considered the ideal time domain filter which are very useful in areas such as digital telecommunication systems and oscilloscopes.

The one-dimensional Gaussian filter has an impulse response given by Eq.(15).

$$g(x) = \sqrt{\frac{a}{\pi}} \cdot e^{-ax^2} \quad \text{where } a \text{ is constant} \quad (15)$$

Moving Average Filter : For smoothing of a series of digital data a Low Pass FIR filter is commonly used which is called as Moving Average. For producing a single output this Moving Average filter takes the M number of samples and calculates the averages of those samples. In communication and digital engineering this filter is commonly used because of its simplicity in designing which can be very useful and efficient in filtering out the noisy part from the signals. In order to increase the smoothness of the filter output the number of samples, M increased but it blunts the sharp transition of the data which results in less effective in frequency response and proven best for the time domain response. The difference equation is given by eq.16:

$$y[n] = \frac{1}{N} \sum_{i=0}^{N-1} x[n-i] \quad (16)$$

In Eq.16 , x[n] represents current input ,y[n] represents current output, , x[n-1] denotes previous input, and the length of the average filter is denoted as N.

Savitzky Golay Filter:

The main purpose of using savitzky golay filtering is to get the smoothed signal, It is mainly used in filtering of High frequency noises also it gives the output without distorting the original signal and it is widely used in the digital filtering. The main functioning of this filter is the convolution process on the data set which is shown by equation 17

$$Y_j = \sum_{i=\frac{1-m}{2}}^{\frac{m-1}{2}} C_i Y_{j+i} \quad \frac{m-1}{2} \leq j \leq n - \frac{m-1}{2} \quad (17)$$

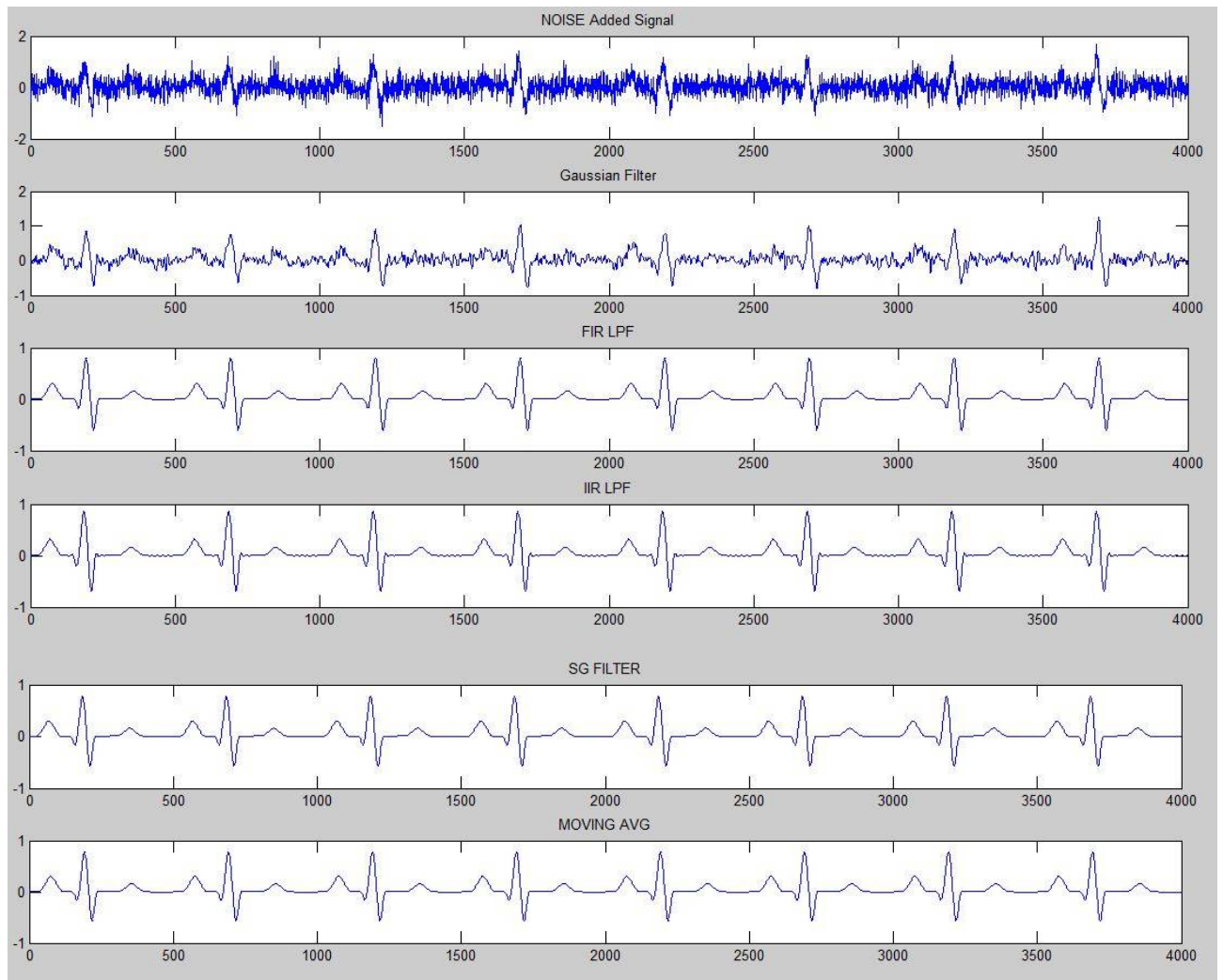


Figure 4.1: Filtering of AWGN noisy signal using different filters

Table 4.1: SNR calculation of AWGN noisy and denoised signals

Type of Filter	SNR(dB) before filtering	SNR(dB) after filtering
Gaussian	-2.5069	1.1473
FIR (order 1)	-2.5069	24.7763
IIR (order 1)	-2.5069	17.4921
S Golay Filter	-2.5069	16.0117
Moving Average	-2.5069	3.6355

After calculating SNR of filtered signals from different filters, the FIR and IIR filters are showing the remarkable results to remove the AWGN noises which are further used for our project work.

4.1 ELIMINATION OF HIGH FREQUENCY NOISES

A filter which is capable of passing range of frequencies lower than f_c and attenuates the frequencies above f_c is known as Low Pass Filter(LPF) and this filter can eliminate the High frequency noises present in Biomedical Signals. The ideal frequency response of the filter is shown in Fig4.2.

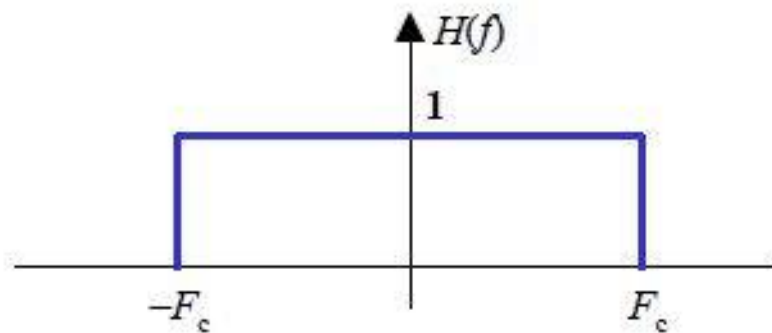


Figure 4.2: Frequency response of Low pass Filter[1]

The equation of frequency response for High Pass Filter is given by Eq. (18).

$$H_d(f) = \begin{cases} 1 & |f| < f_c \\ 0 & \text{otherwise} \end{cases} \quad (18)$$

4.1.1 IMPLEMENTATION OF IIR FILTER USING BUTTERWORTH APPROXIMATIONS

The frequency response of “ n^{th} ” order of Butterworth filter is expressed by Eq. (19)

$$H(j\omega) = \frac{1}{\sqrt{1 + \epsilon^2 \left(\frac{\omega}{\omega_p}\right)^{2n}}} \quad (19)$$

n is the filter order and the result of frequency response of filter is depicted in Fig 4.3

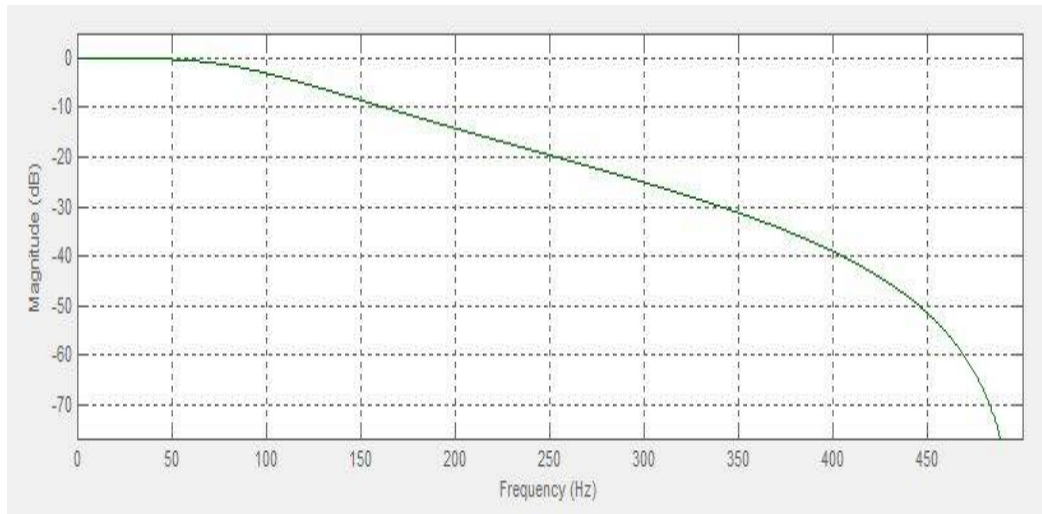


Figure 4.3: Frequency response of Butterworth low pass filter at $f_c = 100\text{Hz}$

