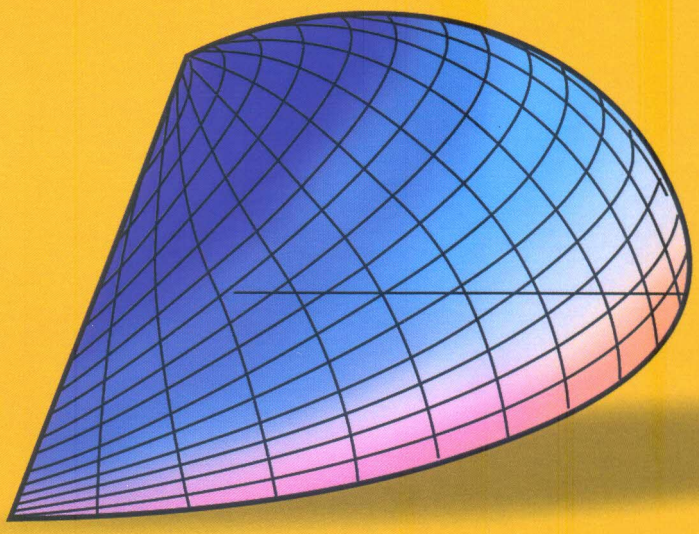
Rakesh Kumar Bajaj • Abhishek Guleria

Spherical Fuzzy Information and Graphs with Soft Computing Applications



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Rakesh Kumar Bajaj
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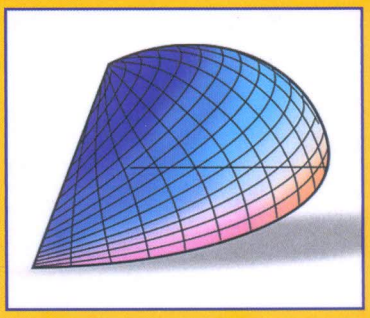

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*"**Spherical Fuzzy Information and Graphs with Soft Computing Applications**"* presents the enhanced and comprehensive structure of spherical fuzzy information and its computational applications. The book contains seven chapters, which will boost reader's confidence and developing motivation to work in this direction. Intended for postgraduate students and researchers in the field of fuzzy set theory and soft computing applications.

Key Features:

- Introduction to Fuzzy Sets and its Extensions
- Spherical Fuzzy Graph
- Introduction to *T*-Spherical Fuzzy Set
- *T*-Spherical Fuzzy Soft Matrices
- *T*-Spherical Fuzzy Soft Set
- *T*-Spherical Fuzzy Correlation Measures
- Eigen Spherical Fuzzy Set

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