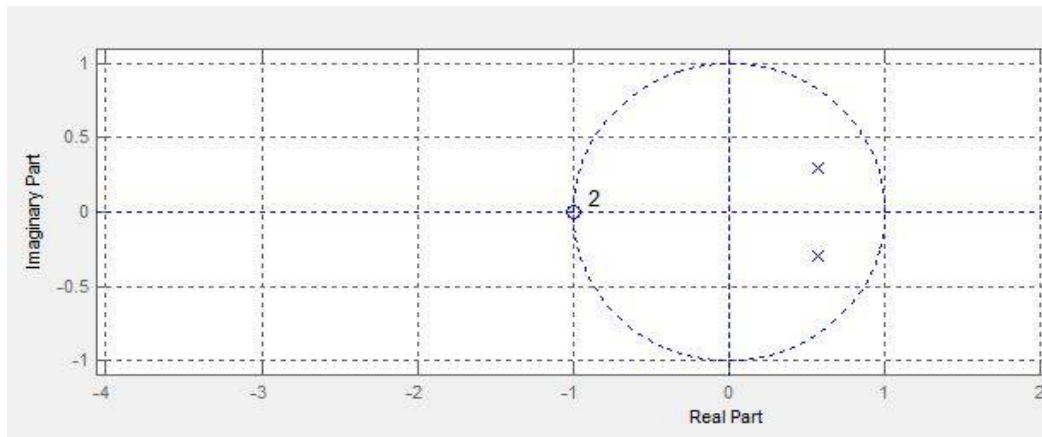


Figure 4.4: Butterworth filter of order 2, Pole Zero Plot

From the results of fig 4.3 it is depicted that the transition is not sharp this is not acceptable so to remove this disadvantage FIR filtering has been done.

4.1.2 IMPLEMENTATION OF FIR FILTER USING WINDOWING TECHNIQUES

In order to remove the High frequency noises from the biomedical signal the FIR windowing method is chosen to overcome the problems occurred in the IIR low pass filtering. In this section the Low Pass Filter is designed using the LabVIEW software where the responses of different windows are studied and effect of order is also studied.

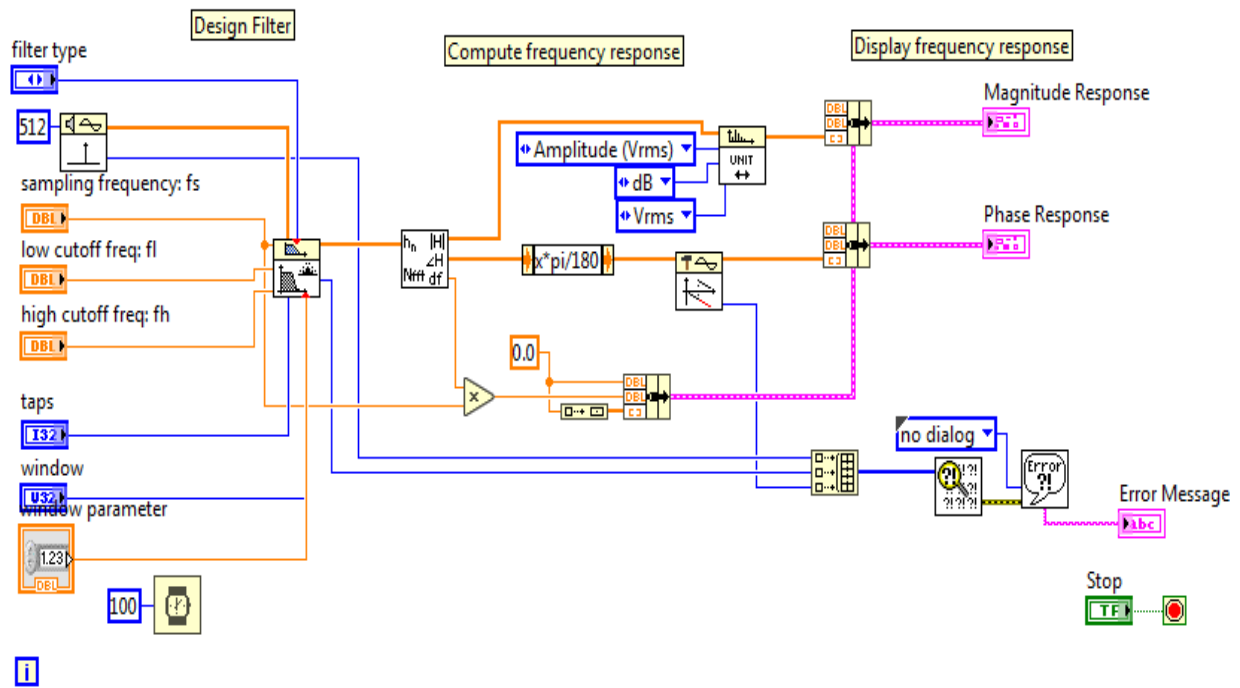


Figure 4.5: Implementation of Low Pass filter Using Labview

Hamming Window: The result of Hamming window for Electromyography noise removal as shown in Fig.4.6

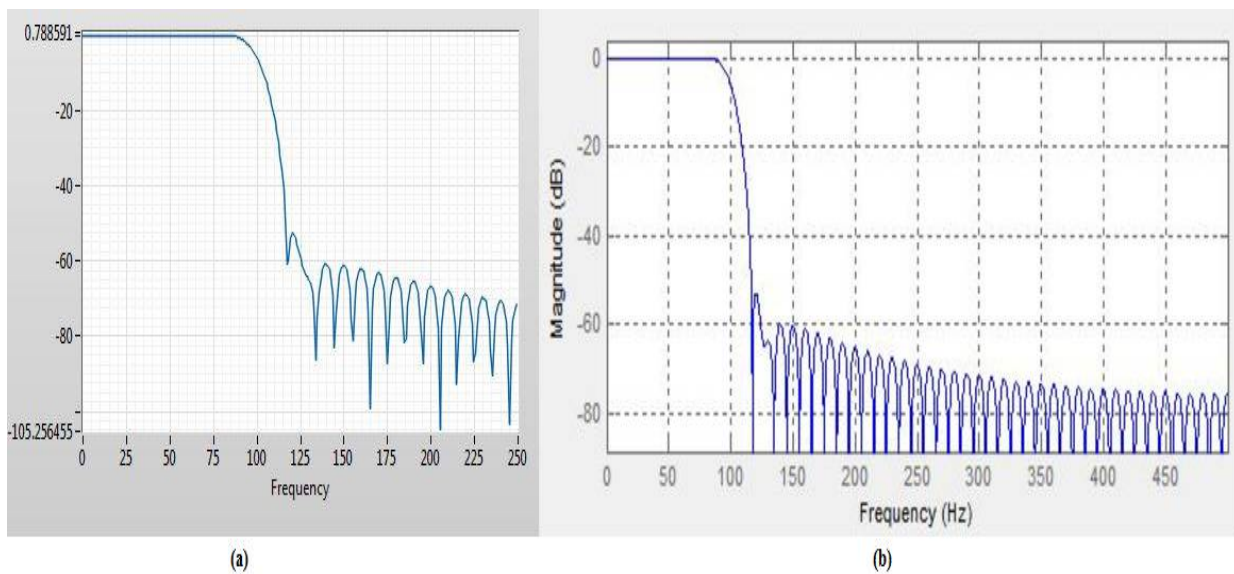


Figure 4.6: a. LabVIEW, b.MATLAB Hamming Window LPF at 100Hz

Hanning Window: The result of Hanning window for Low Frequency noise removal as shown in Fig.4.7

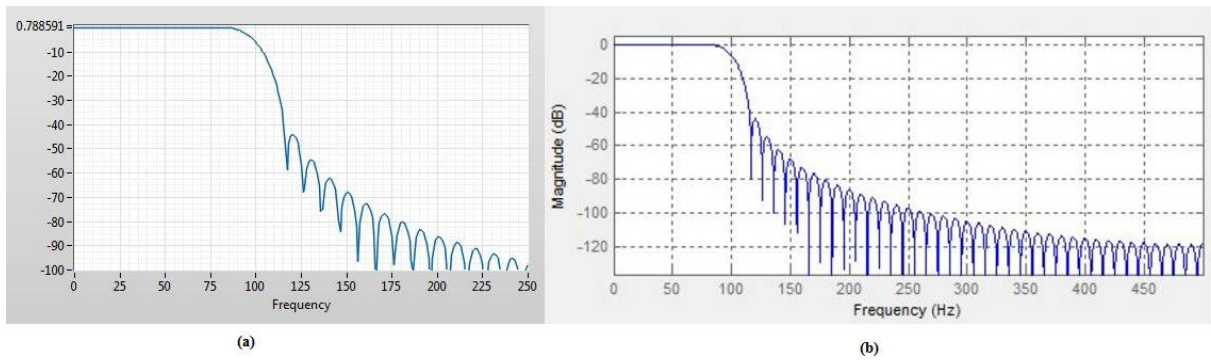


Figure 4.7: a. LabVIEW, b.MATLAB Hanning Window LPF at 100Hz

Kaiser Window: The result of Kaiser Window for Low Frequency noise removal as shown in Fig.4.8

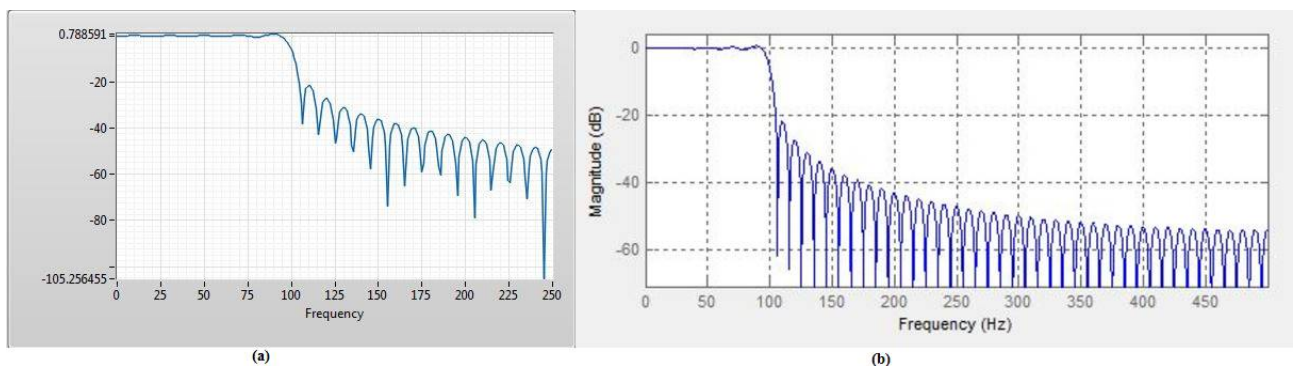


Figure 4.8: a. LabVIEW, b.MATLAB Kaiser Window LPF at 100Hz

Rectangular Window: The result of Rectangular window for Low Frequency noise removal as shown in Fig.4.9

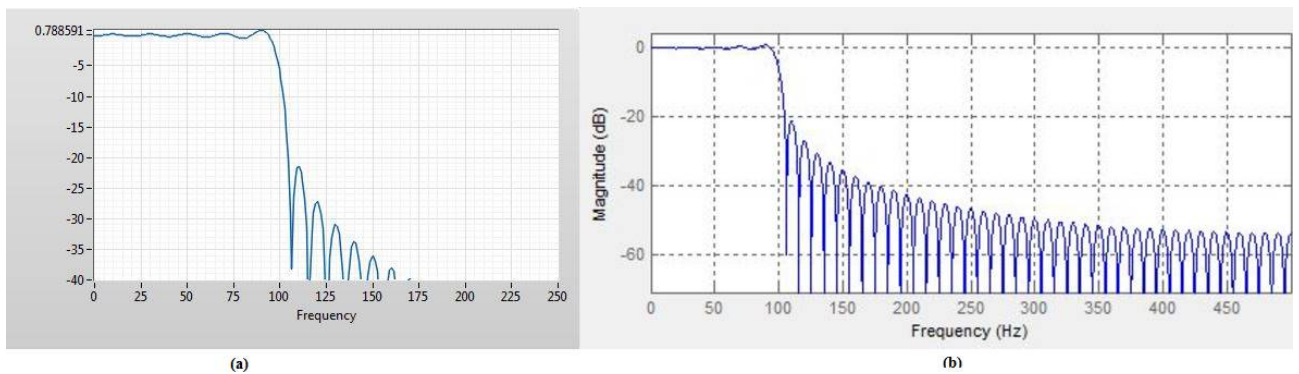


Figure 4.9: a. LabVIEW, b.MATLAB Rectangular Window LPF at 100Hz

Blackman Window: The result of Blackman window for Electromyography noise removal as shown in Fig. 4.10

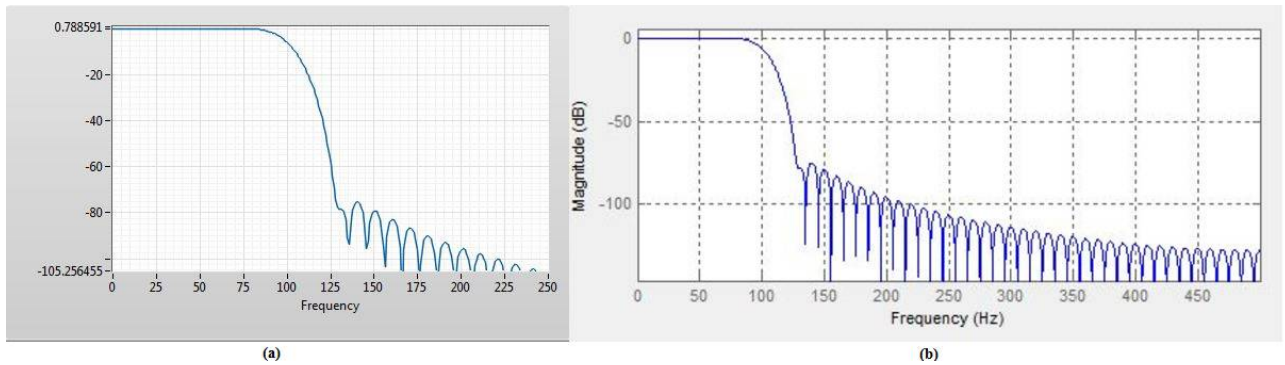


Figure 4.10: a. LabVIEW, b.MATLAB Blackmann Window LPF at 100Hz

Gaussian Window: The result of Gaussian window for Electromyography noise removal as shown in Fig. 4.11

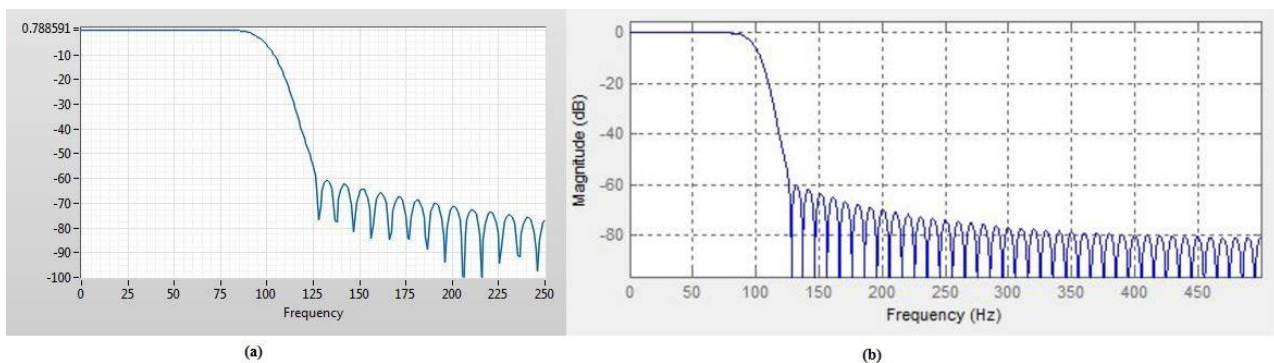


Figure 4.11:a. LabVIEW, b.MATLAB Gaussian Window LPF at 100Hz

Table 4.2: Gain effect on filter order of Kaiser Window of $f_c = 100\text{Hz}$

Order	Gain(dB)
10	-60
50	-52
100	-38
200	-27
301	-22

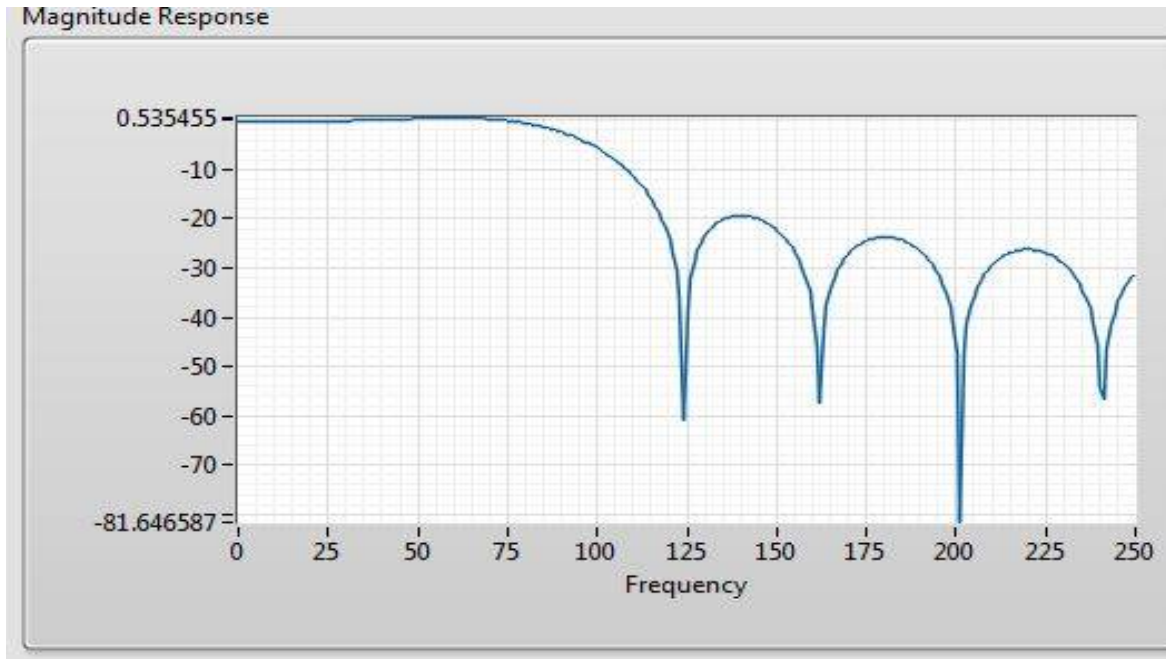


Figure 4.12: LPF of order 10 Frequency response for Kaiser Window

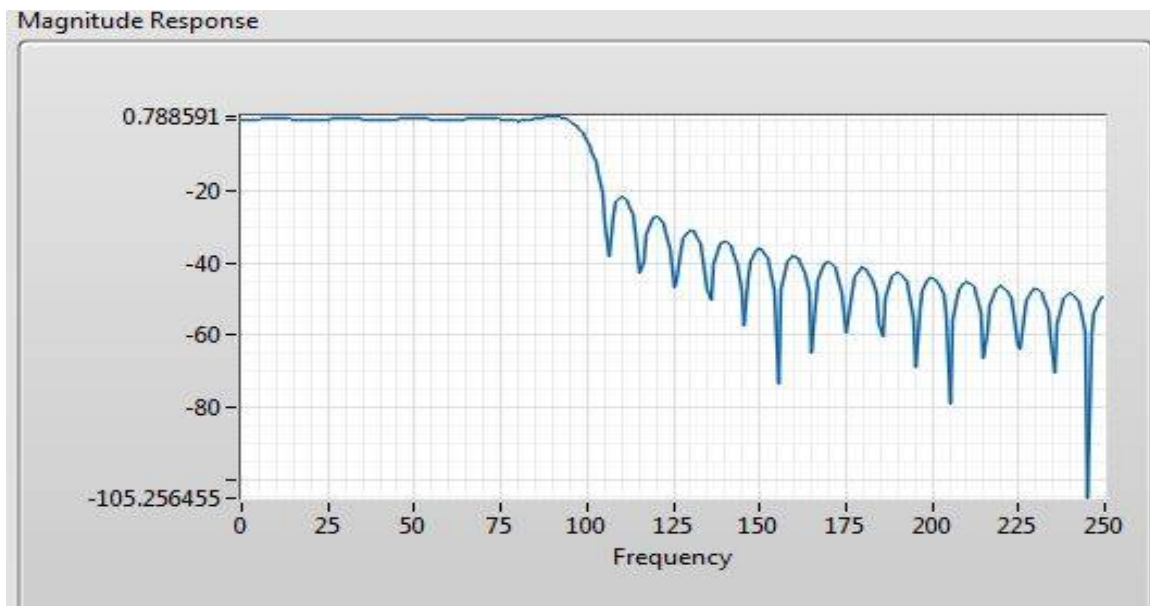


Figure 4.13: LPF of order 100 Frequency response for Kaiser Window

From Table 4.2, Fig 4.12 and Fig 4.13 it is interpreted that as the order of the LPF increases, the gain comparatively decreases but the transition is getting sharper. This is the major requirement for removing of Low Frequency Noises. We have successfully designed a filter using LabVIEW which removes HF noise from biological signals.

4.2 ELIMINATION OF LOW FREQUENCY NOISES

A filter which is capable of passing range of frequencies greater than the f_c and attenuates the frequencies below f_c is known as High Pass Filter(HPF) and this filter can eliminates the Low frequency noises present in Biomedical Signals. The ideal frequency response of the filter is shown in Fig4.14.

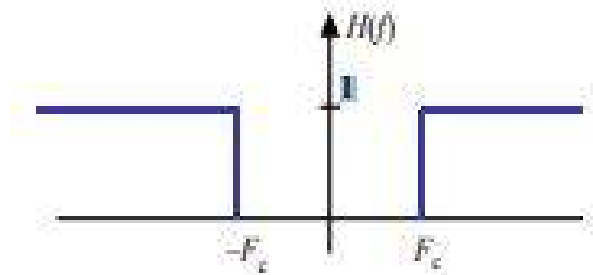


Figure 4.14: Frequency response of High Pass Filter [1]

The equation of frequency response for High Pass Filter is given by:

$$H_d(f) = \begin{cases} 0 & |f| < f_c \\ 1 & \text{otherwise} \end{cases} \quad (15)$$

4.2.1 IMPLEMENTATION OF IIR FILTER USING BUTTERWORTH APPROXIMATION

The IIR High pass filter is implemented and its frequency response and pole zero is studied.

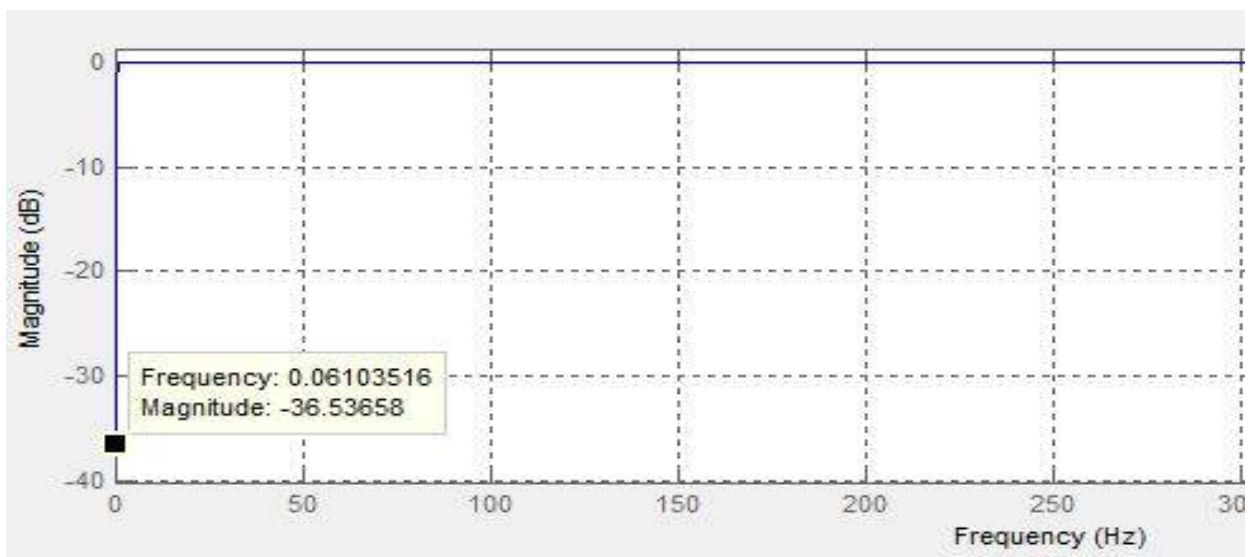


Figure 4.15: Frequency response of IIR High Pass Filter of Order 2

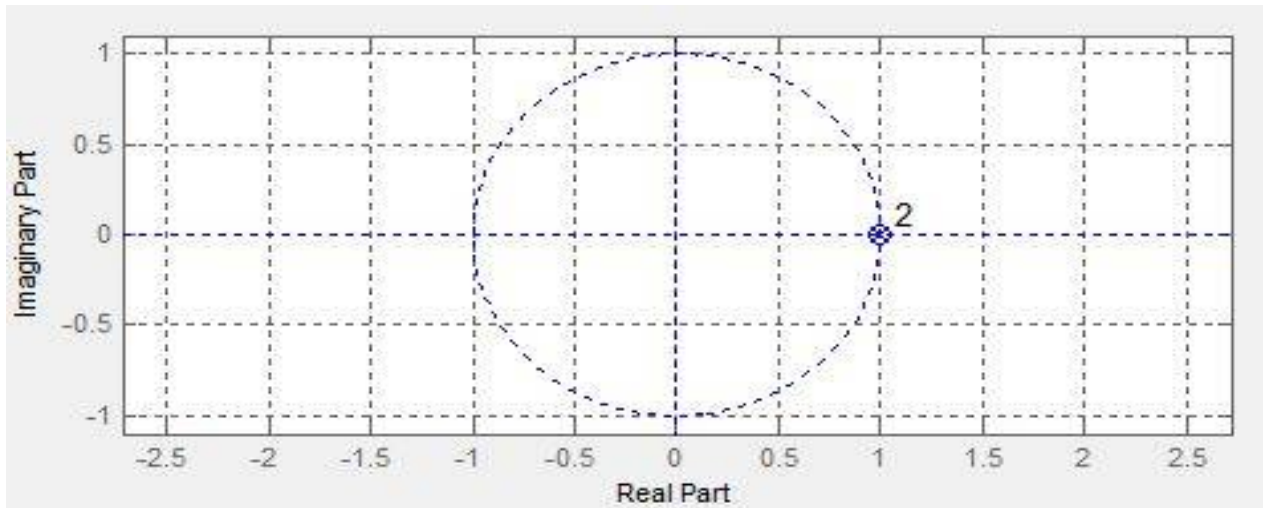


Figure 4.16: IIR HPF order 2 Butterworth Pole Zero plot

From results of IIR HPF implementation it is seen that for 1st order filter gain is approximately -18.33dB and for 2nd order gain is -36.53dB which means that as order of IIR filter increases the value of gain increases because of several disadvantages of IIR filter it is not widely used and one disadvantage is its infinite impulse response which is shown in Fig4.16

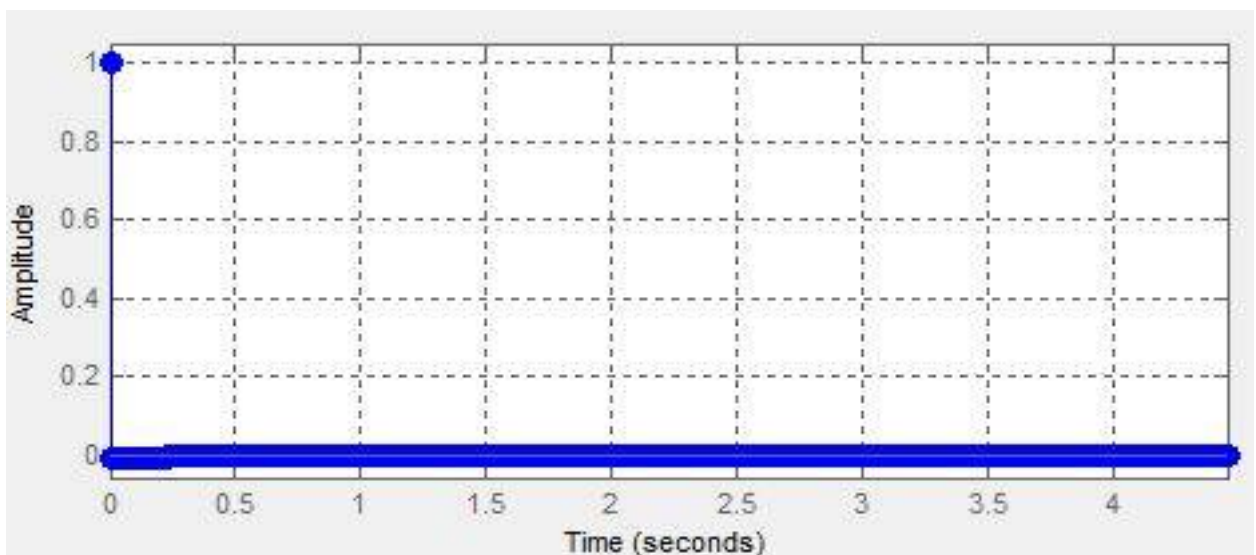


Figure 4.17:HPF Impulse Response order 2

From the above results it is interpreted that if the order of IIR filter increases the gain factor is getting more better but the complexity also gets increase and the impulse response is infinite so to reduce this complexity FIR filter using windowing technique is chosen.

4.2.2 IMPLEMENTATION OF FIR FILTER USING WINDOWING TECHNIQUES

In order to remove the Low Frequency noises from the biomedical signal the FIR windowing method is chosen to overcome the problems occurred in the IIR low pass filtering. In this section the High Pass Filter is designed using the LabVIEW software where the responses of different windows are studied and effect of order is also studied.

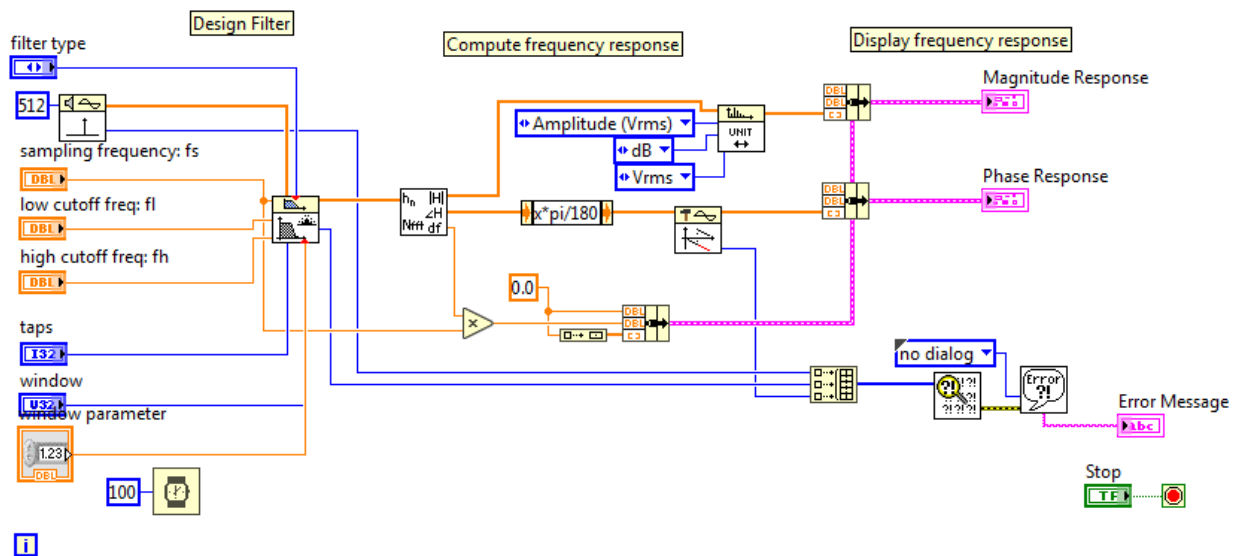


Figure 4.18: Implementation of High pass filter using Labview

The effect of frequency response of the designed FIR HPF using different windows is shown in later section.

Hamming Window: The result of Hamming window for Low Frequency noise removal as shown in Fig.4.19

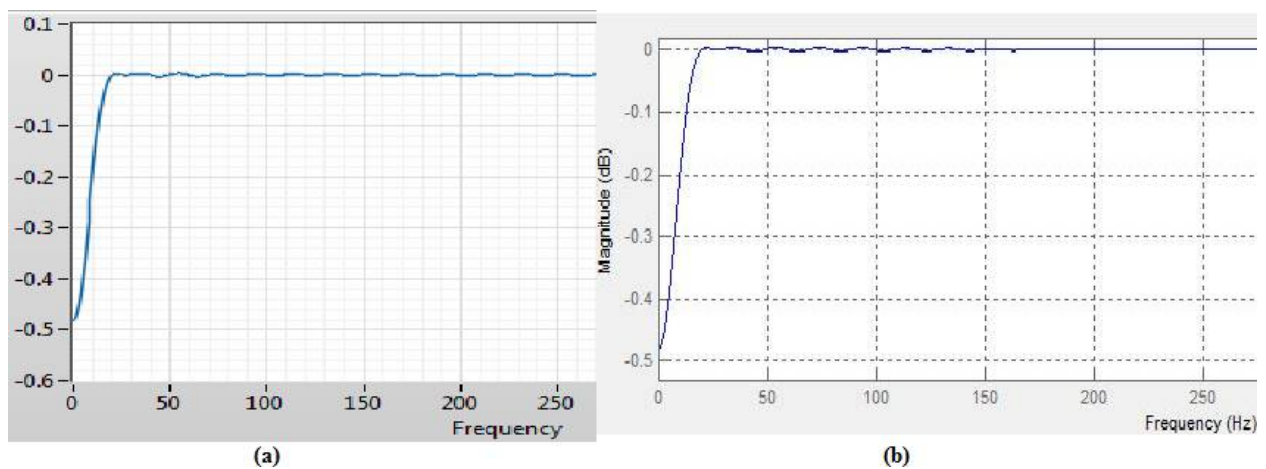


Figure 4.19:a. LabVIEW, b.MATLAB Hamming Window HPF at 0.5Hz

Hanning Window: The result of Hanning window for Low Frequency noise removal as shown in Fig. 4.20

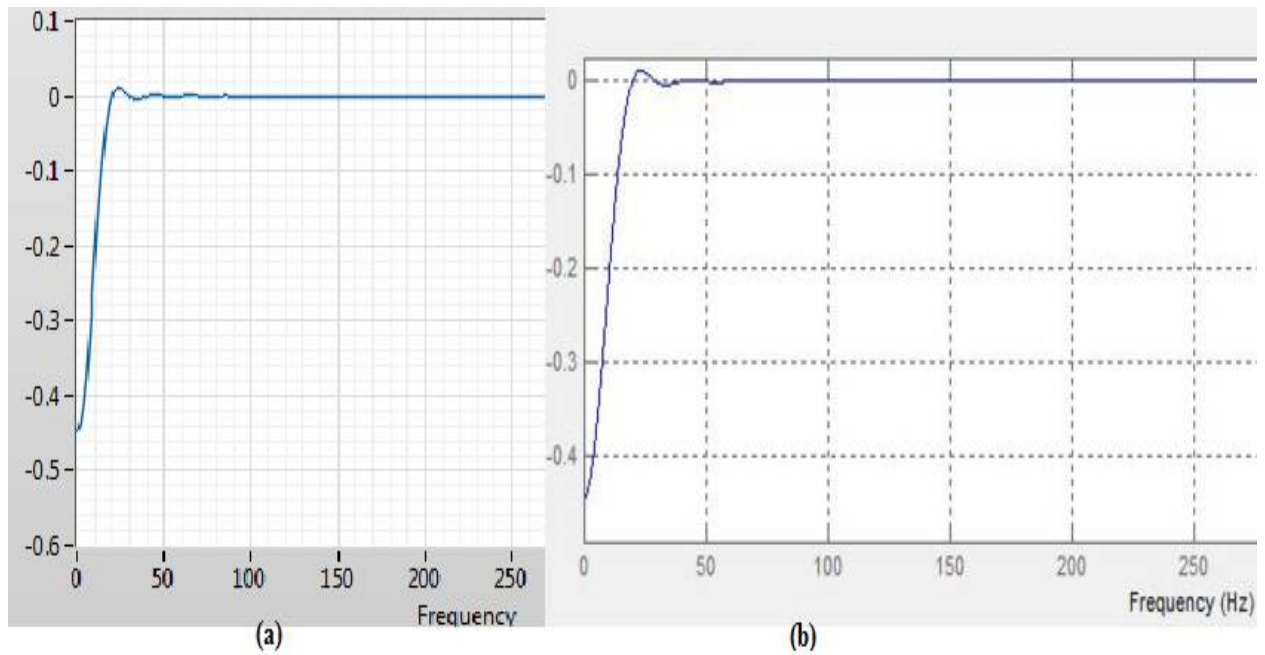


Figure 4.20: a. LabVIEW, b.MATLAB Hanning Window HPF at 0.5Hz

Kaiser Window: The result of Kaiser window for Low Frequency noise removal as shown in Fig.4.21

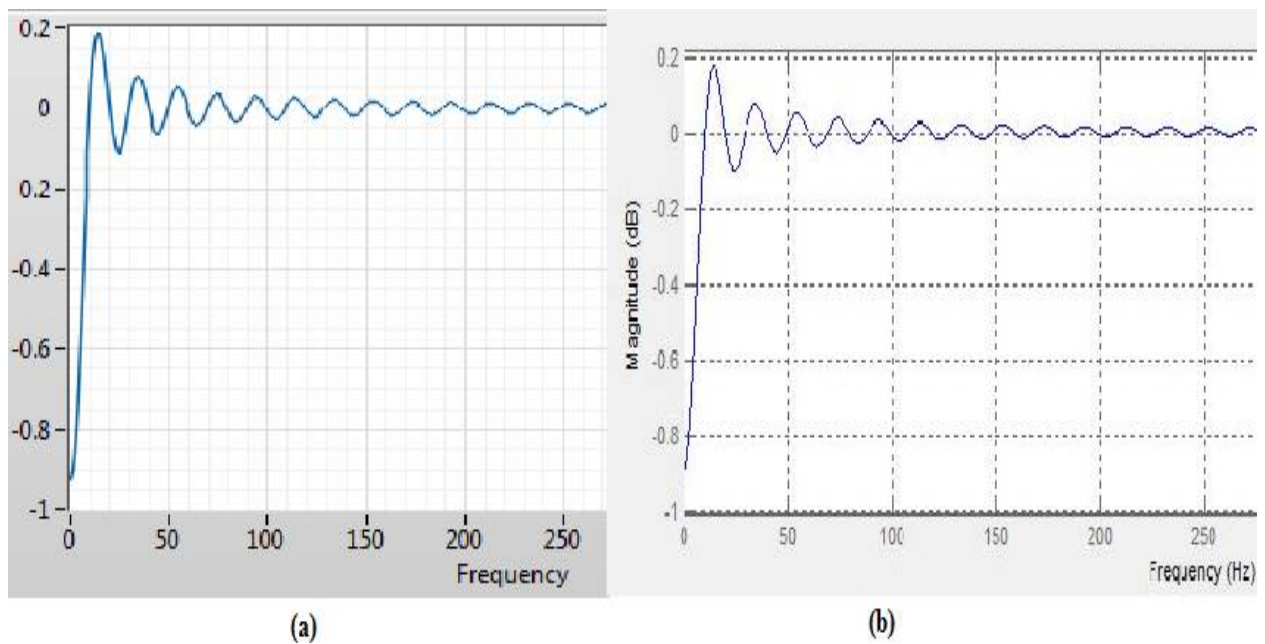


Figure 4.21:a. LabVIEW, b.MATLAB Kaiser Window HPF at 0.5Hz

Blackman Window: The result of Blackman window for Low Frequency noise removal as shown in Fig. 4.22

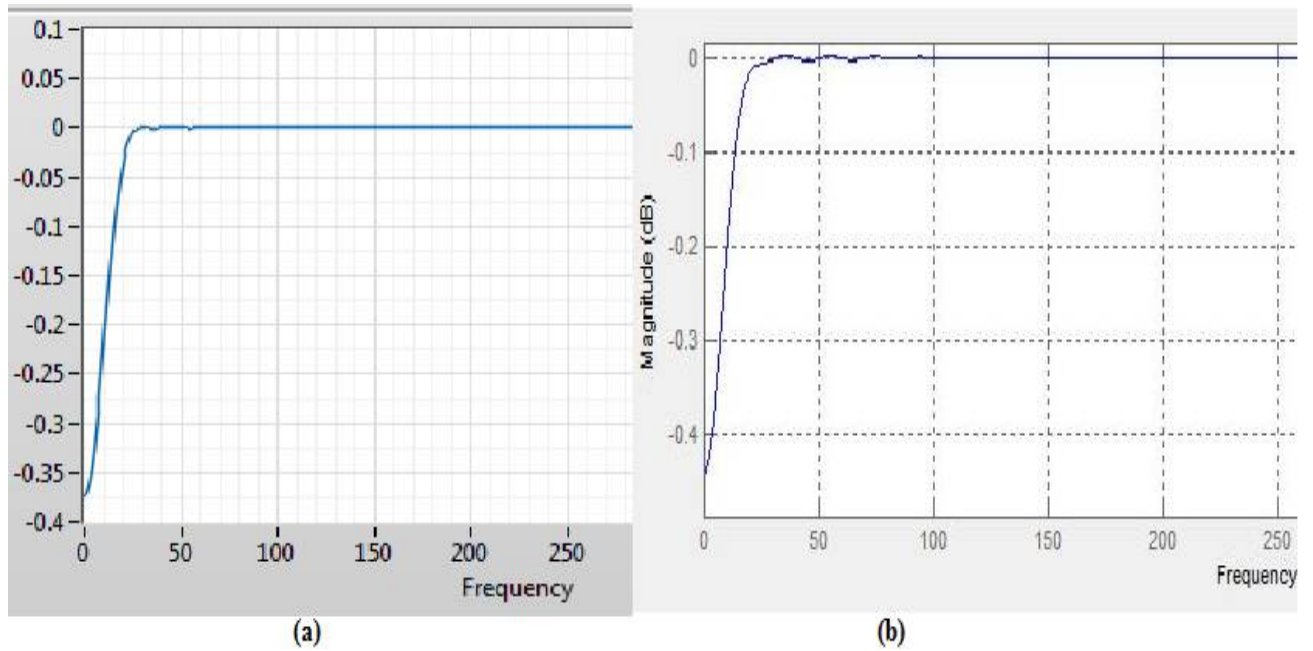


Figure 4.22: a. LabVIEW, b.MATLAB Blackmann Window HPF at 0.5Hz

Gaussian Window: The result of Gaussian window for Low Frequency noise removal as shown in Fig.4.23

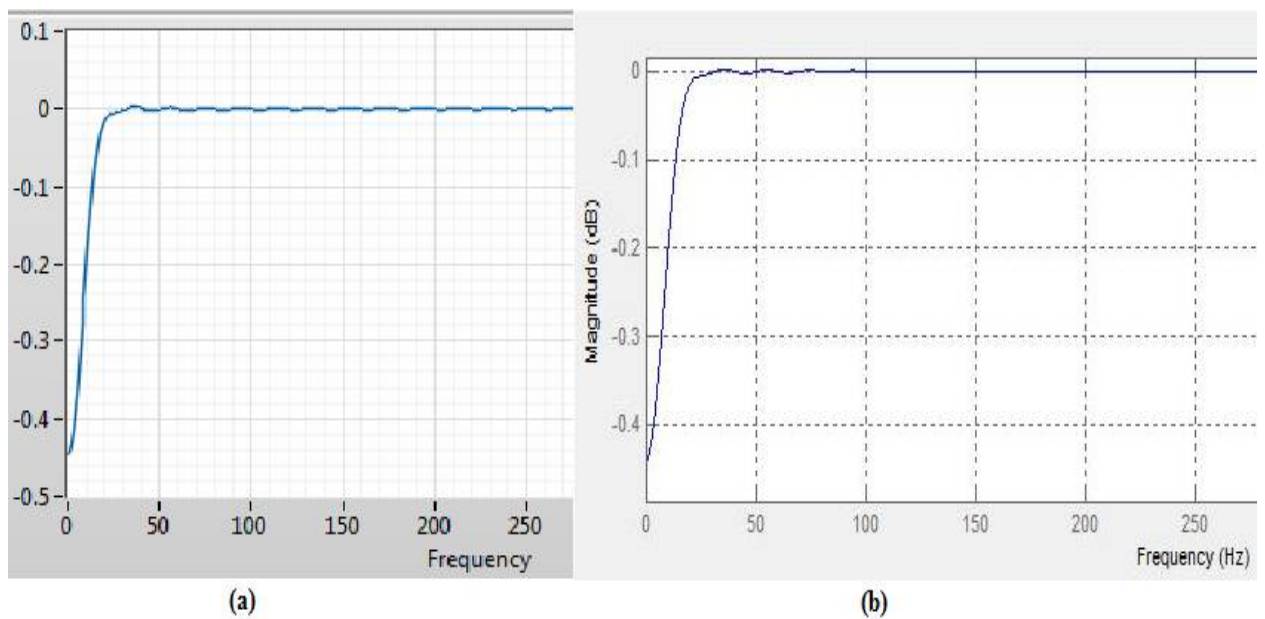


Figure 4.23: a. LabVIEW, b.MATLAB Gaussian Window HPF at 0.5Hz

Rectangular Window: The result of Rectangular window for Low Frequency noise removal as shown in Fig.4.24

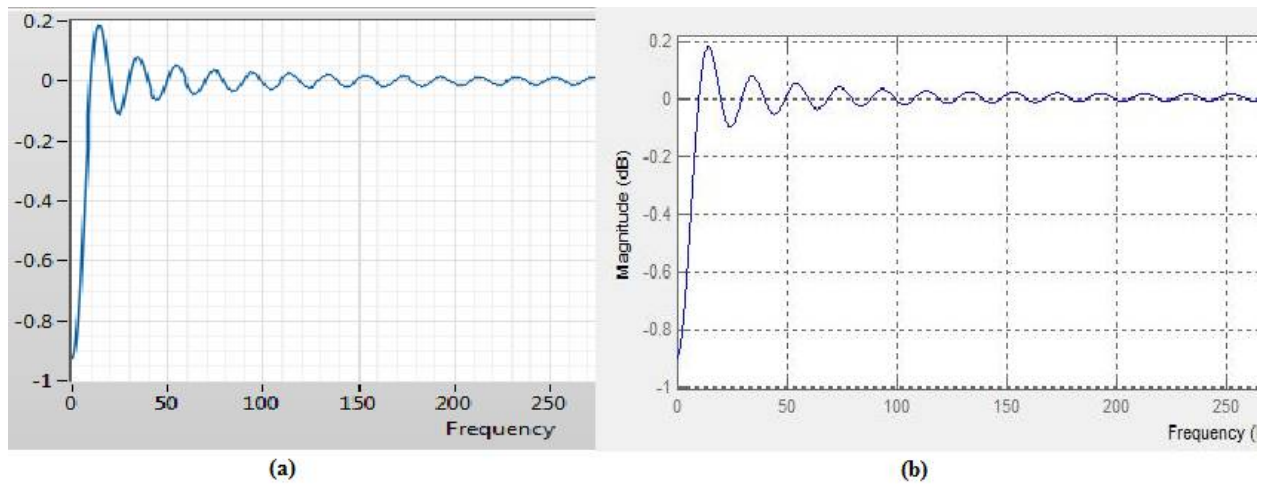


Figure 4.24: a. LabVIEW, b.MATLAB Rectangular Window HPF at 0.5Hz

From the results of above responses of different filter it is found that Kaiser Windows is showing best result in comparison to all filters in terms of gain.

4.2.3 EFFECT OF ORDER ON THE GAIN USING KAISER WINDOW

The Kaiser window response is studied with different order of the filter in order to get the optimum filter. However, for linear-phase (symmetric) FIR filters, the delay can be expressed as in eq.16:

$$D = \frac{\text{Order}}{2} = \frac{N_{\text{taps}}-1}{2} \text{ samples} \quad (16)$$

Table 4.3: Effect of order on the gain of FIR HPF

Order	Gain(dB)
11	-56.89
51	-44.13
101	-38.31
201	-32.48
251	-30.64
301	-29.16

The results depicted from Table 4.3, that as the filter order increases, the gain value seems to drop but transition is getting sharper.

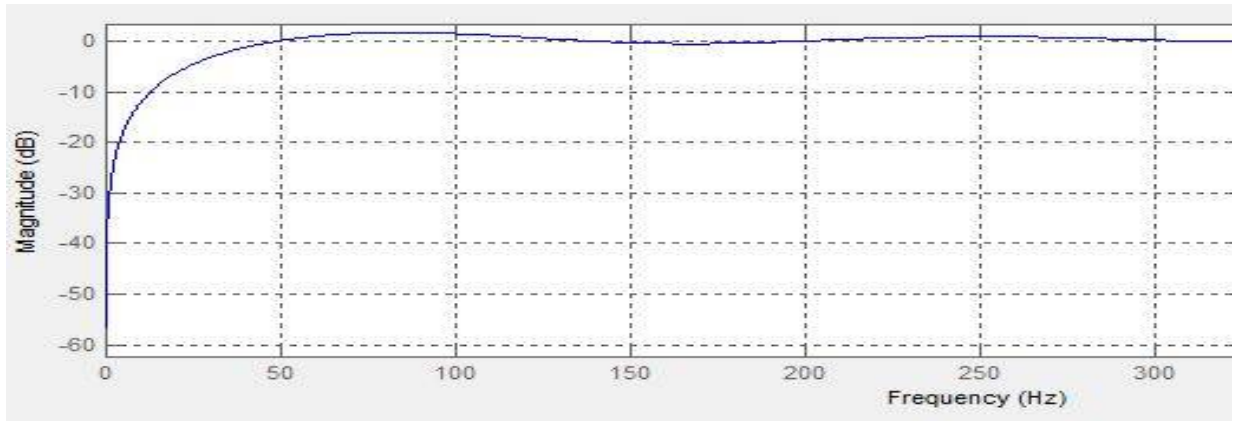


Figure 4.25: FIR HPF order 11 at $f_c=0.5\text{Hz}$

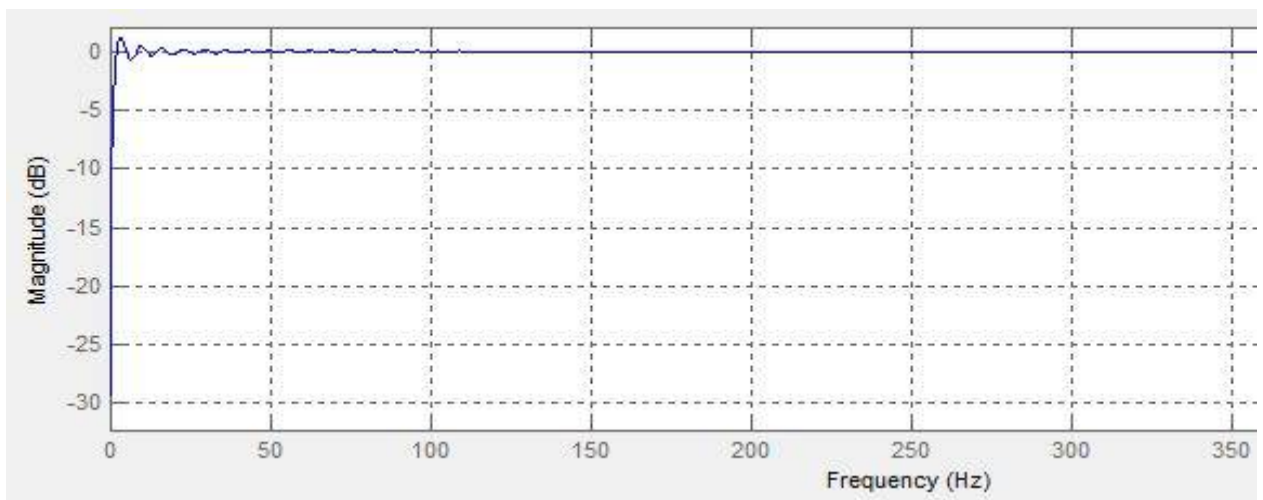


Figure 4.26: FIR HPF order 301 at $f_c=0.5\text{Hz}$

Fig 4.27 and Fig 4.28 depicts impulse and pole zero response of order 11

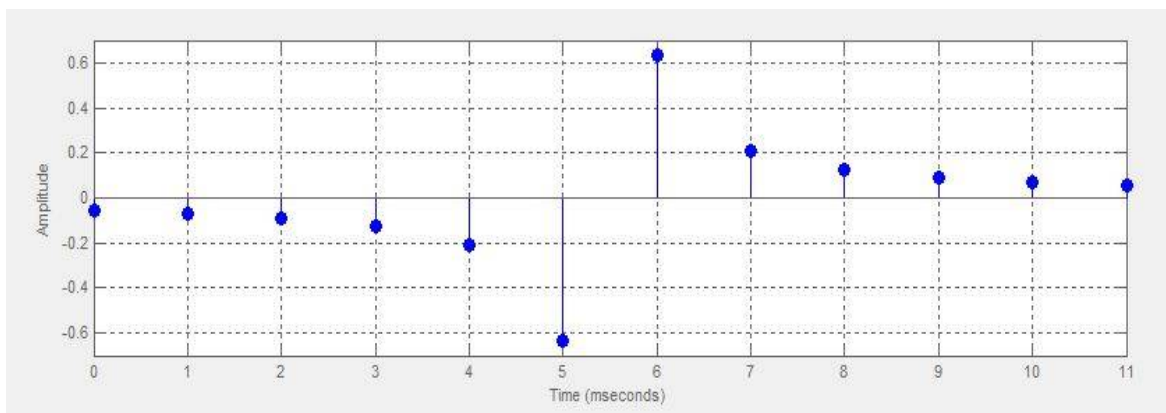


Figure 4.27: FIR HPF order 11 Impulse iresponse

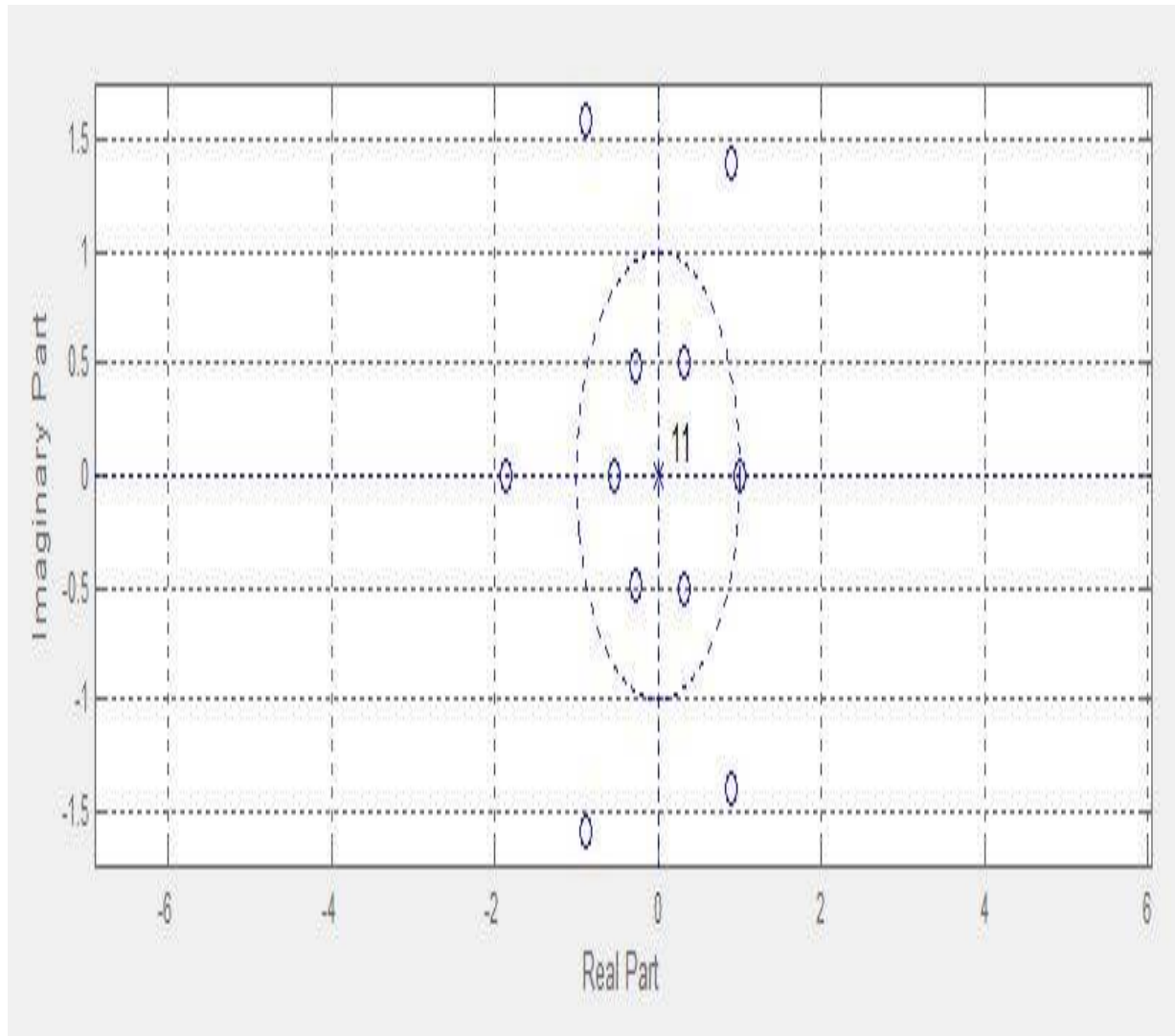


Figure 4.28:High Pass Filter(order 11) Pole zero plot

It is depicted that the impulse response length is even, anti-symmetric and has zero at $z = 1$ this represents that the filter is of Type 4 and is best suited for the high pass filtering. For the linear phase filtering the order of the filter must be an odd integer.

In this chapter the implementation of FIR and IIR Low Pass, High Pass filter is done successfully and it is interpreted that for the removal of the Low and High frequency noise from the biomedical signal the FIR High Pass and Low Pass filter respectively using windowing method is best suited and among the different windows Kaiser Windows shows better results in terms of magnitude and transition width.

CONCLUSION

In this project the main aim is to design an optimum filters which are capable of removing the various noises present in the biomedical signals. The main noises which are taken are 50/60 Hz power supply noise baseline wander noise and electromyography noises. From the literature and many research articles it is studied that these noises are removed by notch filter, highpass filter and low pass filter respectively. For the filtering purpose there are many techniques available but here main emphasis is given to the windowing techniques because of the availability of well structured equations and its smooth tapering at the ends. For the implementation of filters the LABVIEW software is used and the results are verified with the help of MATLAB. According to the Impulse response the FIR filter are given priority because of its stability factor and its finite impulse response nature, another reason to choose this filter is when the AWGN noisy signal is passed through several filters and among all those filter the FIR filter's SNR was comparatively better.

All the filters are designed using windows such as Hamming, Hanning, Kaiser, Rectangular, Blackamnn and Gaussian, among all the windows the best one is found Kaiser because of its sharp response and shape parameter(β) which can wisely be adjusted to get the desired response.

It is also interpreted that as the order of the filter increases the response is getting more better because the high order filter provides better roll off rates between passband and stopband. These are very necessary ito achieve required levels of attenuation or sharpness of cutoff.

Further in future this project can be taken to the Field Programmable Gate Array(FPGA) for the practical implementation.

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LIST OF PUBLICATIONS

- Jain S., Kashyap M., Garg M., Srivastava S., “Design and Simulation of Optimum FIR Digital Filters using Windowing Technique”, The 3rd International Conference on Recent Innovations in Computing (ICRIC-2020), 20th-21st March, 2020, Central University of Jammu, J & K.
- Srivastava S. ,Jain S., “Optimum Digital Filter Design for Removal of different Noises from Biomedical Signals” 1st International Conference on Mobile Radio Communications and 5G Networks MRCN-2020 26th -28th March, 2020 U.I.E.T-KUK

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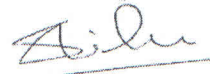
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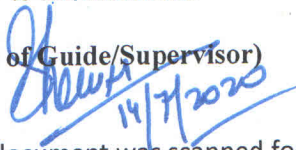


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